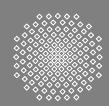


# Design of composite beams according to Eurocode 4-1-1

## Lecture: Ultimate Limit States

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## A short introduction



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# Design of composite beams according to Eurocode 4-1-1

## *Contents*

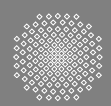
1 - SCOPE

2 - SPECIFIC CHARACTERISTICS OF STRUCTURAL ANALYSIS

3 - METHODS OF GLOBAL ANALYSIS

4 - VERIFICATION FOR BENDING AND SHEAR FOR ULS

5 - SHEAR CONNECTION



Car park,  
Messe Stuttgart

# Part 1: SCOPE



## Definitions according EN 1994-1-1 [§1.5.2]

### COMPOSITE MEMBER

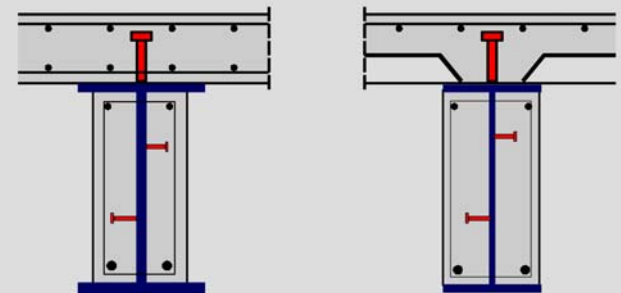
a structural member with components of **concrete** and of structural or cold-formed **steel**, interconnected by **shear connection** so as to limit the longitudinal slip between concrete and steel and the separation of one component from the other

### SHEAR CONNECTION

an interconnection between the concrete and steel components of a composite member that has sufficient strength and stiffness to enable the two components to be designed as parts of a single structural member

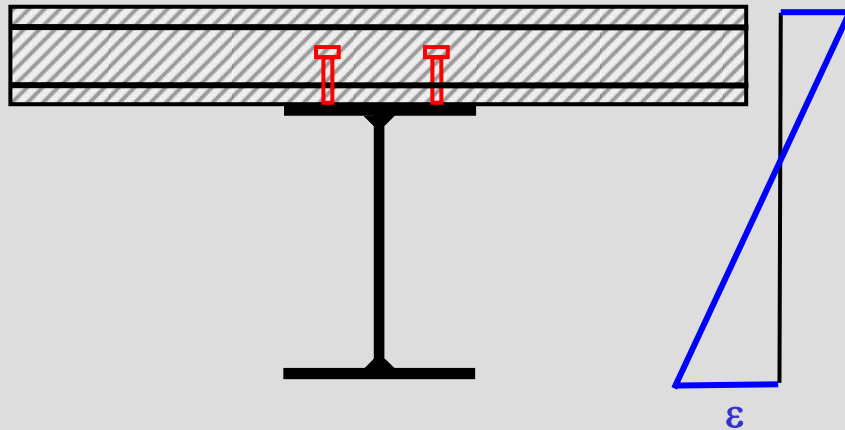
### COMPOSITE BEAM

a composite member subjected mainly to **bending**



## COMPOSITE BEHAVIOUR

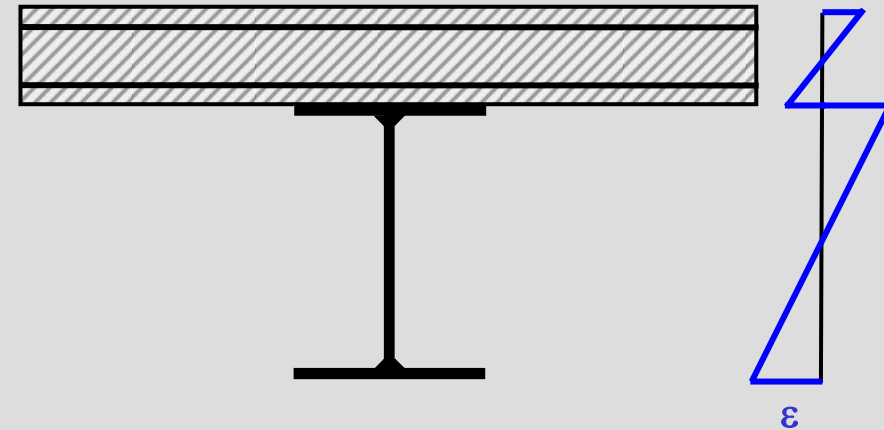
composite beam



composite behaviour

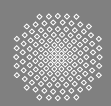
acting as *one* section

steel beam with concrete slab



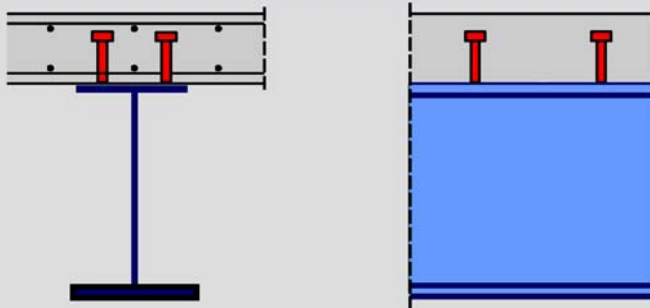
**no** composite behaviour

acting as *two individual sections*

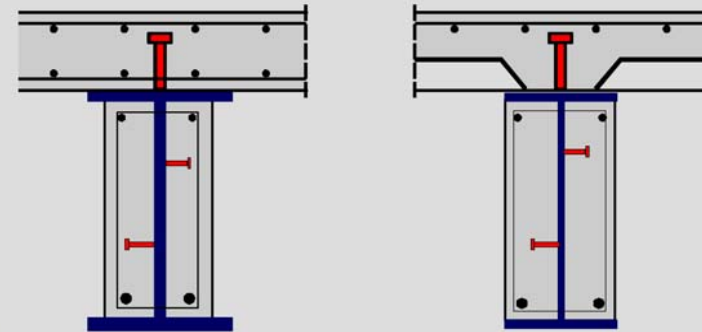


## TYPICAL COMPOSITE BEAMS

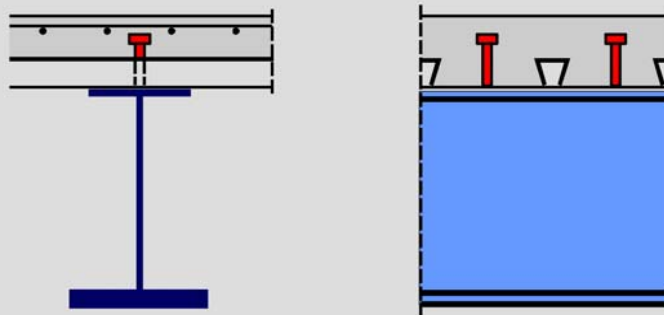
composite beam with solid slab



partially concrete encased beams



composite beam with composite slab



structural steel sections are rolled or welded

[Source: Hanswille]

## Materials according EN 1994-1-1 [§ 3]

### CONCRETE

> C 20/25; LC 20/25

< C 60/75; LC 60/75

### REINFORCEMENT

Acc. EN 1992-1-1 § 3.2

strength:  $400 \text{ N/mm}^2 \leq f_{y,k} \leq 600 \text{ N/mm}^2$

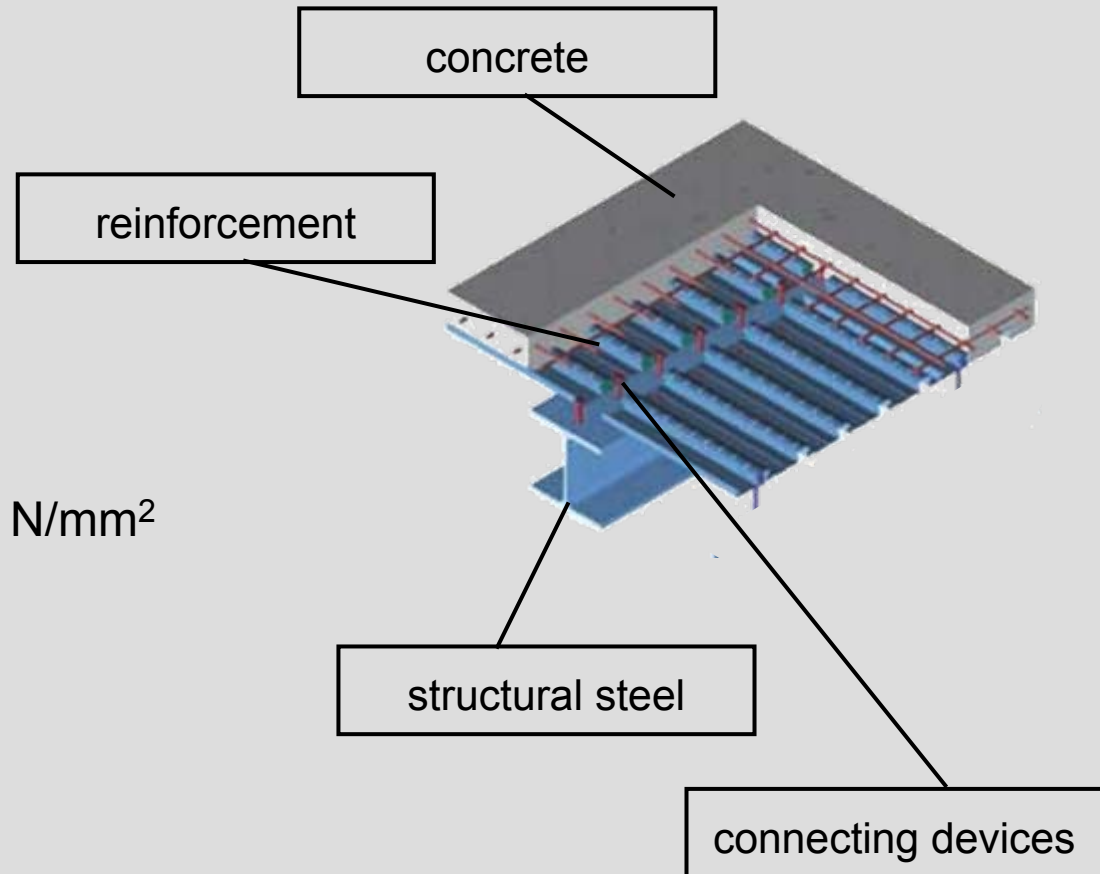
ductility:  $1,05 \leq (f_t/f_y)_k \leq 1,35$

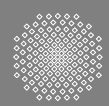
### STRUCTURAL STEEL

$f_y \leq 460 \text{ N/mm}^2$

### CONNECTING DEVICES

Headed stud shear connector acc. EN 13918





## Part 2:

# SPECIFIC CHARACTERISTICS OF STRUCTURAL ANALYSIS

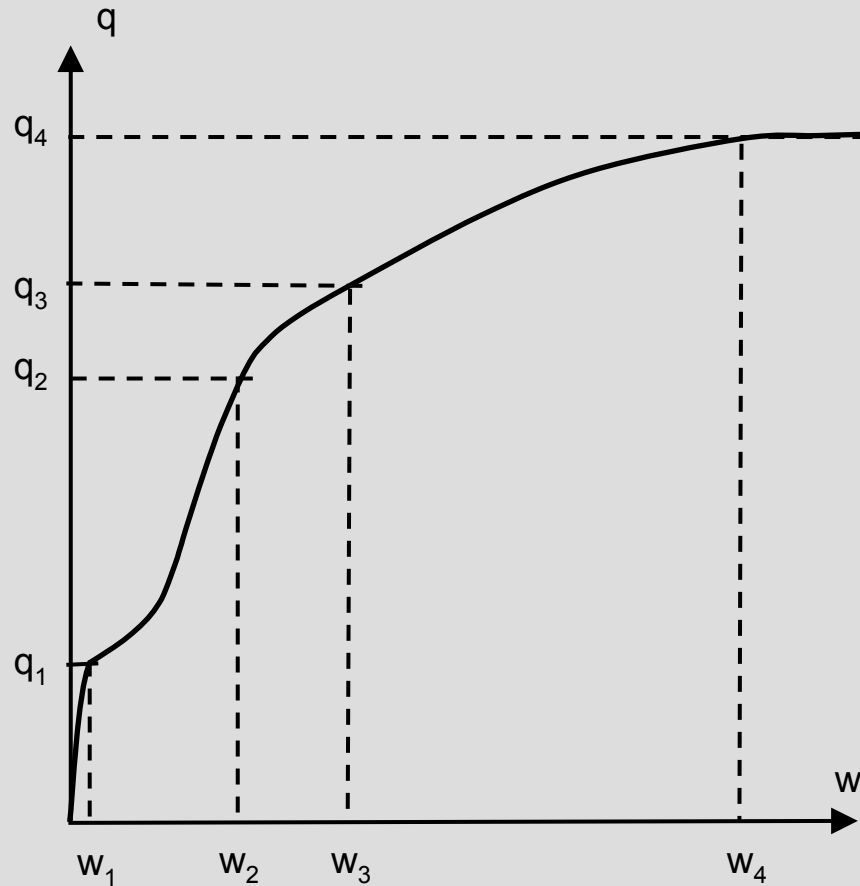


## Characteristics

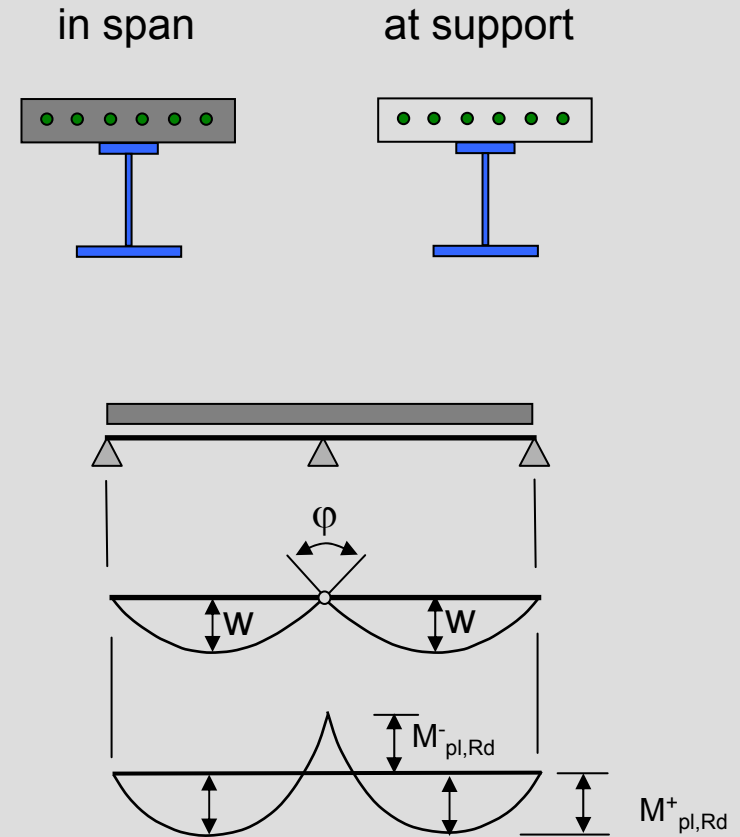
- Non-linear material behaviour
- Influence of erection and load history
- Influence of creep and shrinkage
- Influence of composite interaction



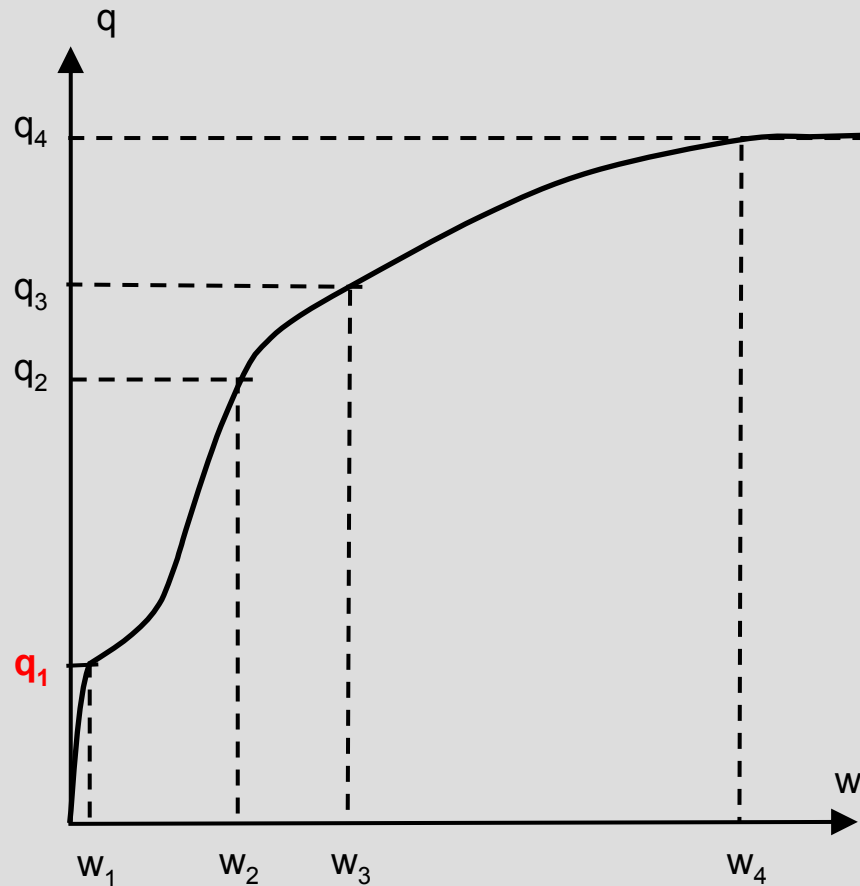
## Non-linear material behaviour



### Cross-section

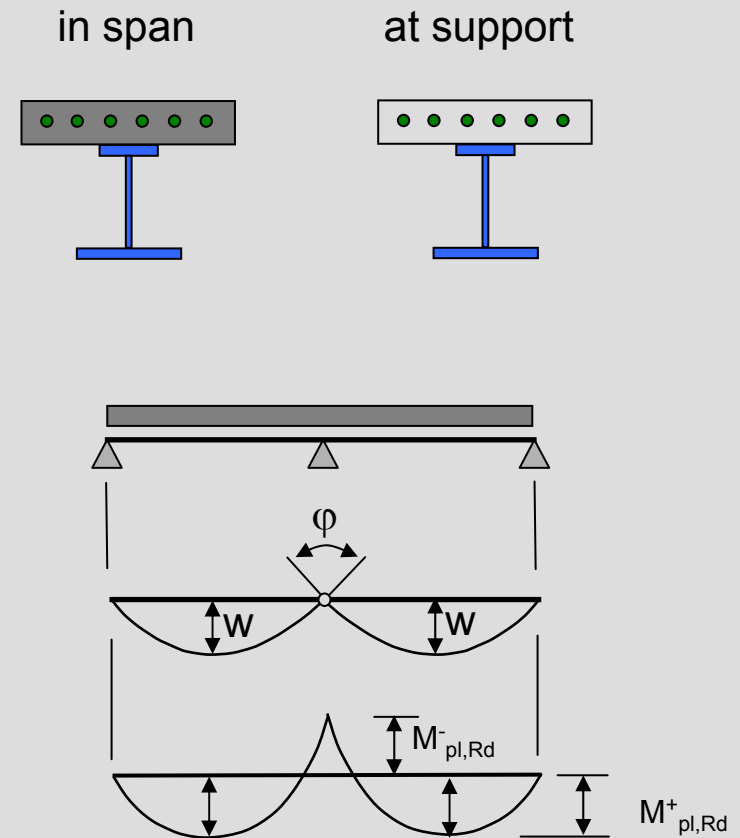


## Non-linear material behaviour

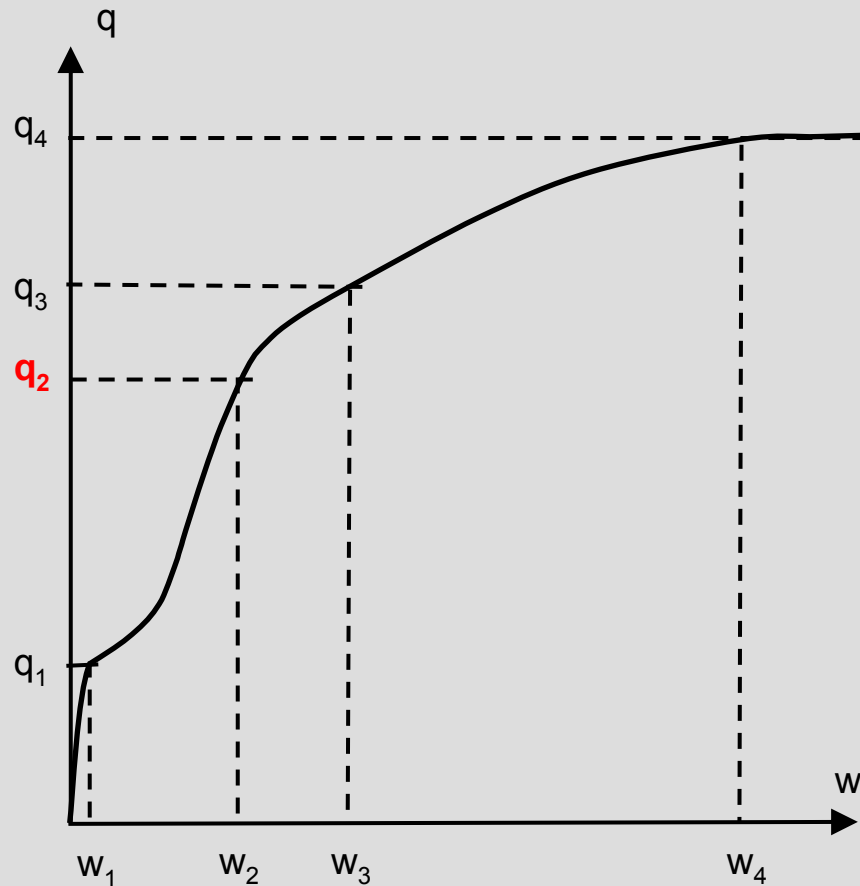


$q_1$  – first cracking (concrete slab) at support

### Cross-section

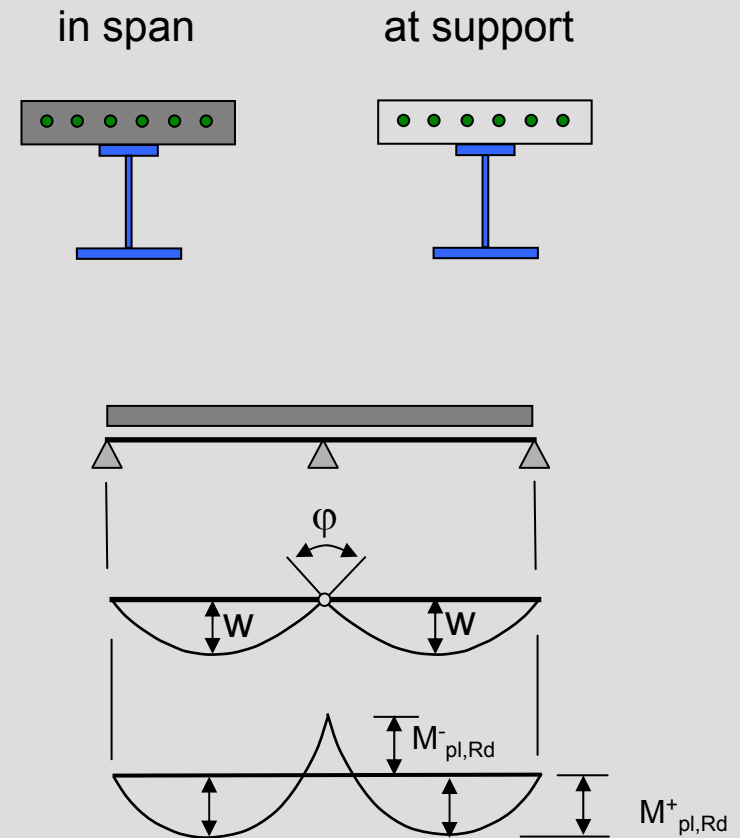


## Non-linear material behaviour

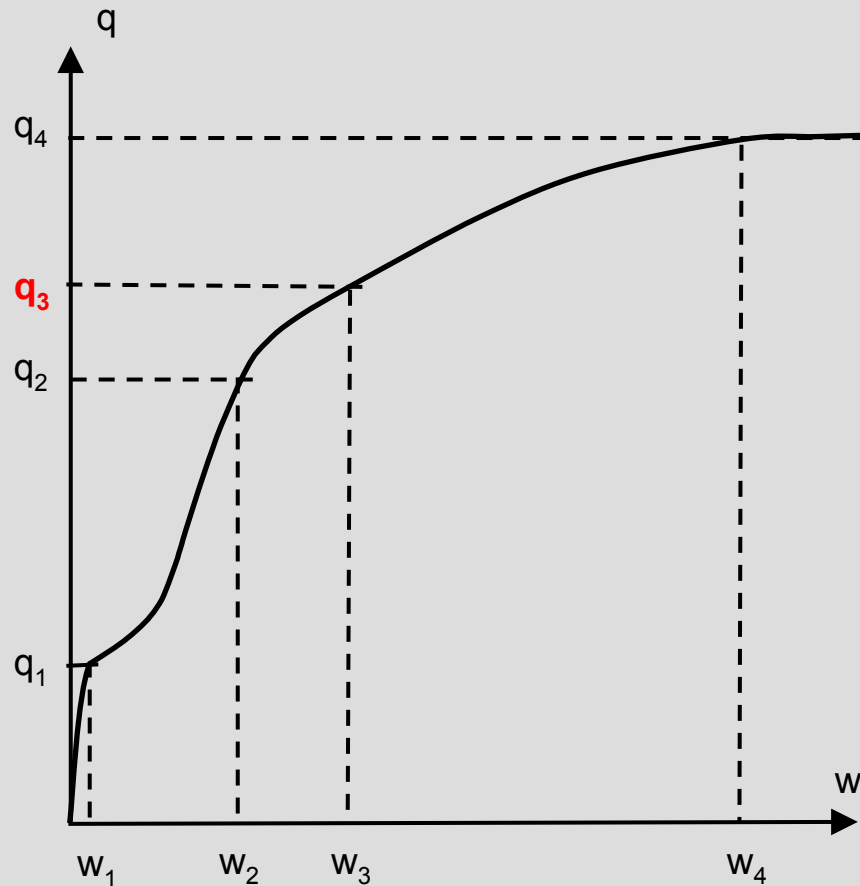


$q_2$  – first yielding (steel section) at support

### Cross-section

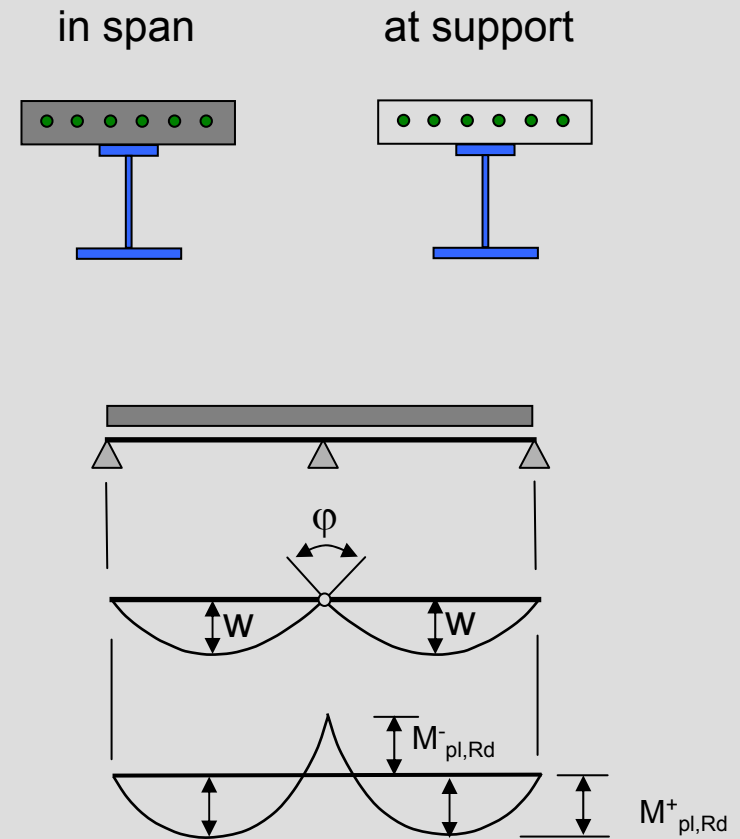


## Non-linear material behaviour

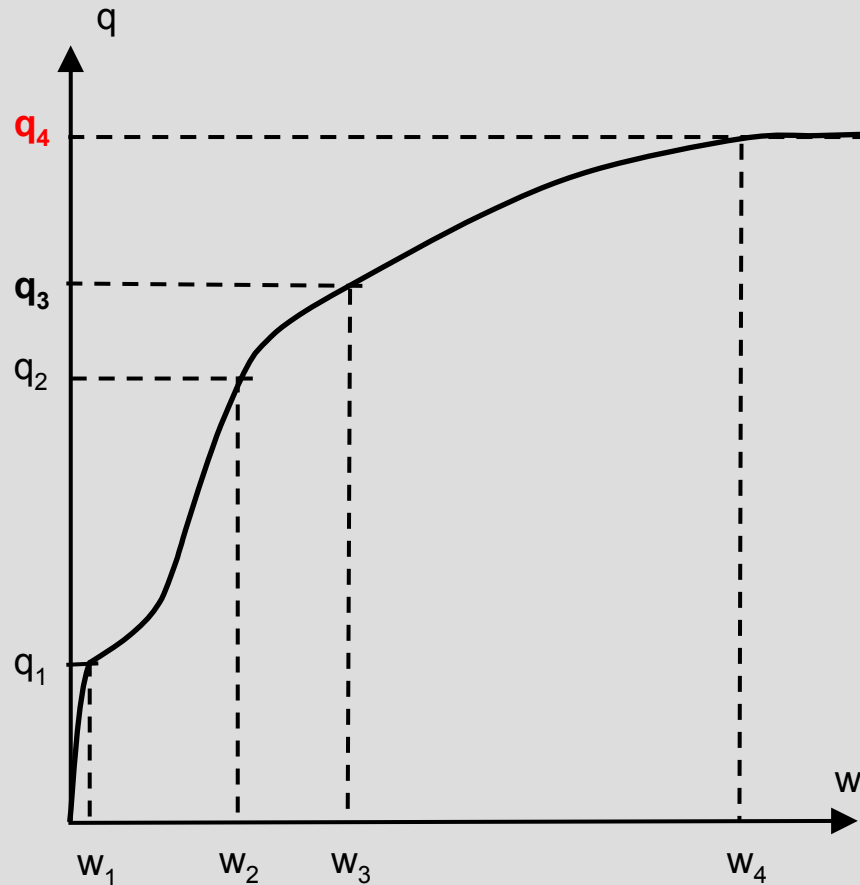


$q_3$  – first plastic hinge  $M_{pl,Rd}^-$  at support

### Cross-section

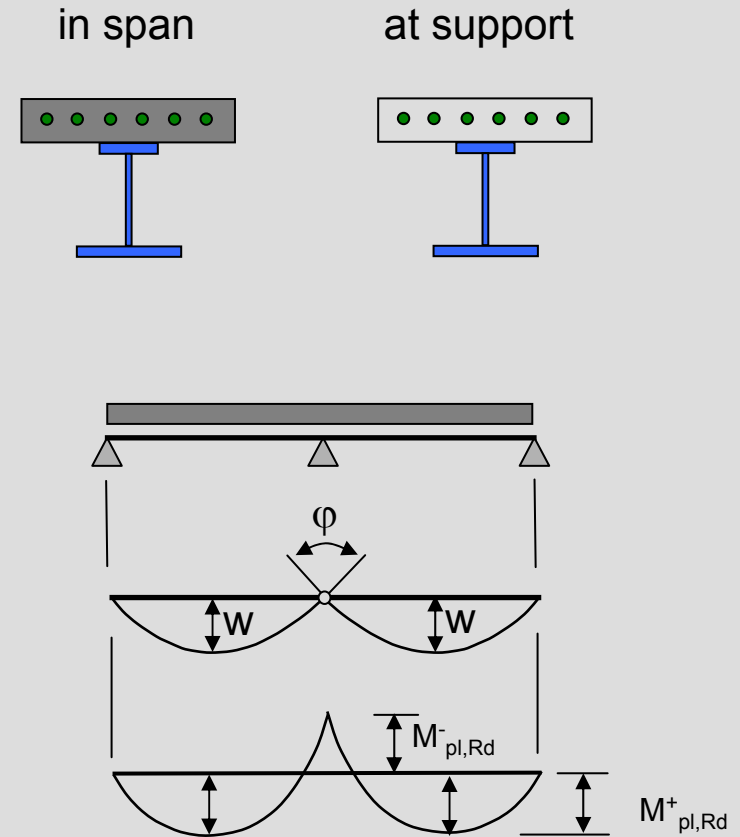


## Non-linear material behaviour

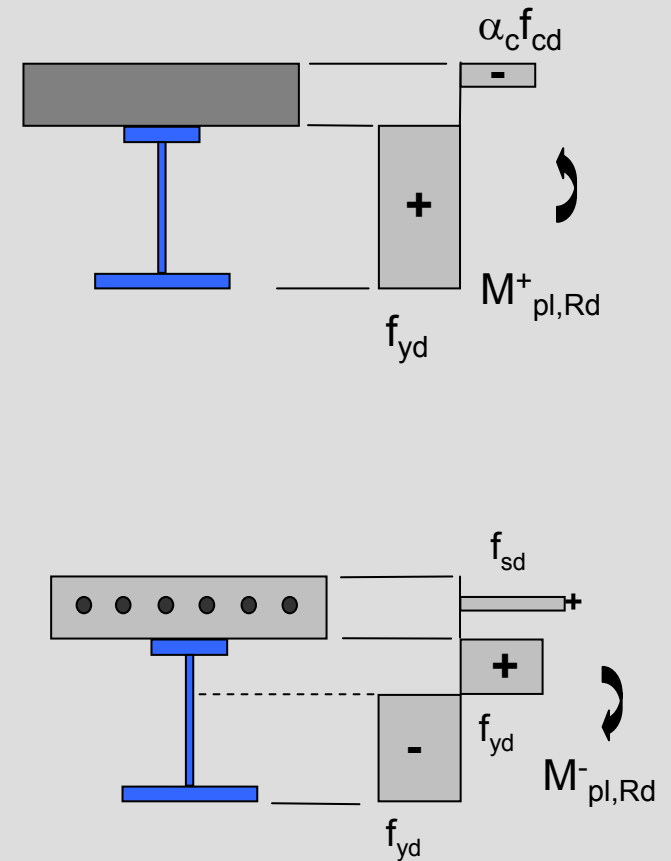
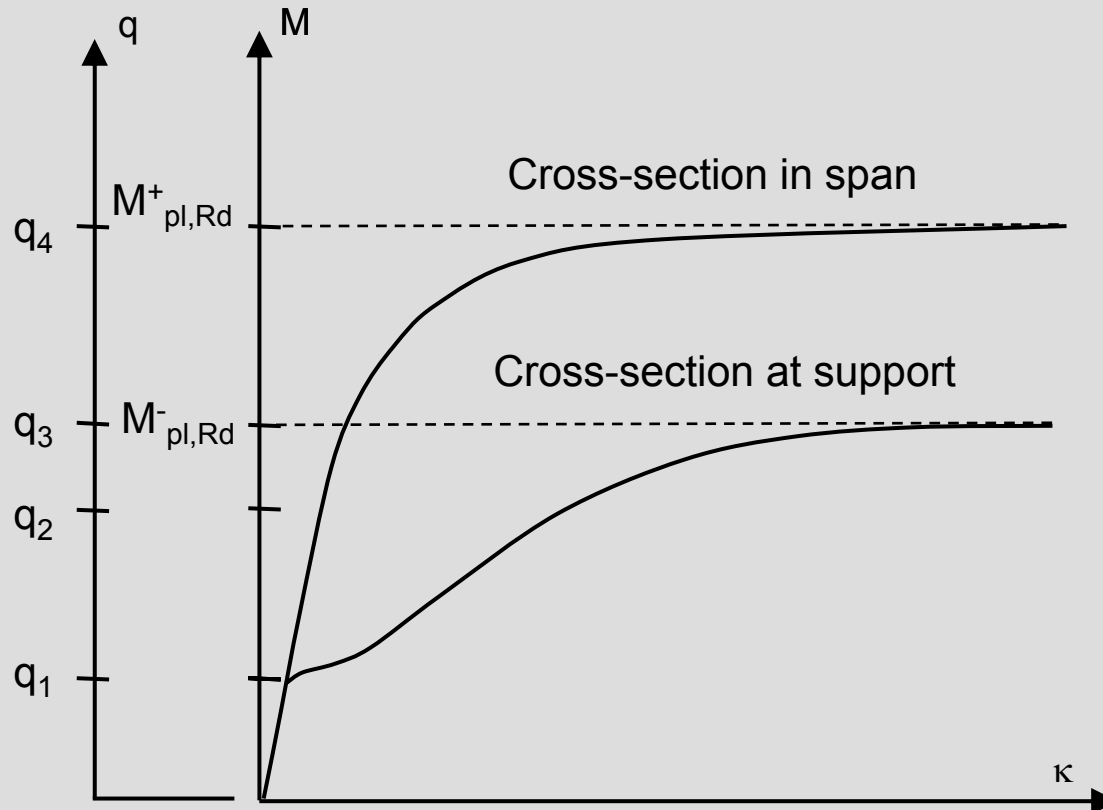


$q_4$  – last plastic hinge  $M_{pl,Rd}^+$  in span

### Cross-section

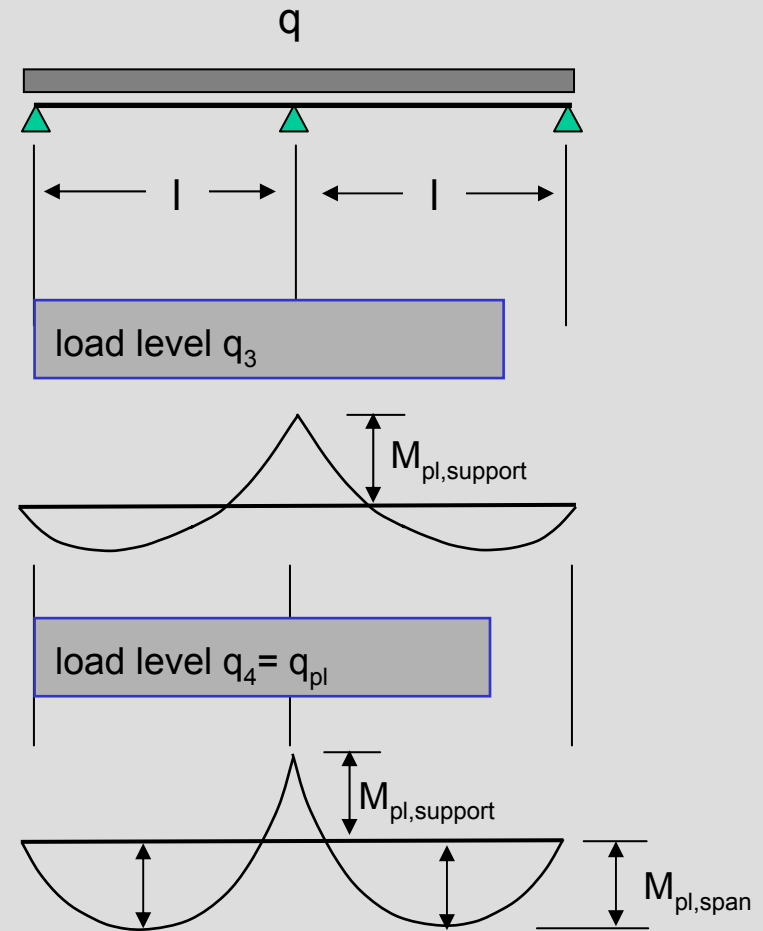
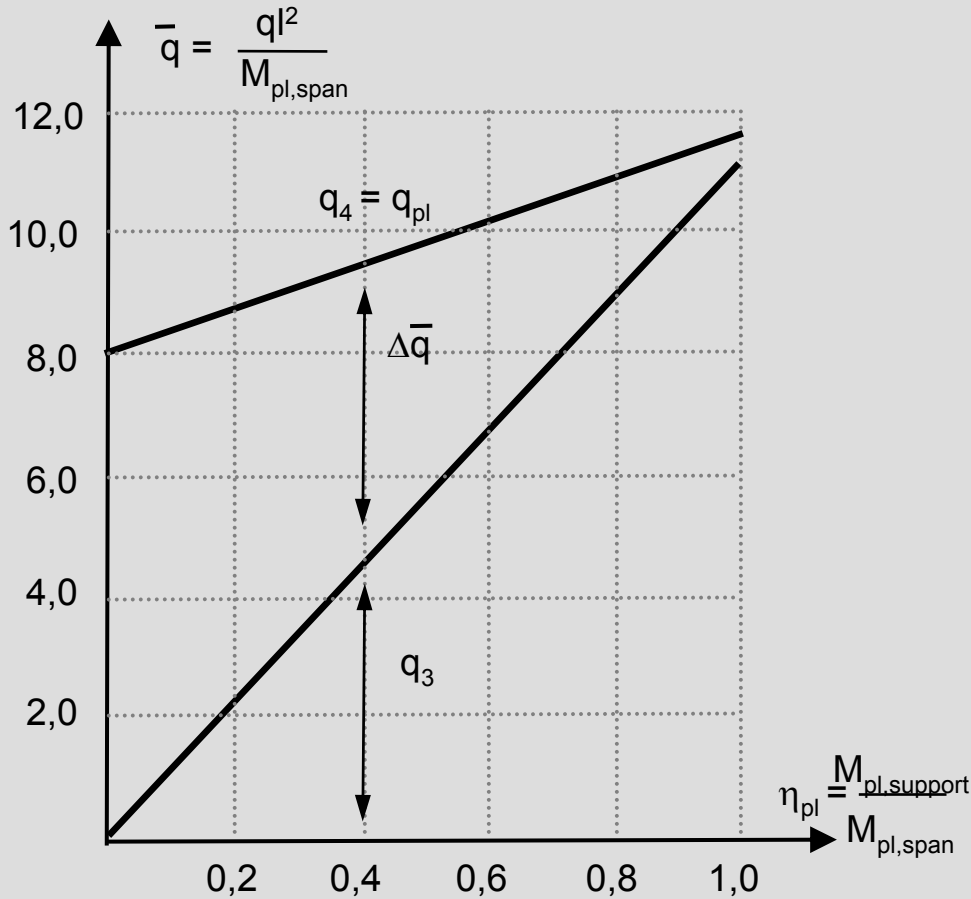


## Non-linear material behaviour



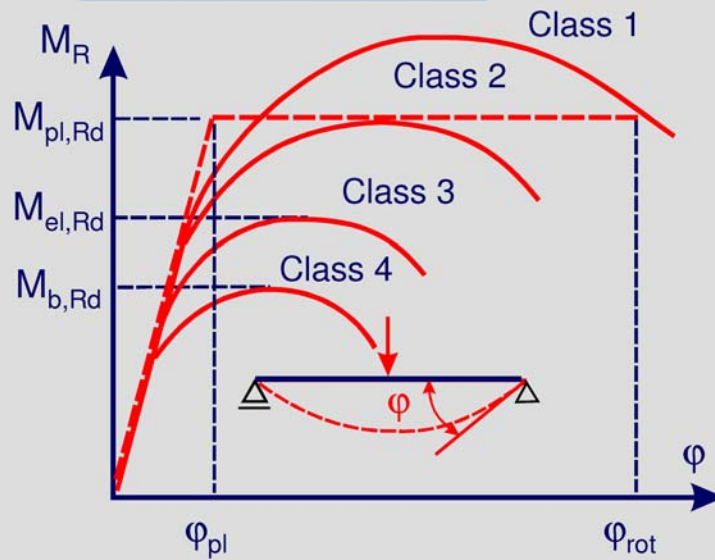


## Non-linear material behaviour

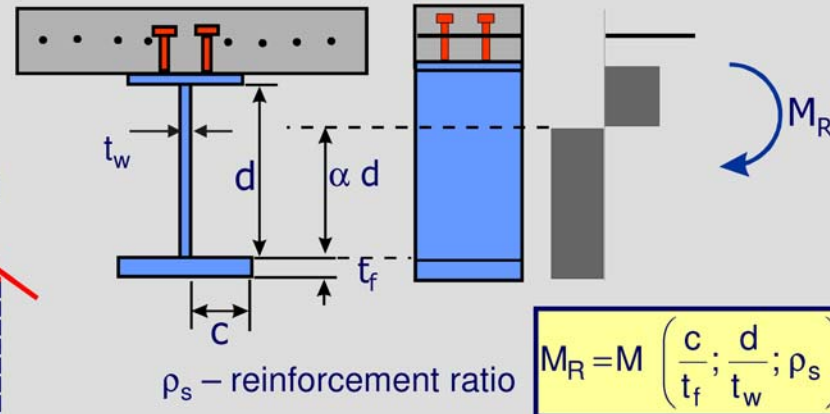


**High efficiency** of plastic hinge theory due to difference of plastic bending moment in span and at support - requires **rotation capacity** of section with first plastic hinge (at support)

## Non-linear material behaviour



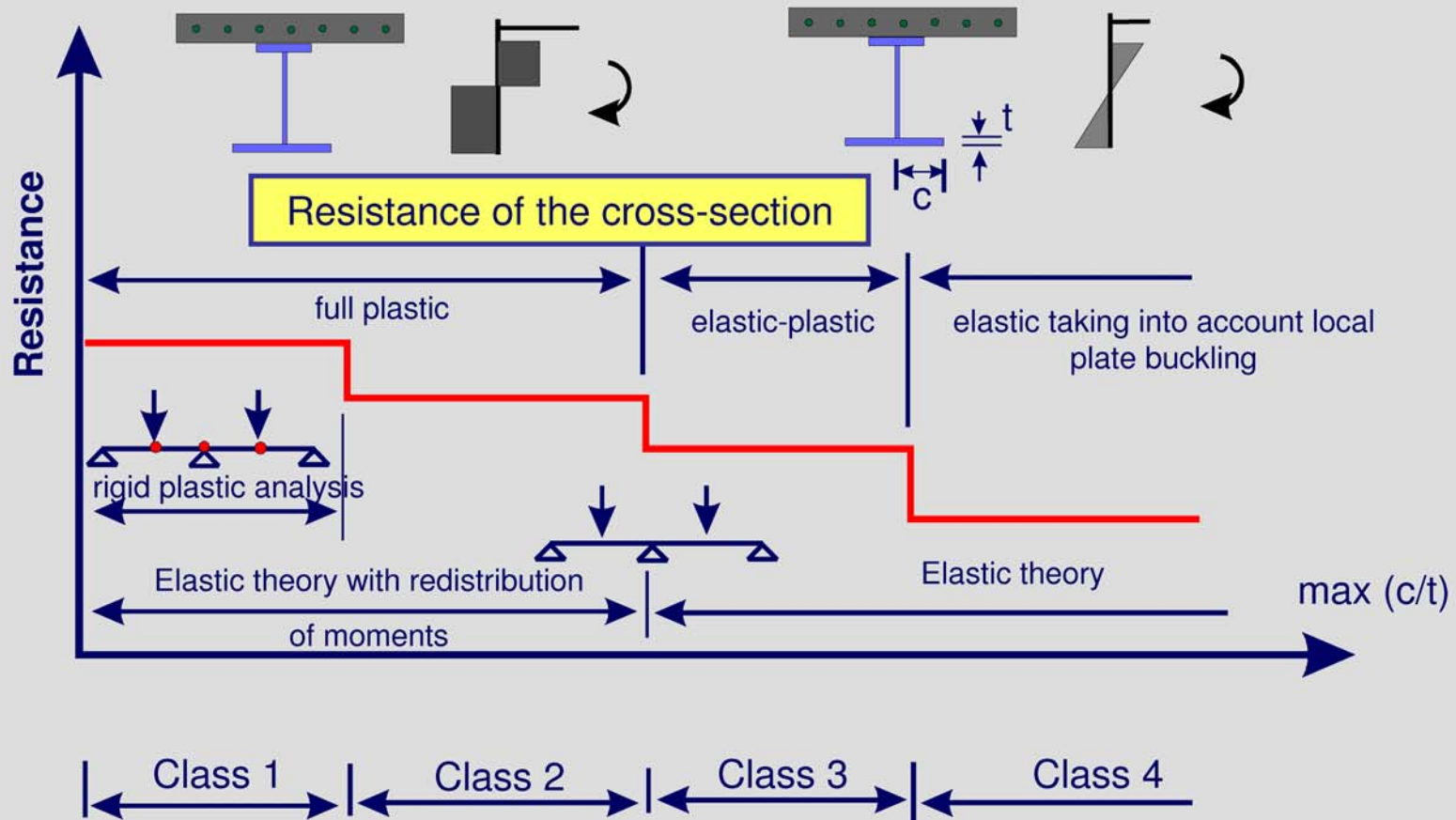
Rotation capacity: 
$$R = \frac{\varphi_{rot} - \varphi_{pl}}{\varphi_{pl}} = \frac{\varphi_{rot}}{\varphi_{pl}} - 1$$



Class	Bending resistance
1 and 2	plastic
3	elastic
4	elastic taking into account local buckling

[Source: Hanswille]

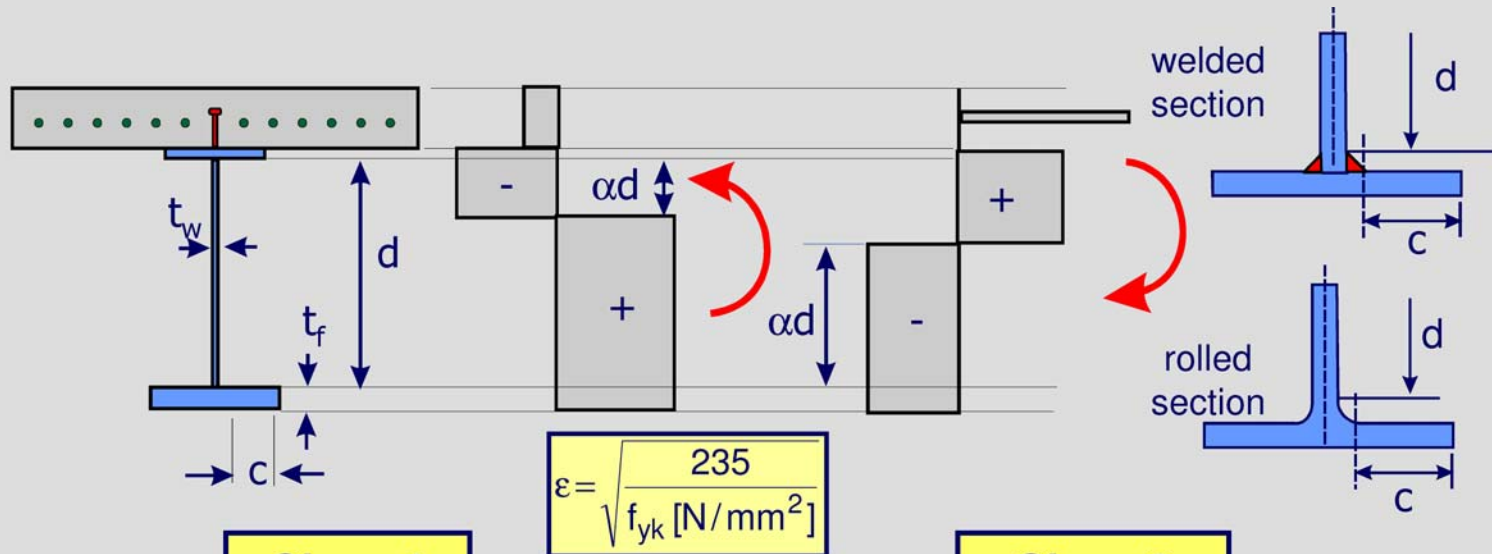
## Non-linear material behaviour



[Source: Hanswille]

## Non-linear material behaviour

## Classes 1 and 2



**Class 1**

**Class 2**

**web:**  $\frac{d}{t_w} \leq \frac{36 \epsilon}{\alpha}$  for  $\alpha \leq 0,5$

$\frac{d}{t_w} \leq \frac{396 \epsilon}{13 \alpha - 1}$  for  $\alpha > 0,5$

**flange:**  $c/t_f \leq 9\epsilon$

**web:**  $\frac{d}{t_w} \leq \frac{41,5 \epsilon}{\alpha}$  for  $\alpha \leq 0,5$

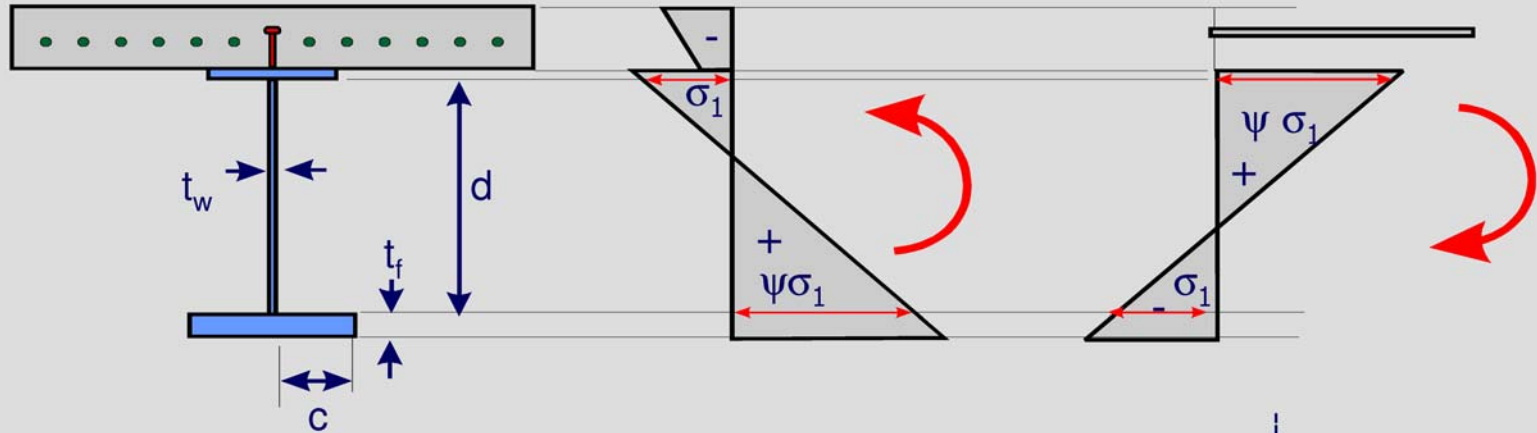
$\frac{d}{t_w} \leq \frac{456 \epsilon}{13 \alpha - 1}$  for  $\alpha > 0,5$

**flange:**  $c/t_f \leq 10\epsilon$

[Source: Hanswille]

## Non-linear material behaviour

## Class 3



web:

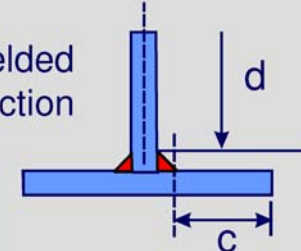
$$\text{for } \psi > -1,0: \quad \frac{d}{t_w} \leq \frac{42 \varepsilon}{0,67 + 0,33 \psi}$$

$$\text{for } \psi \leq -1,0: \quad \frac{d}{t_w} \leq 0,62 \varepsilon (1 - \psi) \sqrt{-\psi}$$

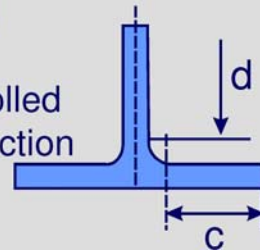
flange:  $c/t_f \leq 14\varepsilon$

$$\varepsilon = \sqrt{\frac{235}{f_{yk} [\text{N/mm}^2]}}$$

welded section

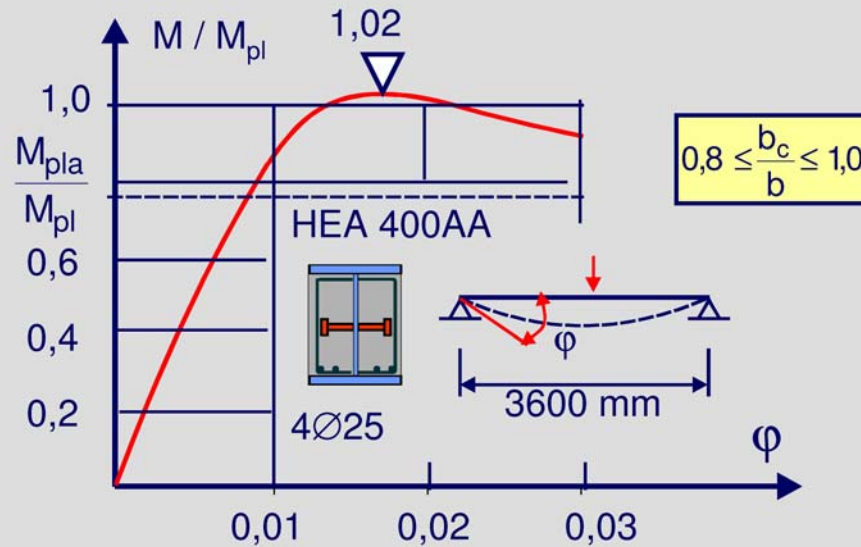


rolled section

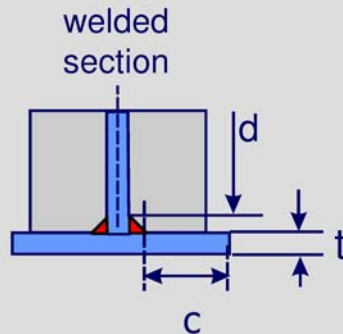


[Source: Hanswille]

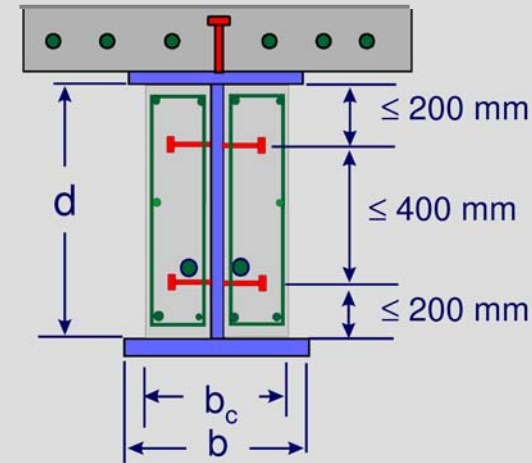
## Non-linear material behaviour



A steel web in class 3 may be represented by an effective web of the same cross-section in Class 2



## Classification with partial concrete encasement



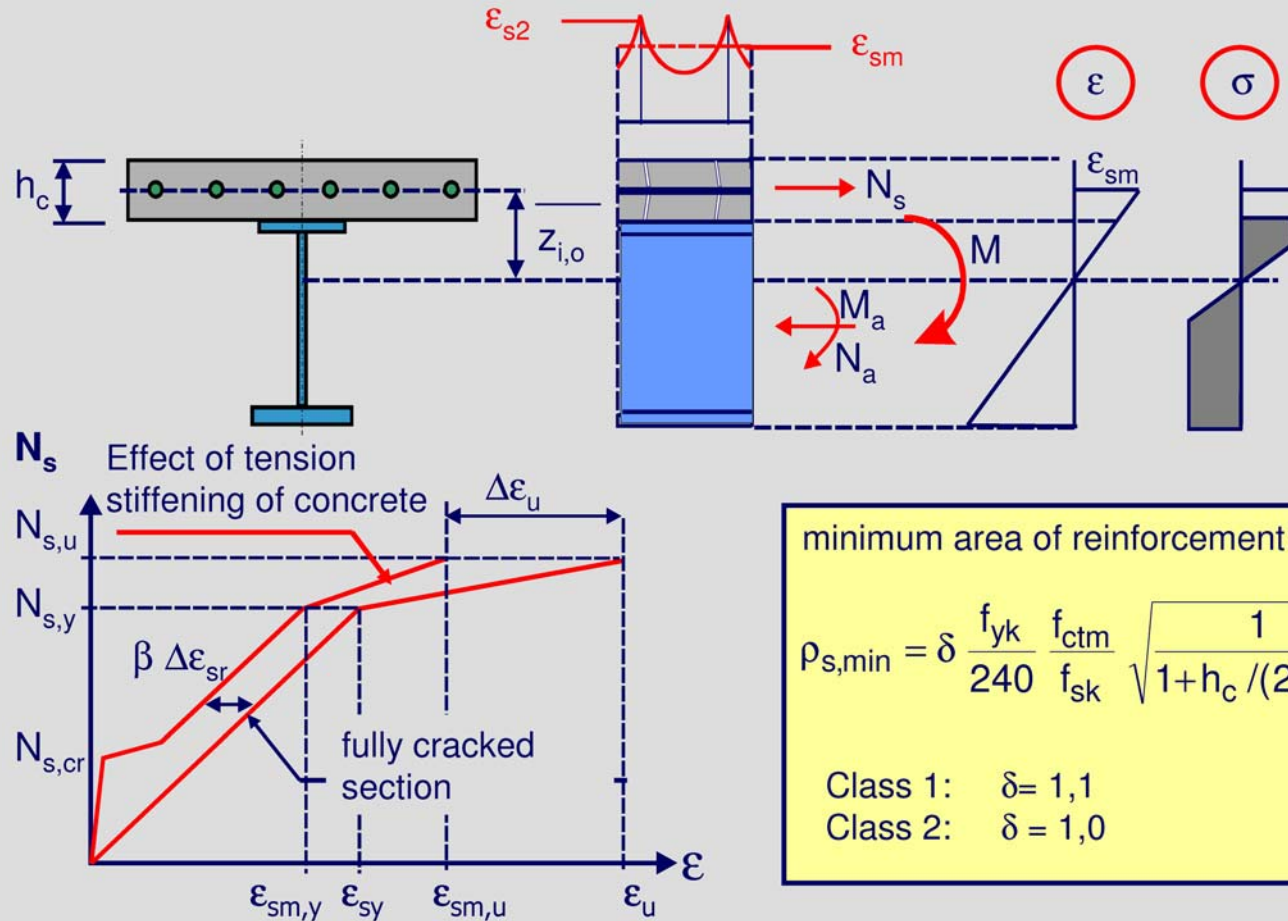
compression flanges	
Class	max $c/t_f$
1	$9\epsilon$
2	$14\epsilon$
3	$20\epsilon$

[Source: Hanswille]



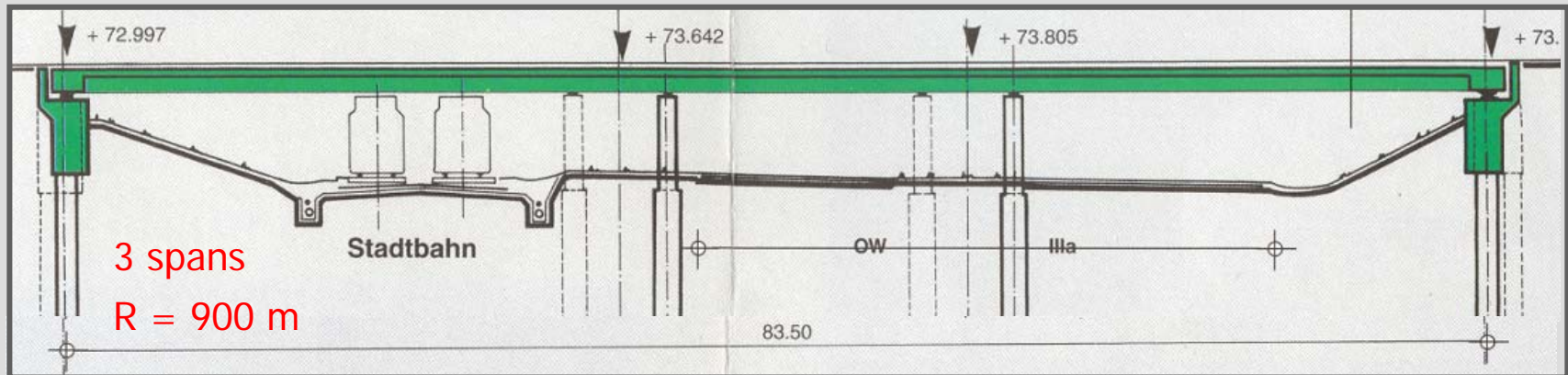
## Non-linear material behaviour

## Reinforcement in tension flanges



[Source: Hanswille]

## Influence of erection and load history



### Example:

Bridge Arminiusstraße in Dortmund

- erection steel structure





## Influence of erection and load history

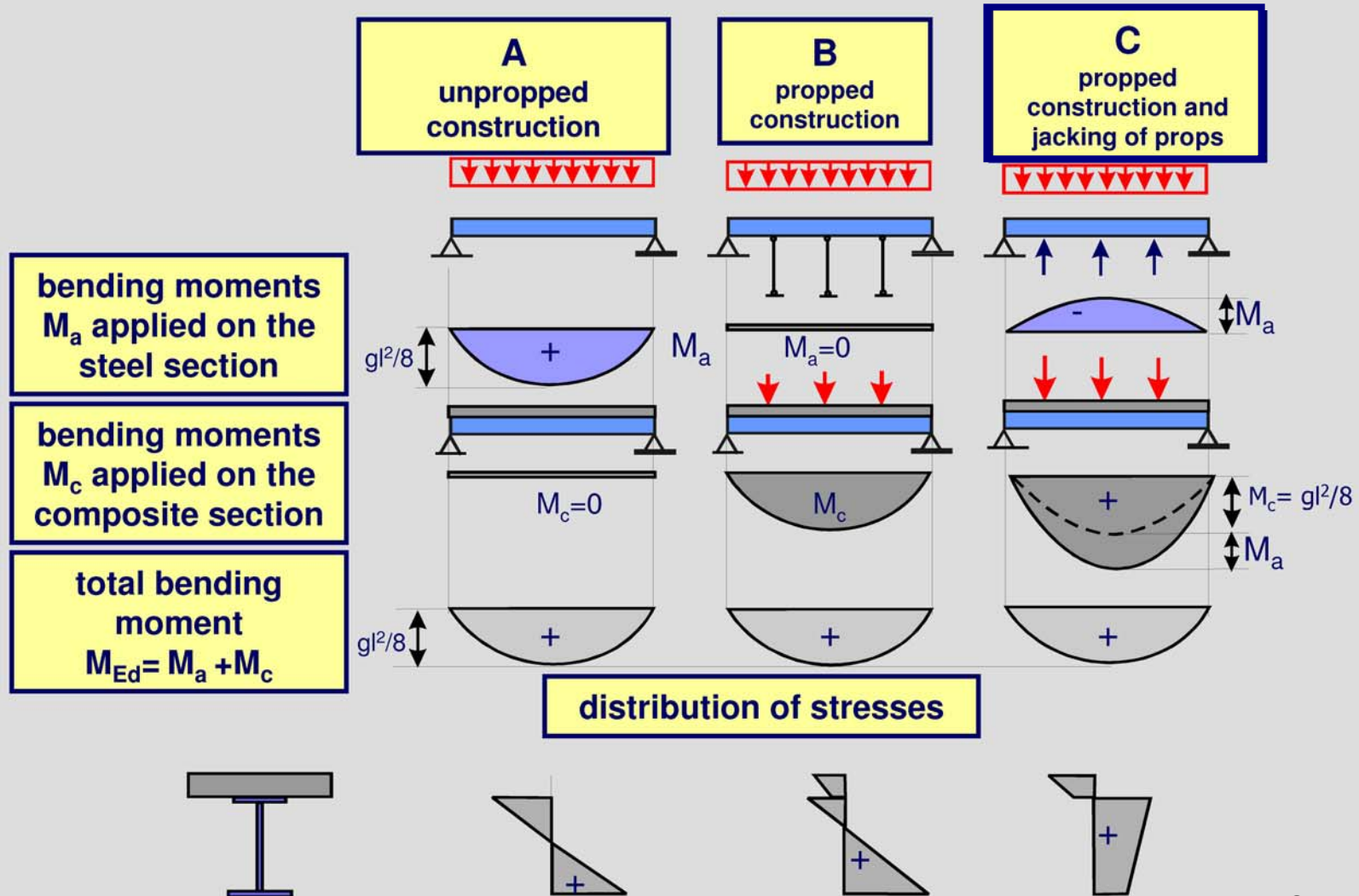
### Example:

Bridge Arminiusstraße in Dortmund

- raising at inner supports
- scaffolding hanging at steel structure
- concreting and hardening of concrete
- lowering at inner supports
- finalizing (pavement etc.)
- traffic opening

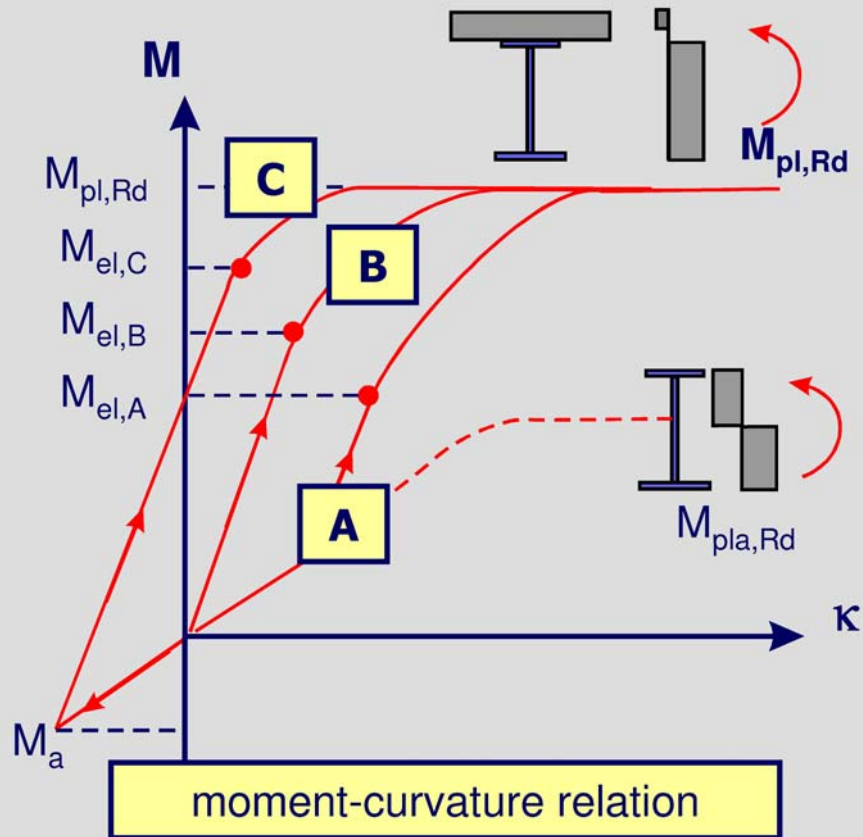


## Influence of erection and load history



[Source: Hanswille]

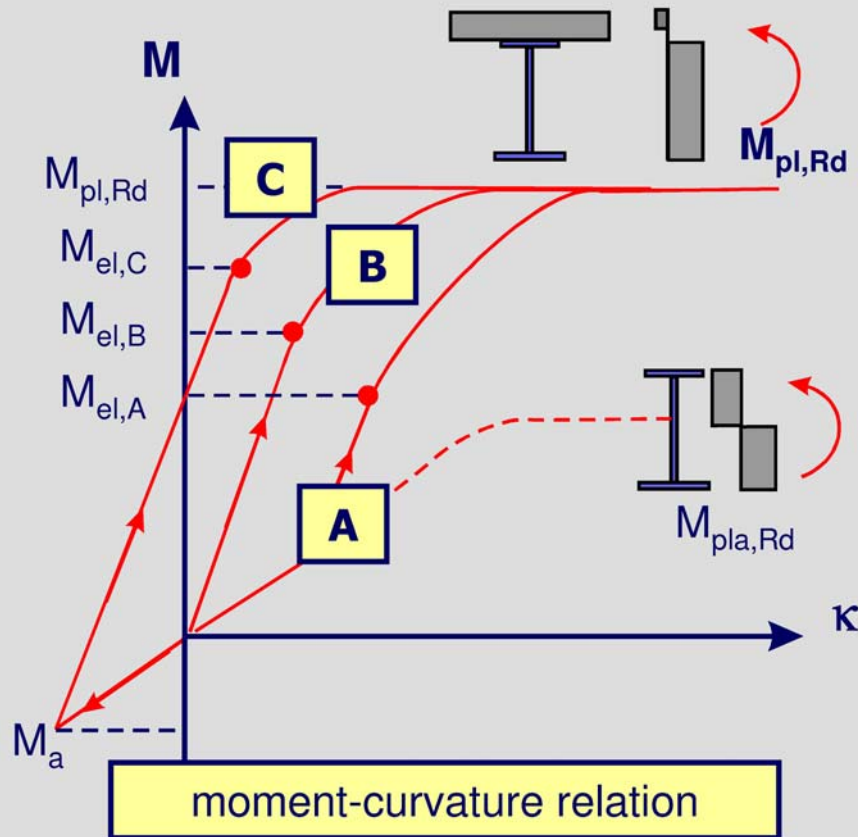
## Influence of erection and load history



- A** unpropped construction
- B** propped construction
- C** propped construction + jacking of props

[Source: Hanswille]

## Influence of erection and load history



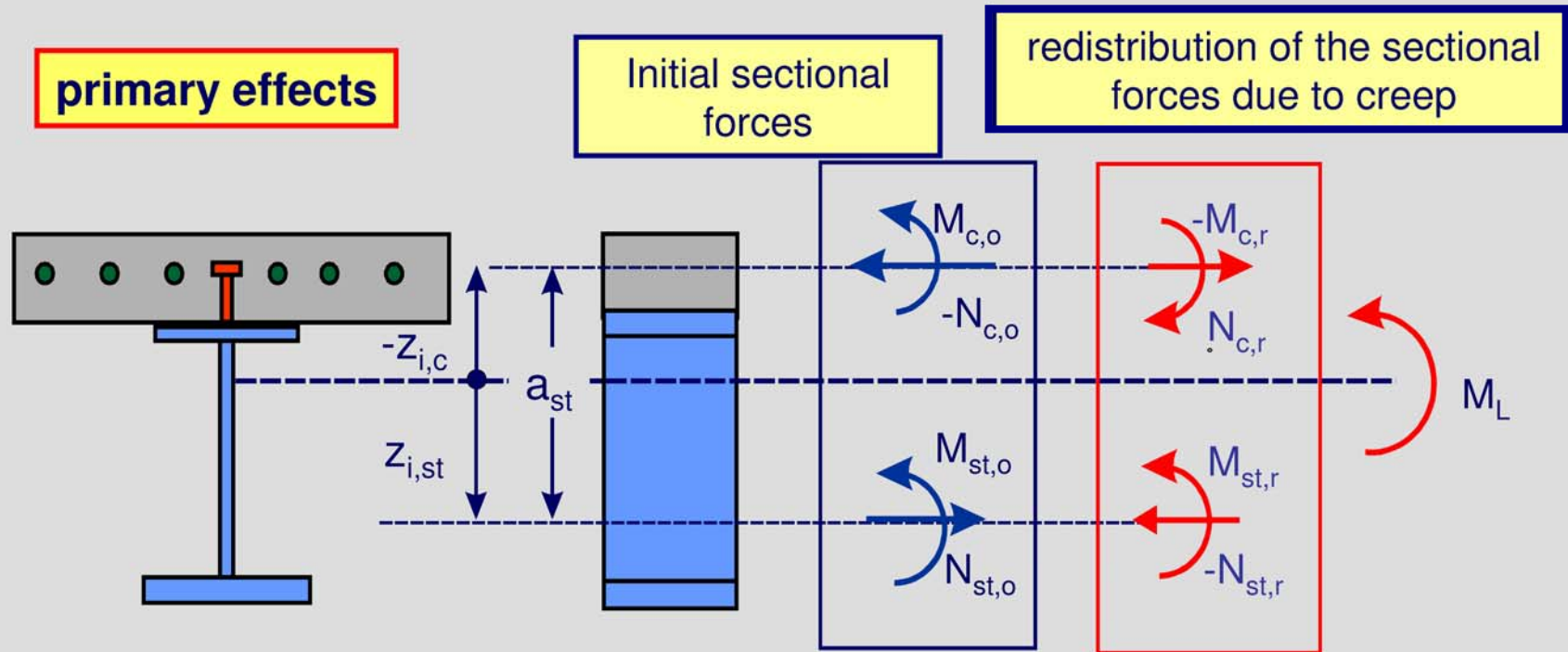
The bending capacity  $M_{pl,Rd}$  is independent of the loading history in case of Class 1 or Class 2 cross sections

Using Class 3 or Class 4 cross sections the elastic behaviour of the loading history has to be taken into account in ULS

[Source: Hanswille]



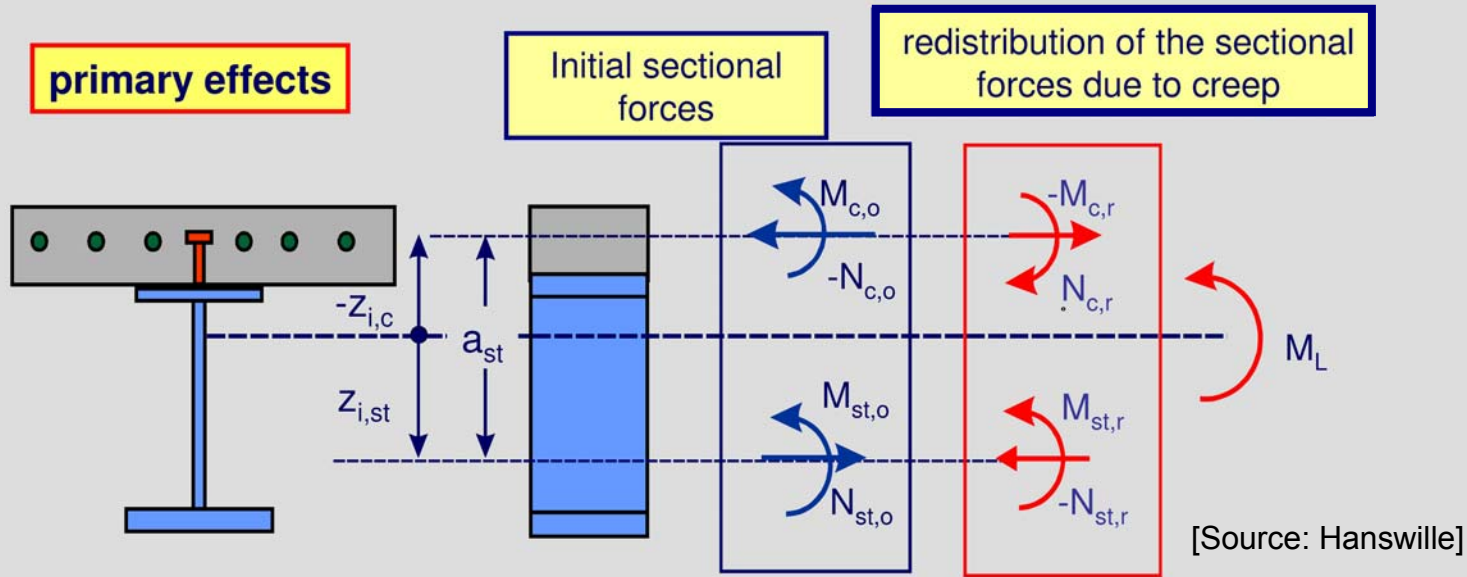
## Influence of creep and shrinkage



The effects of shrinkage and creep of concrete result in internal forces in cross sections, and curvatures and longitudinal strains in members

[Source: Hanswille]

## Influence of creep and shrinkage



Due to creep and shrinkage:

For statically determinate structures:

only external deformations

For Class 1 and 2 sections

bending capacity independent of creep and shrinkage

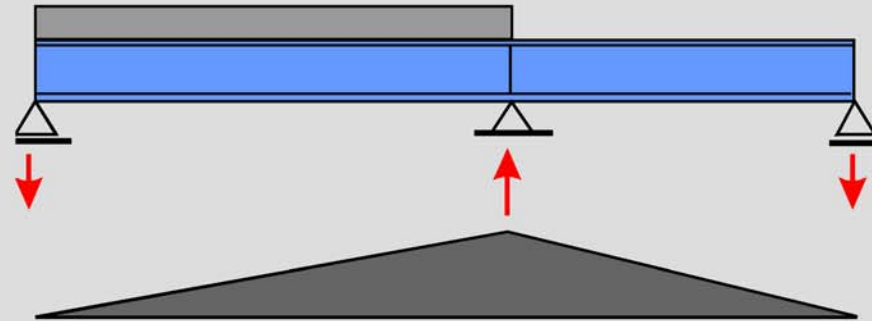
For Class 3 and 4 sections

creep and shrinkage has to be considered

## Influence of creep and shrinkage

### secondary effects

time - dependent statically  
indeterminate effects

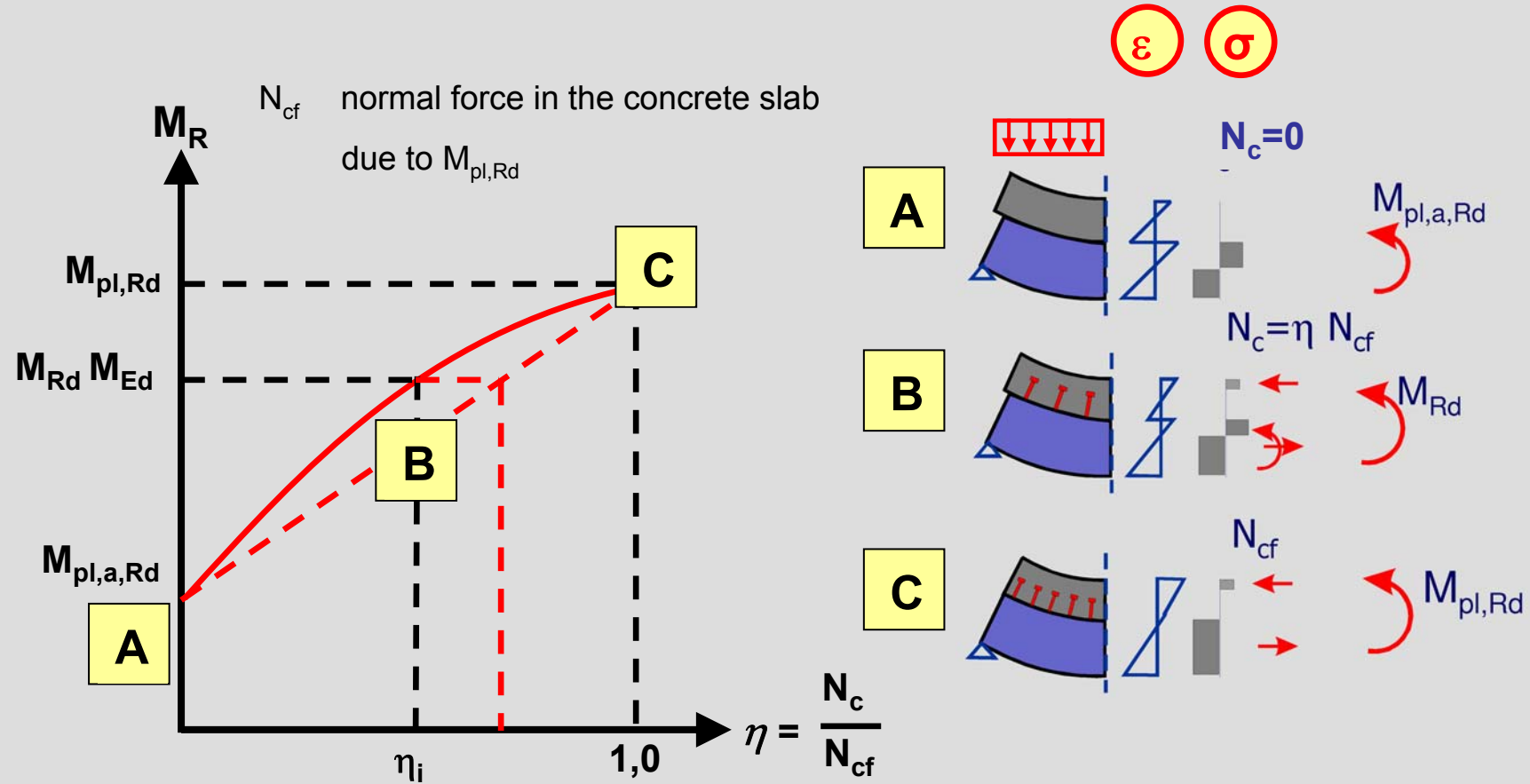


[Source: Hanswille]

In statically indeterminate structures the primary effects of shrinkage and creep are associated with additional **action effects**, such that the total effects are compatible;

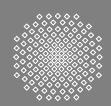
These shall be classified as secondary effects and **shall be considered** as indirect actions in any case

## Influence of composite interaction

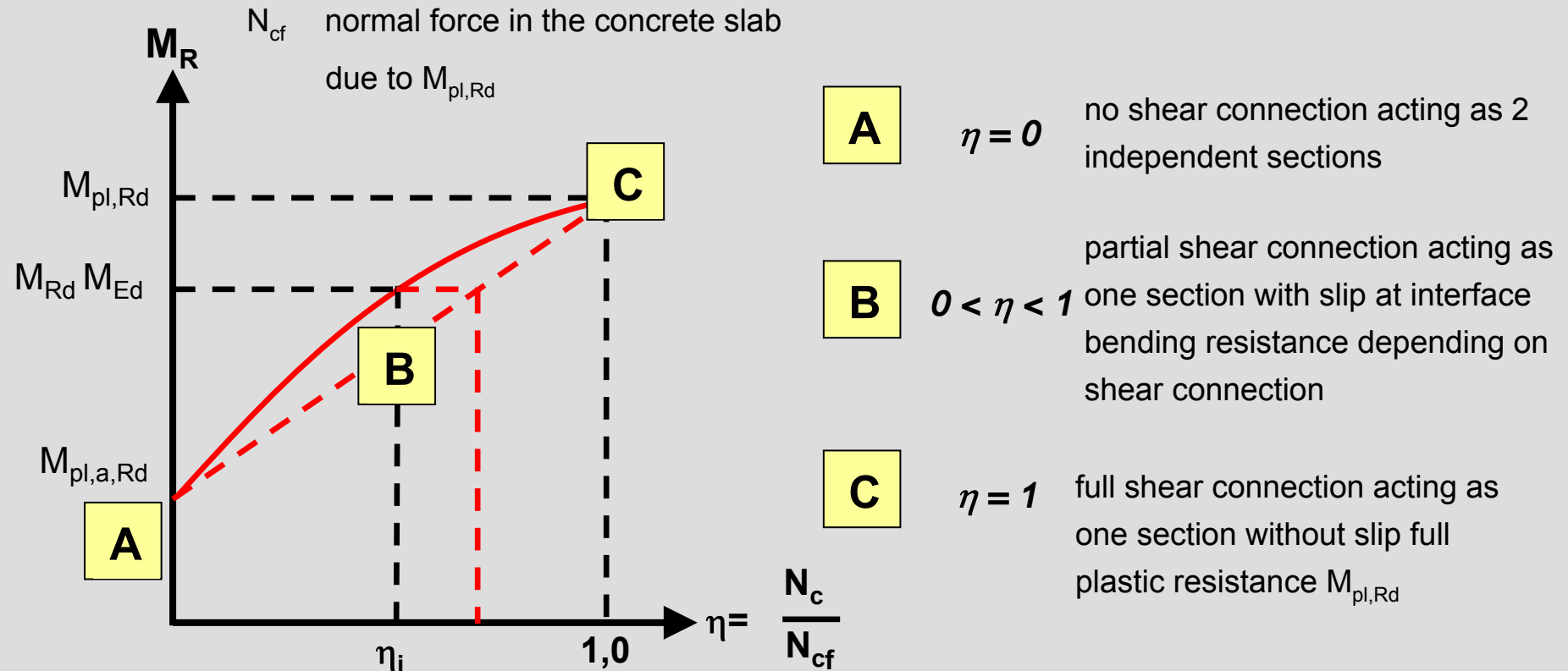


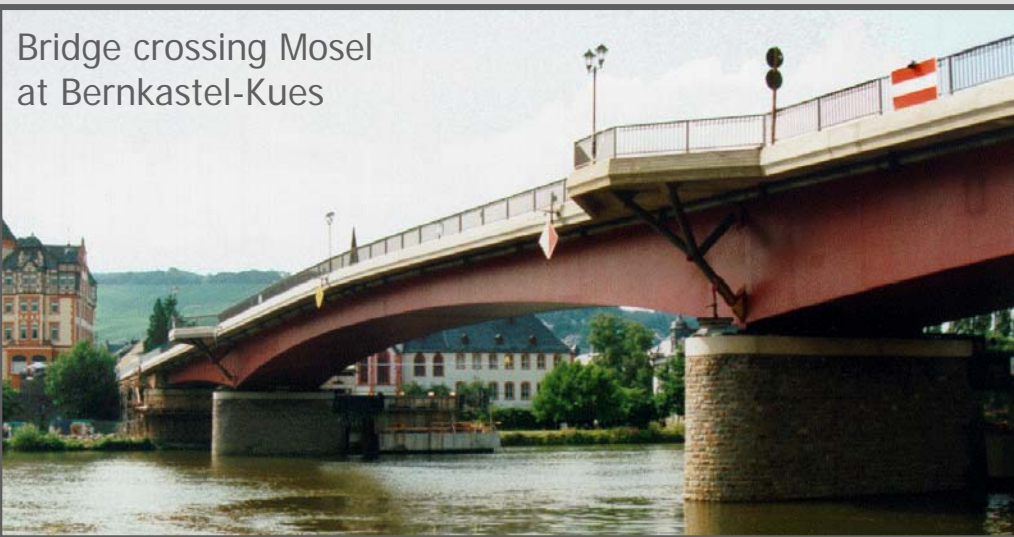
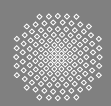
$\eta$ ...degree of shear connections

[Source: Hanswille]



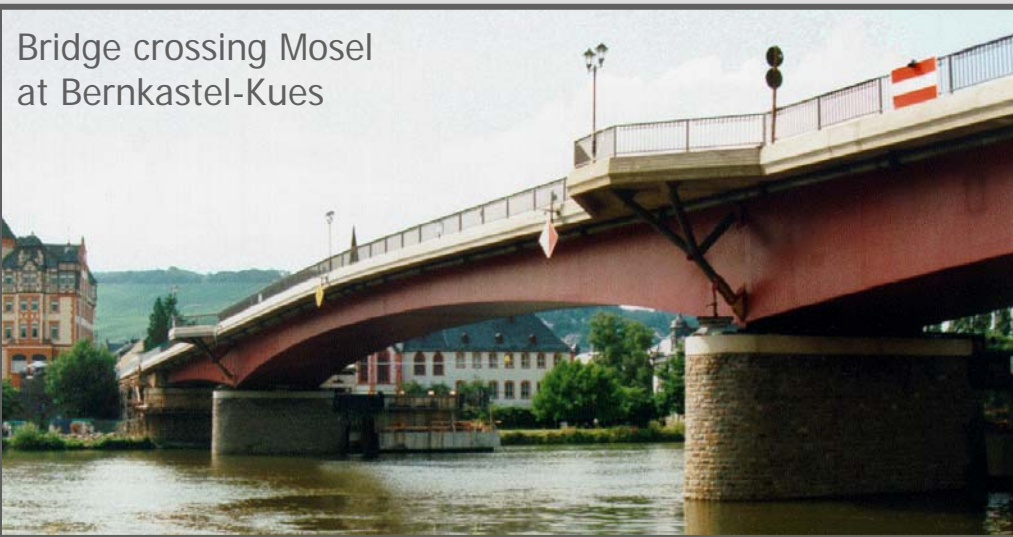
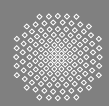
## Influence of composite interaction





## Part 3:

# METHODS OF GLOBAL ANALYSIS



- Structural stability
- Calculation of action effects  
based on elastic theory
- Rigid plastic analysis
- Stresses based on elastic theory

## Structural stability

General case

- Portal frames w/ shallow roof slopes
- Beam-and-column type plane frames

$$\alpha_{cr} = \frac{F_{cr}}{F_{Ed}} \geq 10$$

undeformed geometry

$$\alpha_{cr} = \left( \frac{H_{Ed}}{V_{Ed}} \right) \left( \frac{h}{\delta_{H,Ed}} \right) \geq 10$$

5.2.1(3)

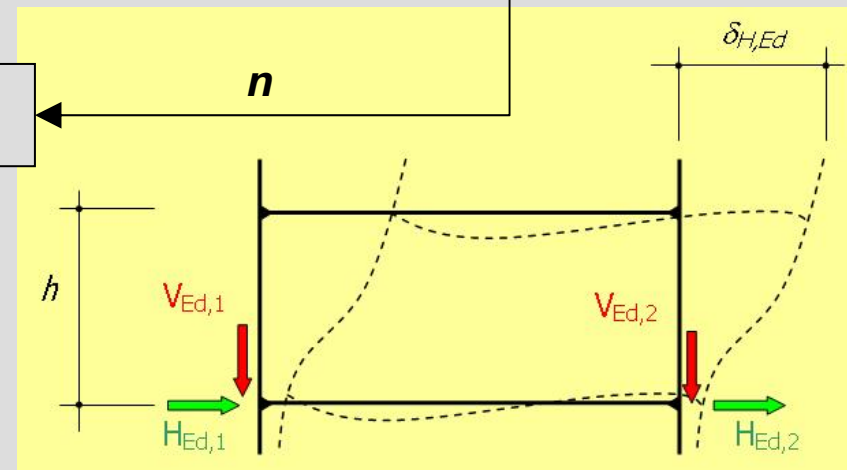
5.2.1(4)B

*n*

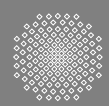
deformed geometry

*n*

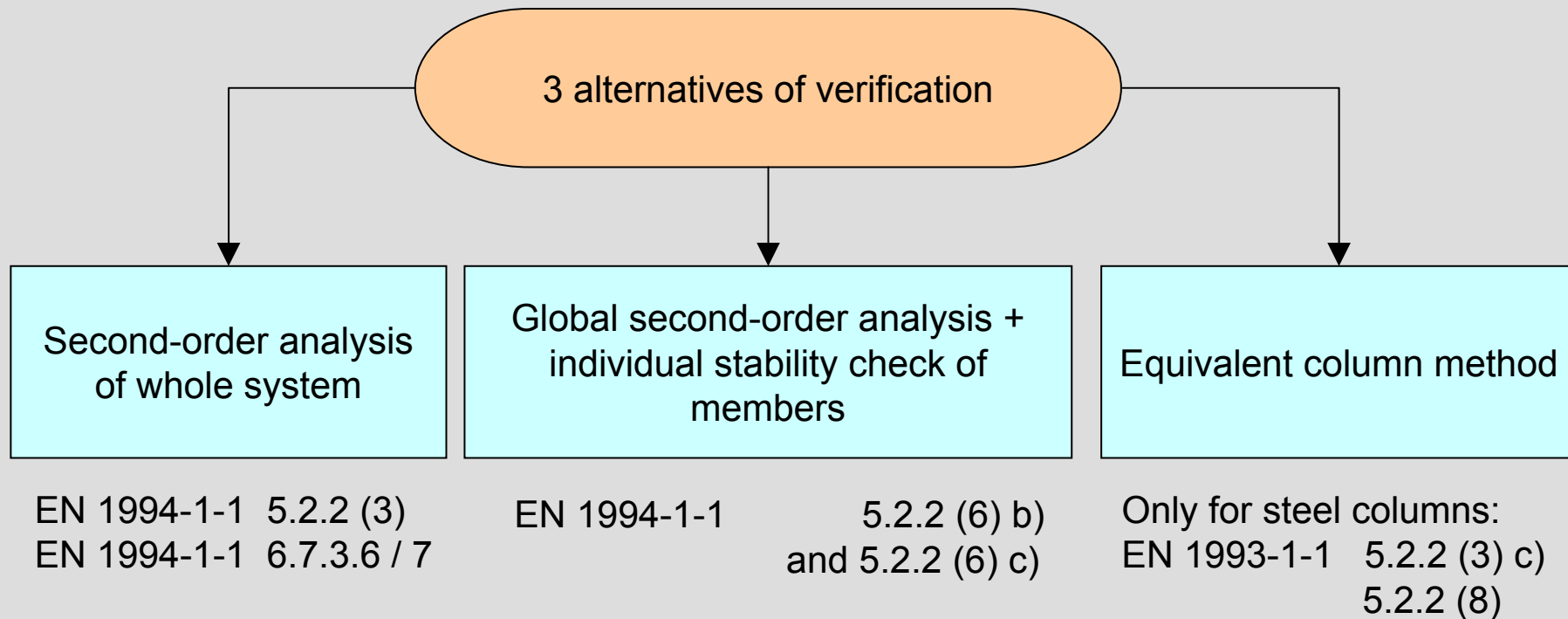
3 alternatives of verification







## Structural stability

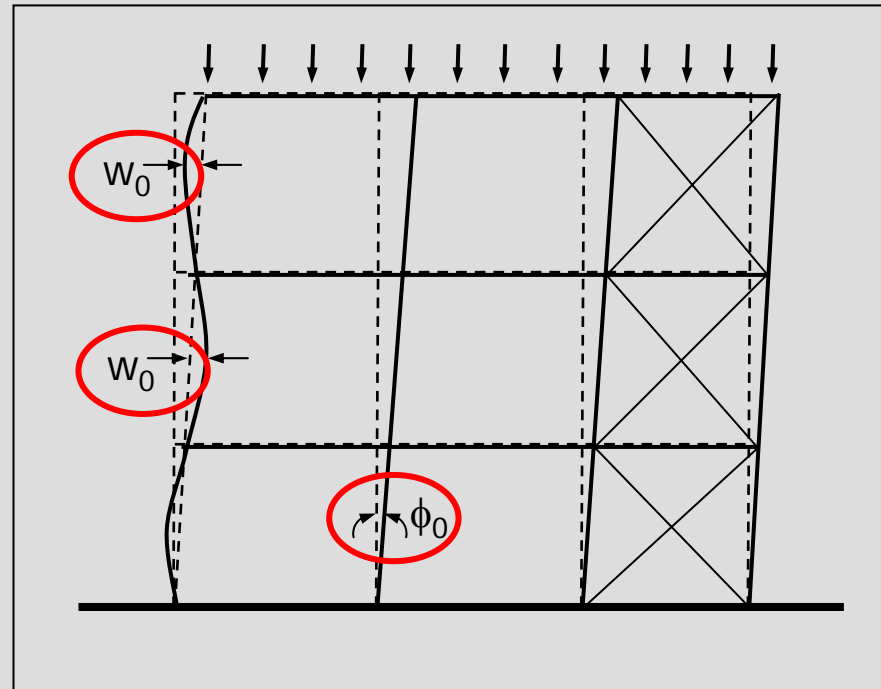


## Structural stability

3 alternatives of verification

Second-order analysis  
of whole system

accounting for  
global and local  
imperfections



## Structural stability

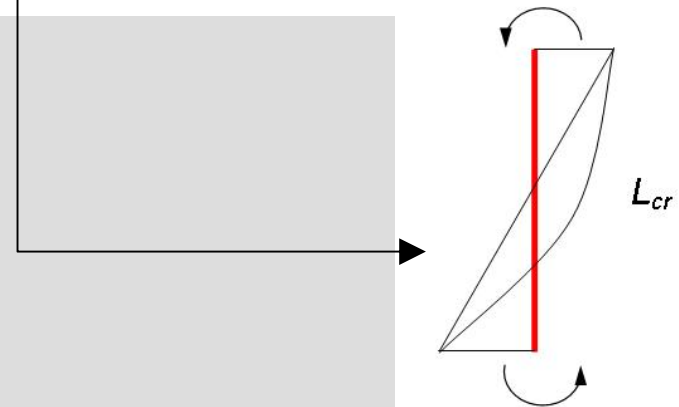
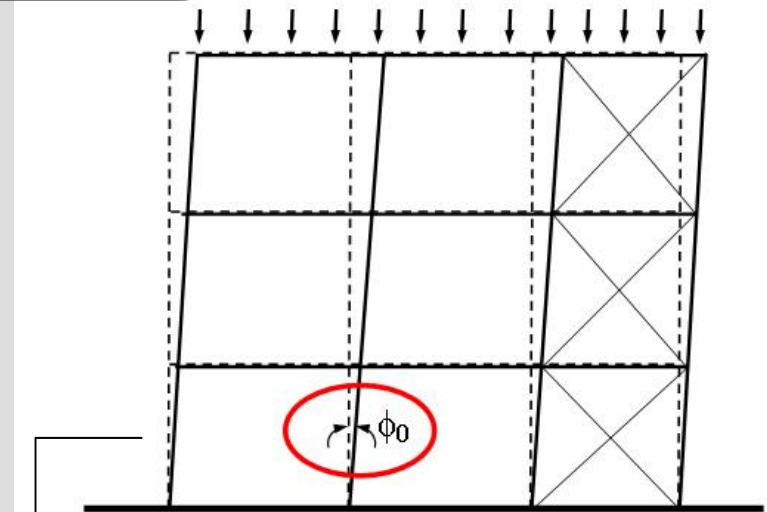
3 alternatives of verification

Global second-order analysis +  
individual stability check of  
members

including global imperfections

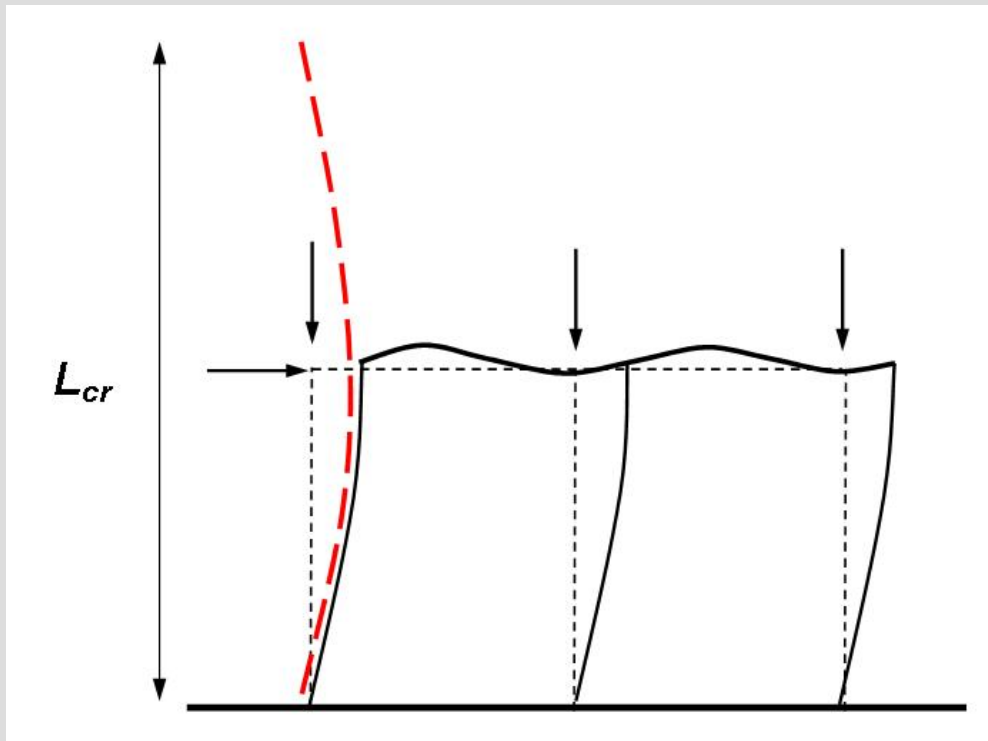
Individual stability check of  
members acc. to EN 1994-1-1  
6.7.3.4 or 6.7.3.5

Buckling length = system length



## Structural stability

3 alternatives of verification

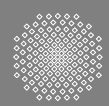


Equivalent column method

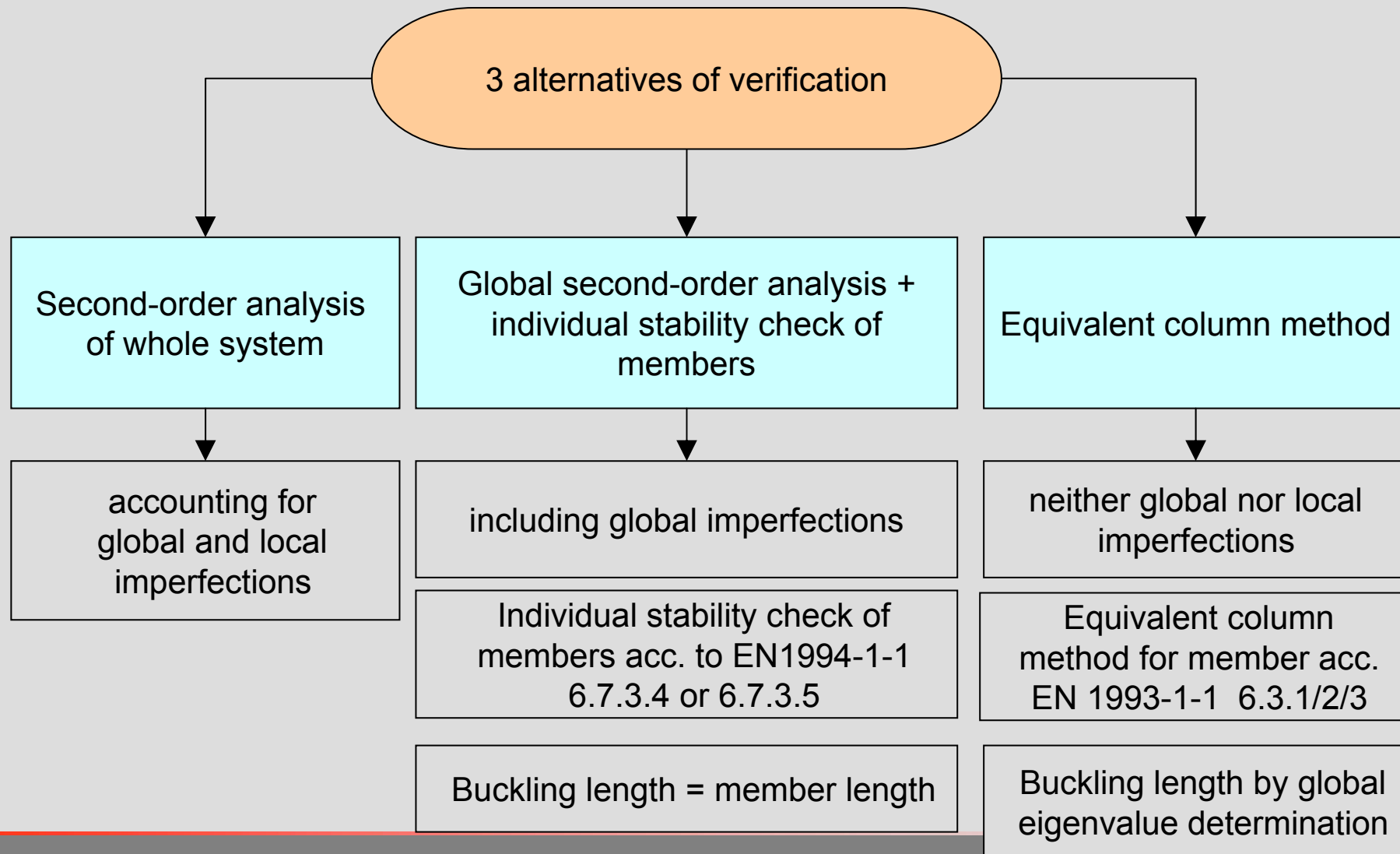
neither global nor local  
imperfections

Equivalent column  
method for member acc.  
EN 1993-1-1 6.3.1/2/3

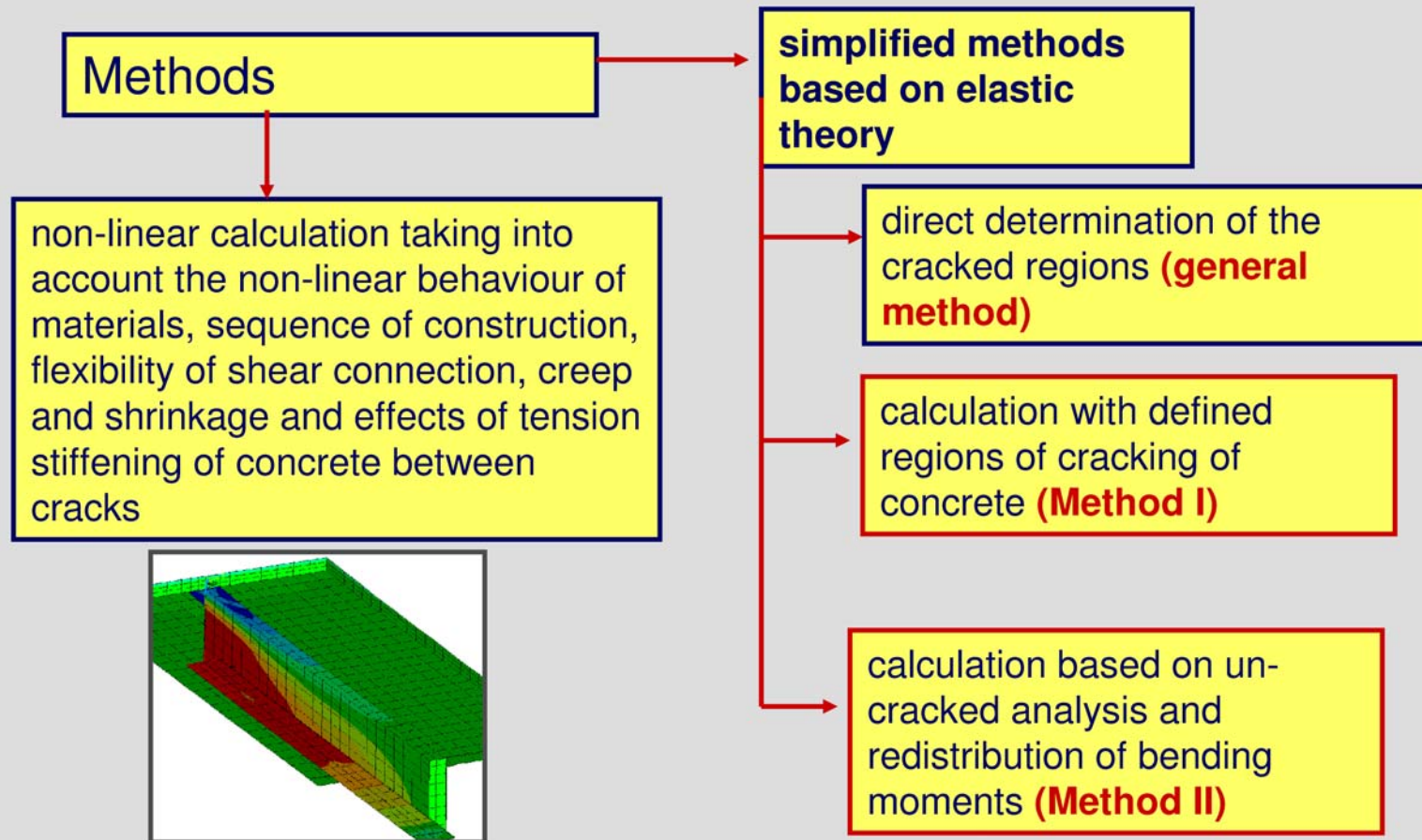
Buckling length by global  
eigenvalue determination



## Structural stability



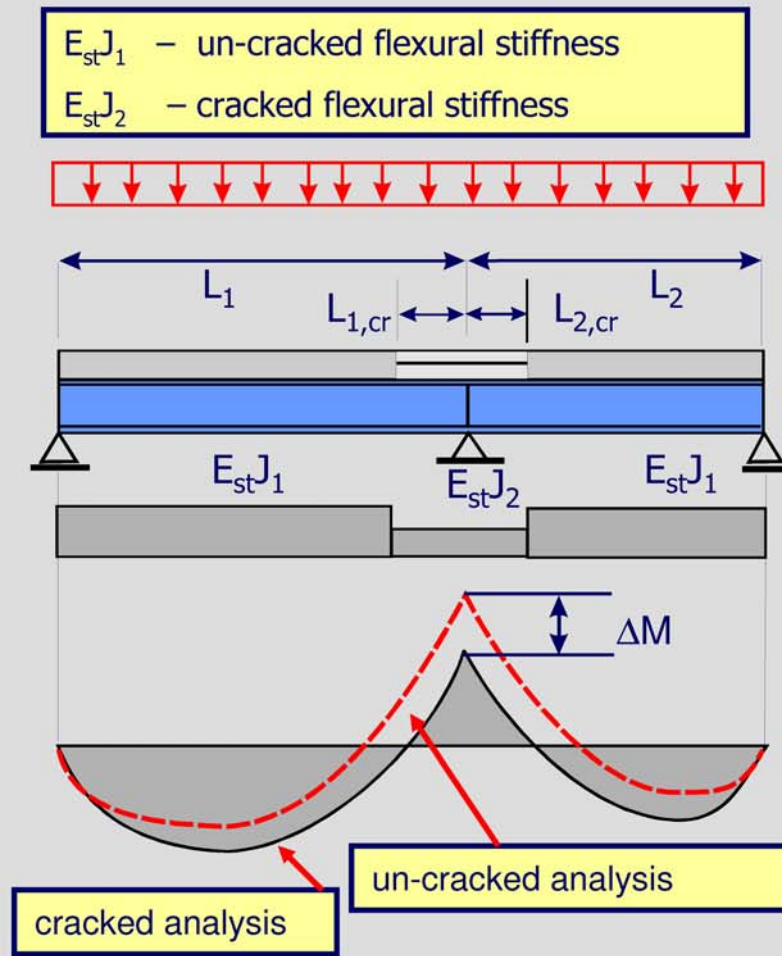
## Calculation of action effects based on elastic theory



[Source: Hanswille]



## Calculation of action effects based on elastic theory - General method



- Determination of internal forces by un-cracked analysis for the characteristic combination.
- Determination of the cracked regions with the extreme fibre concrete tensile stress  $\sigma_{c,max} = 2,0 f_{ct,m}$ .
- Reduction of flexural stiffness to  $EJ_2$  in the cracked regions.
- New structural analysis for the new distribution of flexural stiffness.

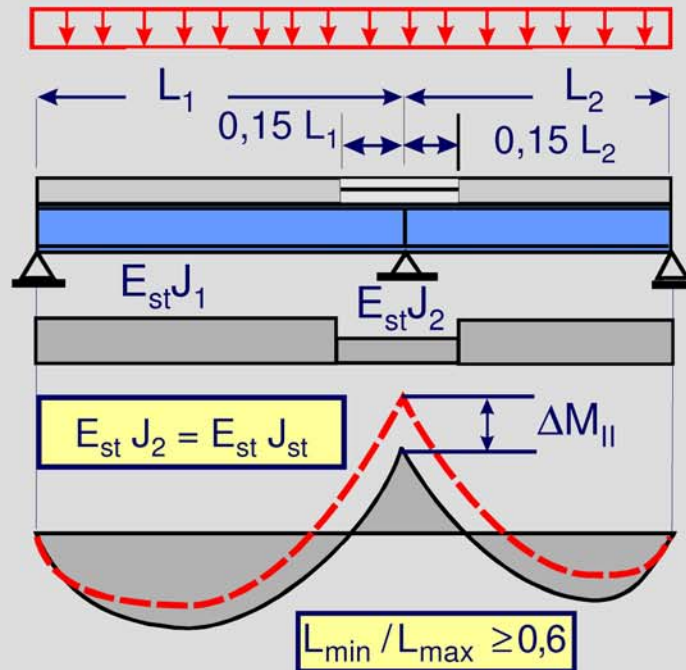
$\Delta M$  Redistribution of bending moments due to cracking

[Source: Hanswille]

## Calculation of action effects based on elastic theory

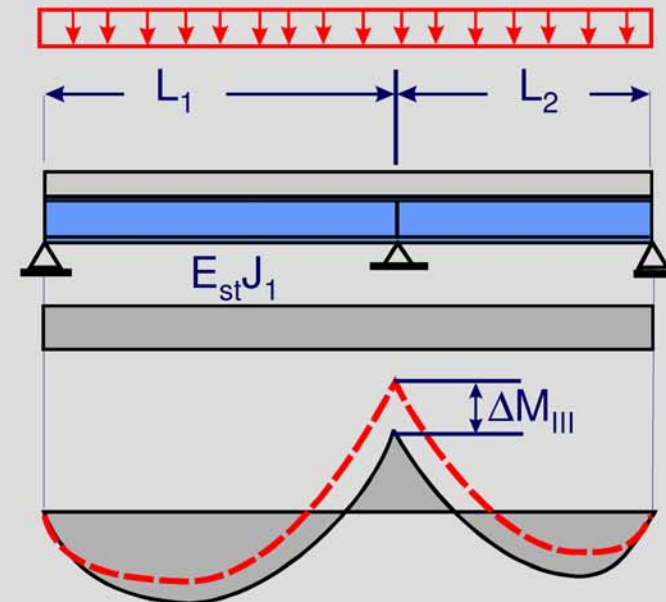
Method I:

Cracked analysis



Method II:

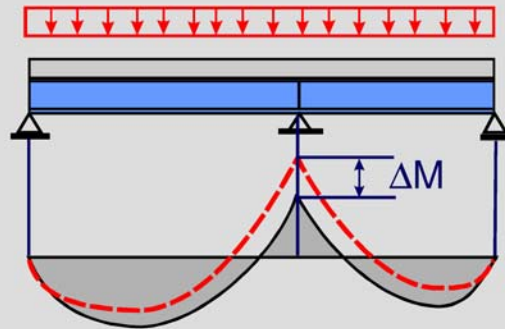
Un-cracked analysis with limited redistribution



Redistribution of bending moments by 10%

[Source: Hanswille]

## Calculation of action effects based on elastic theory



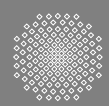
--- bending moments acc. to Method I or II  
— redistribution of bending moments  $\Delta M$

For composite cross-sections in Class 3 or 4, the maximum percentages of redistribution relate to bending moments assumed in design to be applied to the composite member. Moments applied to the steel member should not be redistributed.

		percentage of redistribution $\Delta M$			
Class of the cross-section		1	2	3	4
<b>Method II (un-cracked analysis)</b>	S235 S355	40	30	20	10
	S420 S460	30		10	10
<b>Method I (cracked analysis) or general method</b>	S235 S355	25	15	10	0
	S420 S460	15		0	0

– In beams with all cross-sections in Classes 1 or 2 only, maximum hogging moments may be increased by amounts not exceeding 10%, for un-cracked elastic analysis or 20% for cracked elastic analysis

[Source: Hanswille]



## Relation

## Classification - method of global analysis - resistance

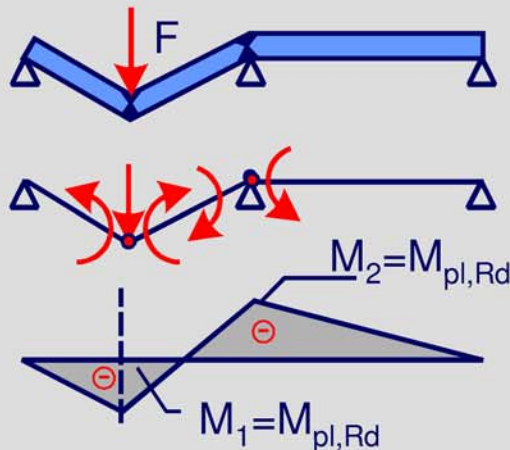
Class of the cross-section	global analysis (action effects $E_d$ )	Consideration of creep, shrinkage, cracking of concrete and sequence of construction	Resistance $R_d$
1	rigid plastic or elastic analysis with redistribution of bending moments	no	plastic
2	elastic analysis with redistribution of bending moments	no	plastic
3	elastic analysis	yes	elastic
4	elastic analysis	yes	elastic acc. to EN 1993-1-5

[Source: Hanswille]

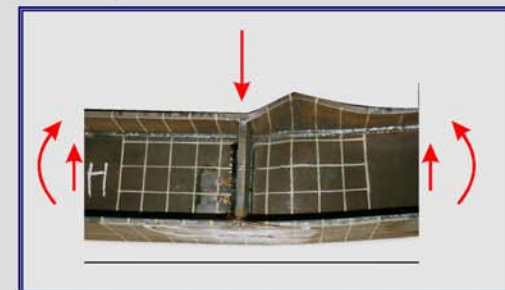
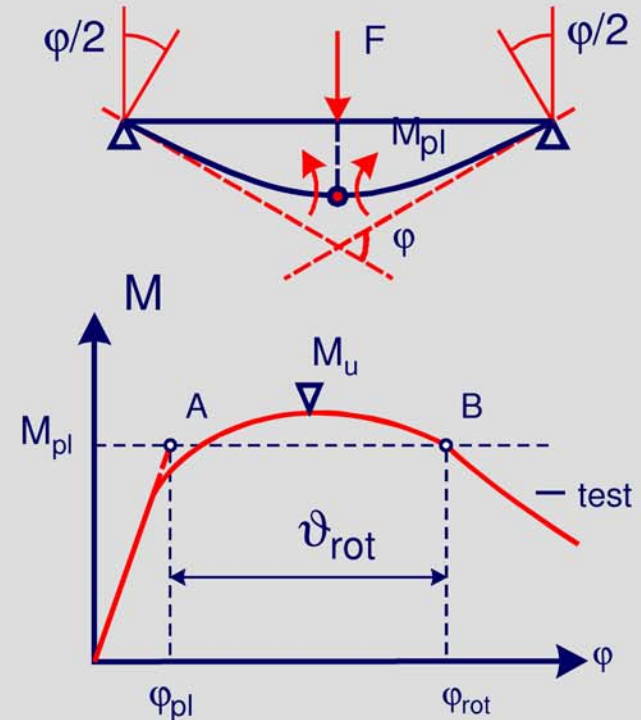


## Rigid plastic analysis

Rigid plastic global analysis may be used for ultimate limit state verifications other than fatigue, where second-order effects do not have to be considered and provided that all the members and joints of the frame are steel or composite, the steel **material** satisfies **ductility requirements** EN 1993-1-1, the **cross-sections** of steel members have **sufficient rotation capacity** and the **joints** are able to sustain their plastic resistance moments for a sufficient rotation capacity.

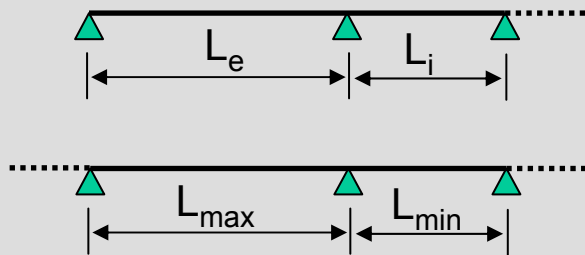


[Source: Hanswille]



## Rigid plastic analysis

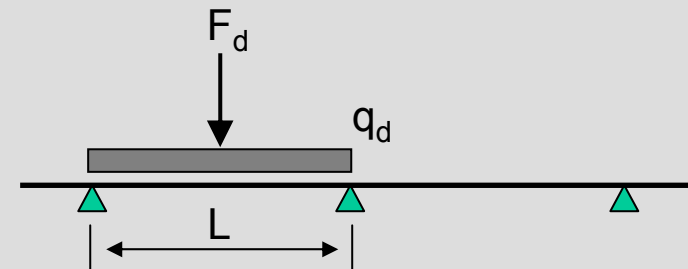
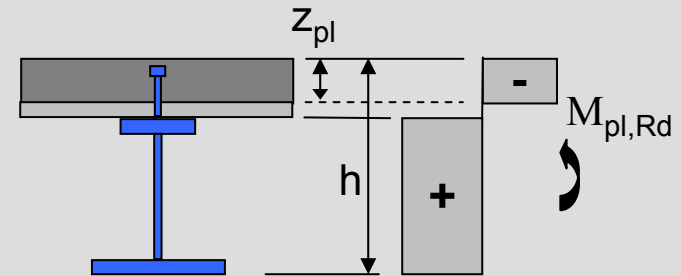
Limitation of span ratio:



exterior span:  $L_e < 1,15 L_i$

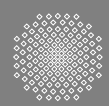
interior span:  $L_{max}/L_{min} \leq 1,50$

Beam with single load and rotation requirements at span:



$$\frac{z_{pl}}{h} \leq 0,15 \quad \text{if} \quad \frac{F_d}{F_d + q_d L} > 0,5$$

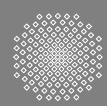




## Rigid plastic analysis

Where rigid-plastic global analysis is used, at each plastic hinge location:

- a) the cross-section of the structural steel section shall be symmetrical about a plane parallel to the plane of the web or webs,
- b) the proportions and restraints of steel components shall be such that lateral-torsional buckling does not occur,
- c) lateral restraint to the compression flange shall be provided at all hinge locations at which plastic rotation may occur under any load case,
- d) the rotation capacity shall be sufficient, when account is taken of any axial compression in the member or joint, to enable the required hinge rotation to develop and
- e) where rotation requirements are not calculated, all members containing plastic hinges shall have effective cross-sections of Class 1 at plastic hinge locations.



## Rigid plastic analysis

For composite beams in buildings, the rotation capacity may be assumed to be sufficient where:

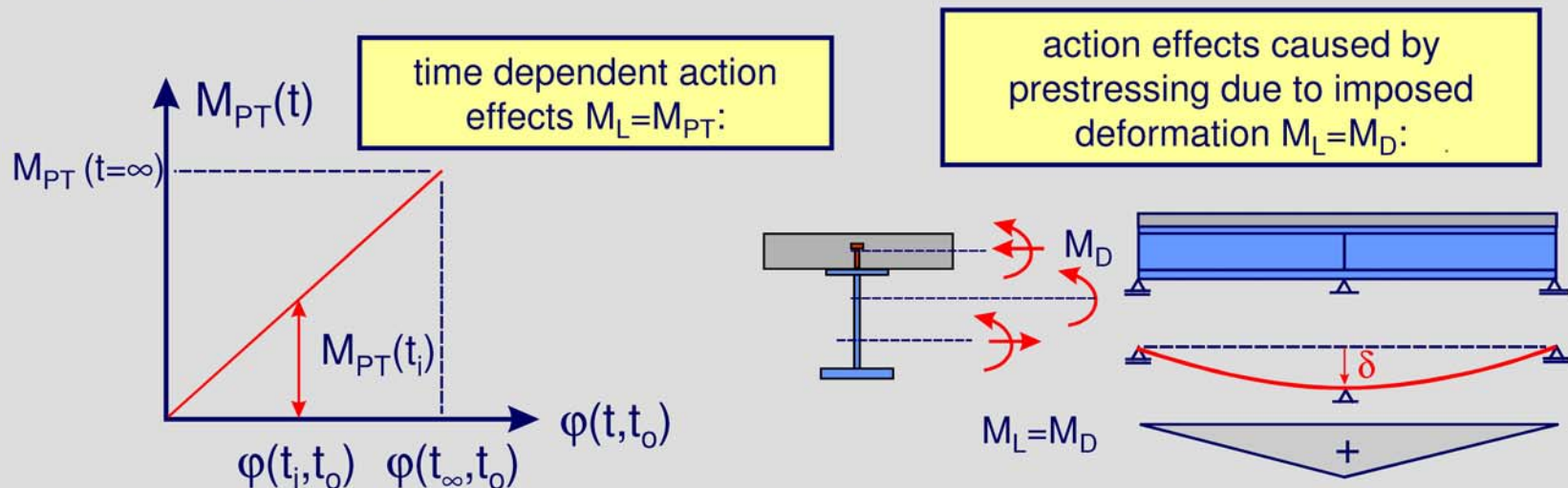
- a) the grade of structural steel does not exceed S355,
- b) the contribution of any reinforced concrete encasement in compression is neglected when calculating the design resistance moment,
- c) all effective cross-sections at plastic hinge locations are in Class1; and all other effective cross-sections are in Class1 or Class2,
- d) each beam-to-column joint has been shown to have sufficient design rotation capacity, or to have a design resistance moment at least 1,2 times the design plastic resistance moment of the connected beam,
- e) adjacent spans do not differ in length by more than 50% of the shorter span,
- f) end spans do not exceed 115% of the length of the adjacent span,
- g) in any span in which more than half of the total design load for that span is concentrated within a length of one-fifth of the span, then at any hinge location where the concrete slab is in compression, not more than 15% of the overall depth of the member should be in compression; this does not apply where it can be shown that the hinge will be the last to form in that span,
- h) the steel compression flange at a plastic hinge location is laterally restrained.

## Stresses based on elastic theory

### Types of loading and action effects:

In the following the different types of loading and action effects are distinguished by a subscript L :

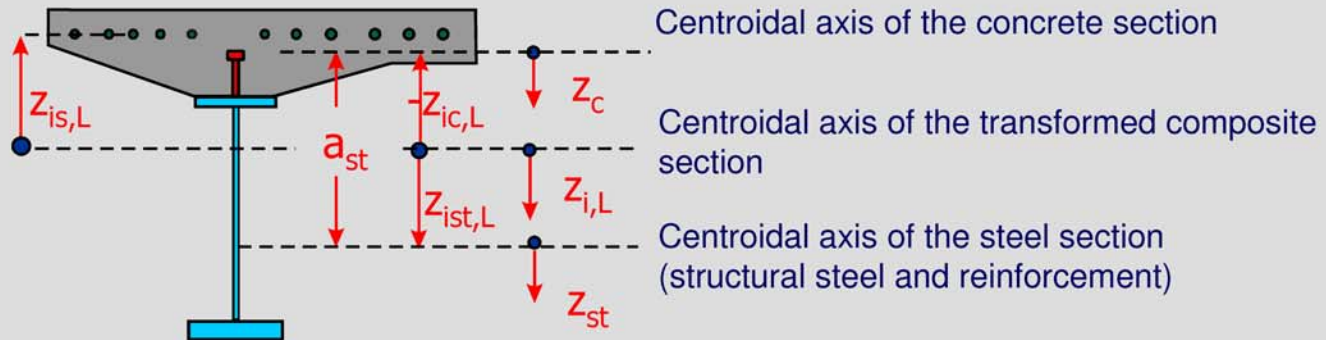
- L=P** for permanent action effects not changing with time
- L=PT** time-dependent action effects developing affine to the creep coefficient
- L=S** action effects caused by shrinkage of concrete
- L=D** action effects due to prestressing by imposed deformations (e.g. jacking of supports)



[Source: Hanswille]

## Stresses based on elastic theory

Modular ratios taking into account effects of creep



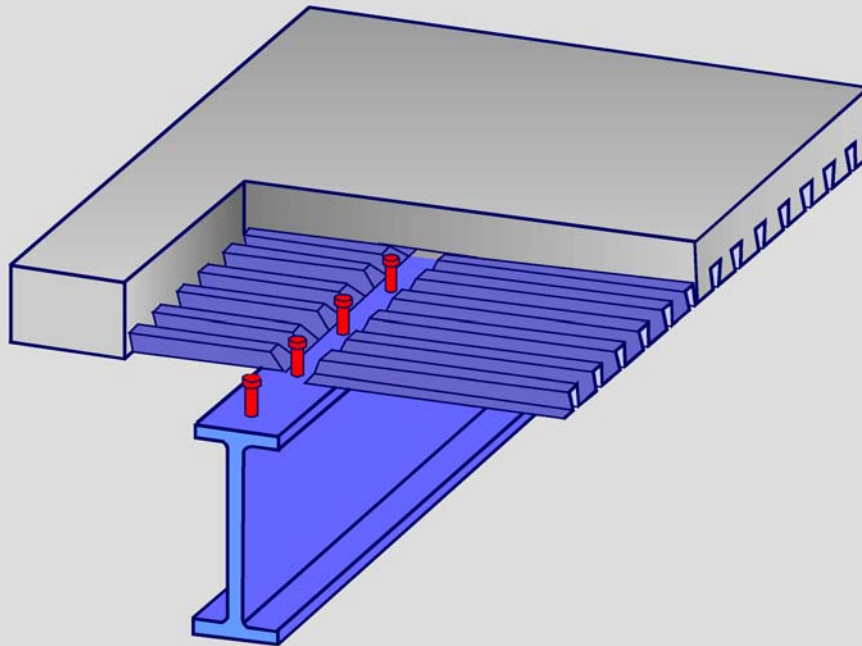
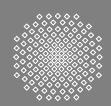
**Modular ratios:**

$$n_L = n_o [1 + \psi_L \varphi(t, t_o)] \quad n_o = \frac{E_a}{E_{cm}}$$

**Creep multipliers  $\psi_L$ :**

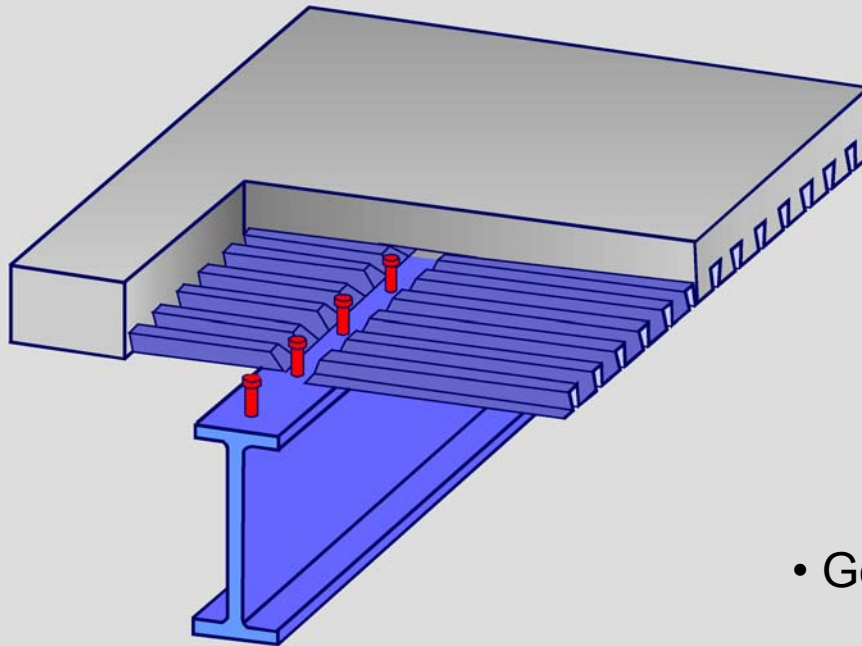
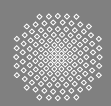
short term loading	$\Psi=0$
permant action constant in time	$\Psi_P=1,10$
shrinkage	$\Psi_S=0,55$
Prestressing by imposed deformations	$\Psi_D=1,50$
time-dependent action effects	$\Psi_{PT}=0,55$

[Source: Hanswille]



**Part 4:**

# **VERIFICATION FOR BENDING AND SHEAR FOR ULTIMATE LIMITE STATE**



- General
- Resistance of class 1 and 2 sections
- Resistance of class 3 and 4 sections
- Lateral torsional buckling

## General - Basis of design

Ultimate limit  
state:

$$E_d \leq R_d$$

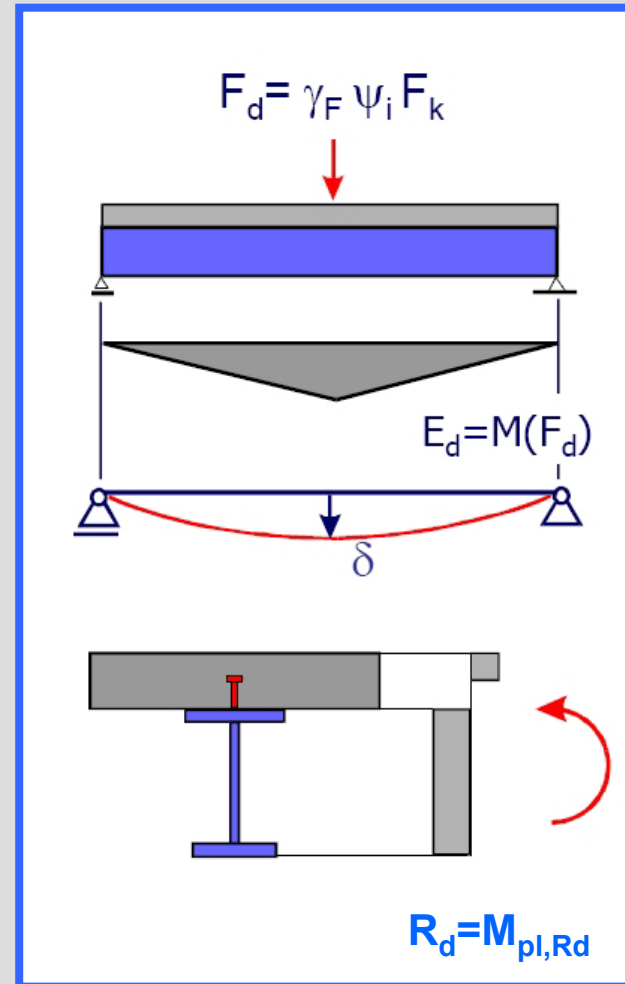
$$R_d = R \left[ \frac{f_{yk}}{\gamma_a}, \frac{\alpha_c f_{ck}}{\gamma_c}, \frac{f_{sk}}{\gamma_s}, \frac{P_{Rk}}{\gamma_v} \right]$$

$$E_d = E (\gamma_F \psi F_k)$$

Serviceability  
limit state:

$$E_d \leq C_d$$

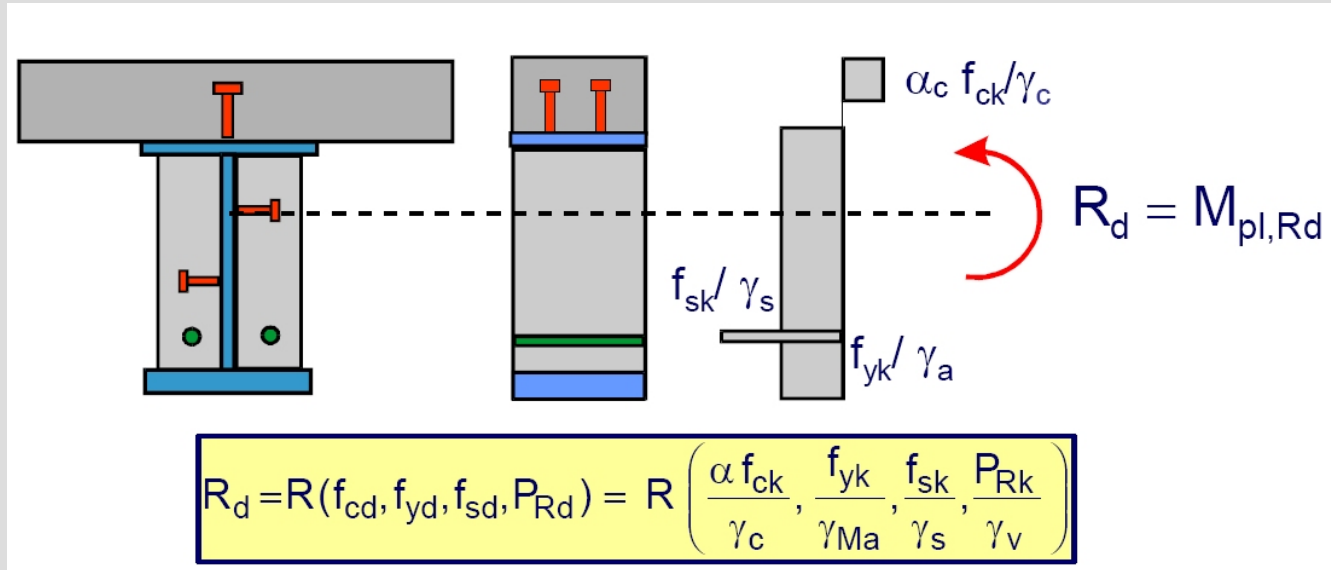
$$E_d = E (\psi F_k)$$



[Source: Hanswille]



## General - Basis of design



Partial safety factor for concrete

$\gamma_C$  according to EN 1992-1-1 e.g.  $\gamma_C = 1.5$

Partial safety factor for reinforcement steel

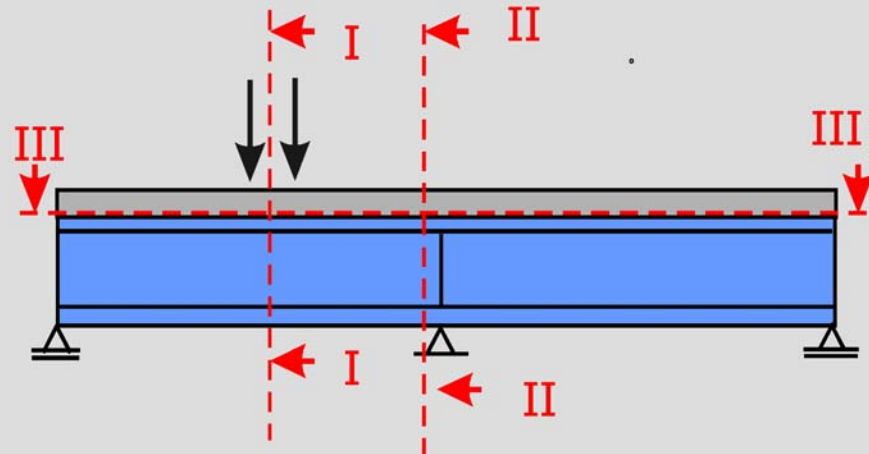
$\gamma_S$  according to EN 1992-1-1 e.g.  $\gamma_S = 1.15$

Partial safety factor for structural steel

$\gamma_{Ma}$  according to EN 1993-1-1 e.g.  $\gamma_{M0} = 1.0$

[Source: Hanswille]

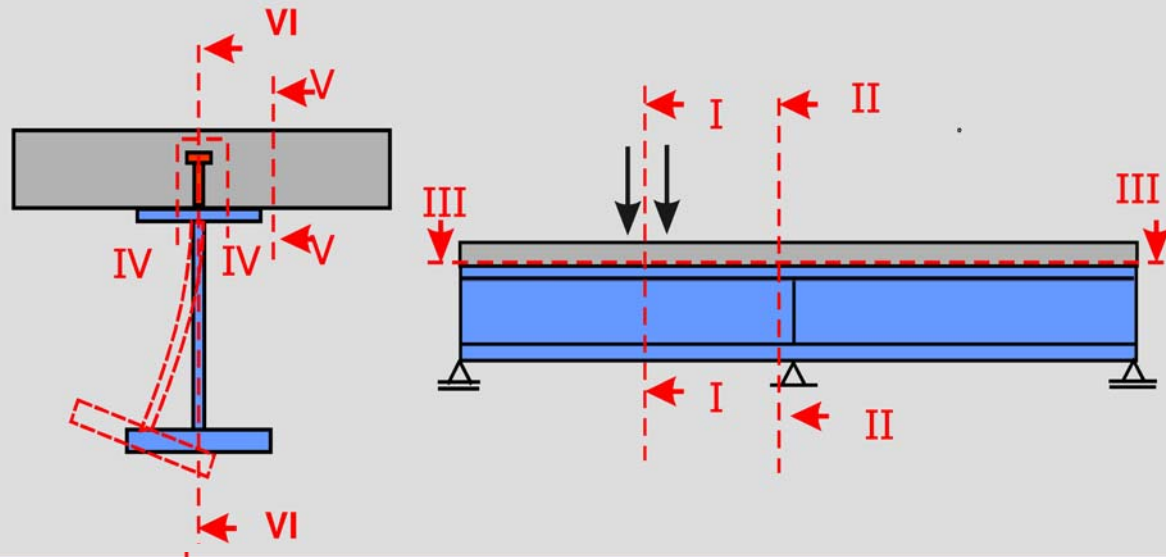
## General - Required verifications for composite beams



- |         |   |
|---------|---|
| I-I     | resistance to bending and shear                     |
| II-II   | resistance to bending and shear and M-V interaction |
| III-III | shear connection – longitudinal shear               |

[Source: Hanswille]

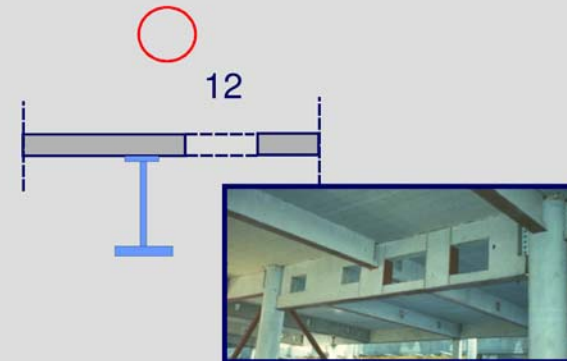
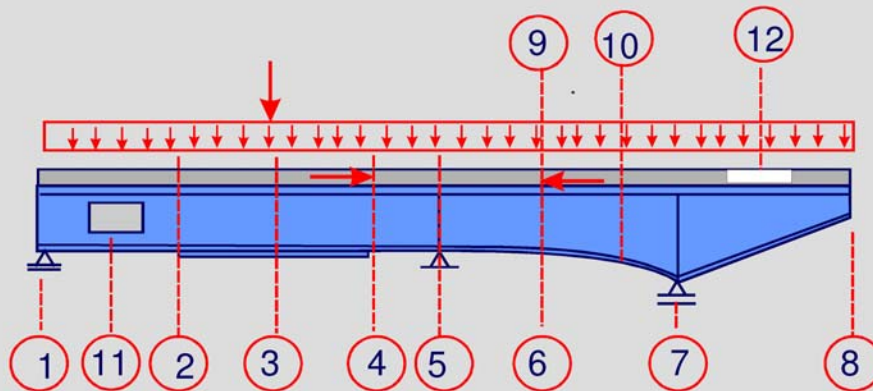
## General - Required verifications for composite beams



- |         |  |
|---------|--|
| I-I     | resistance to bending and shear                                      |
| II-II   | resistance to bending and shear and M-V interaction                  |
| III-III | shear connection – longitudinal shear                                |
| IV-IV   | local introduction of longitudinal shear forces in the concrete slab |
| V-V     | Longitudinal shear of the concrete flange                            |
| VI-VI   | lateral torsional buckling   |

[Source: Hanswille]

## General – Critical cross section



### critical cross-sections

- sections of maximum bending (3,5,7)
- supports (1,5,7)
- sections subjected to concentrated loads (3)
- sudden change of cross-section (2,4)
- introduction of longitudinal forces (4,6)
- cross-sections with web openings (11)
- cross-sections with openings in the concrete flange (12)

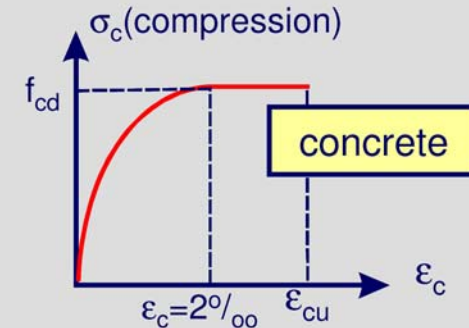
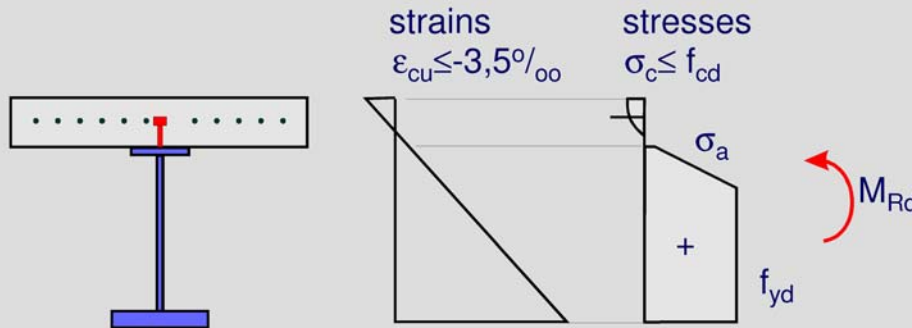
For longitudinal shear verification, a critical length consists of a length between two critical cross-sections. for this case critical cross-sections also include:

- free ends of cantilevers (8)
- in tapering members, sections so chosen that the ratio of the greater to the lesser plastic resistance moment for any pair of adjacent cross-sections does not exceed 1,5 (9,10).

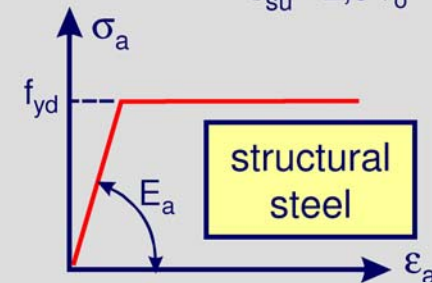
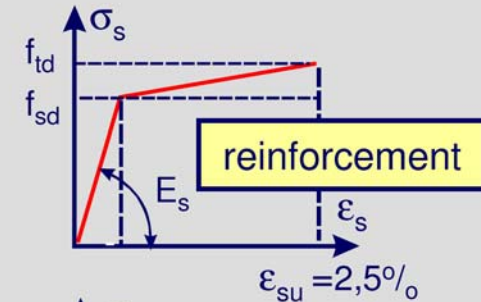
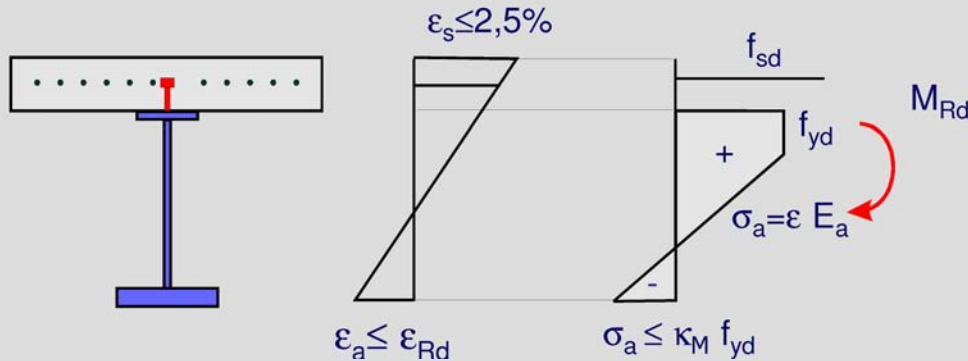
[Source: Hanswille]

## General – Non-linear bending resistance

### limitation of strains in case of sagging bending



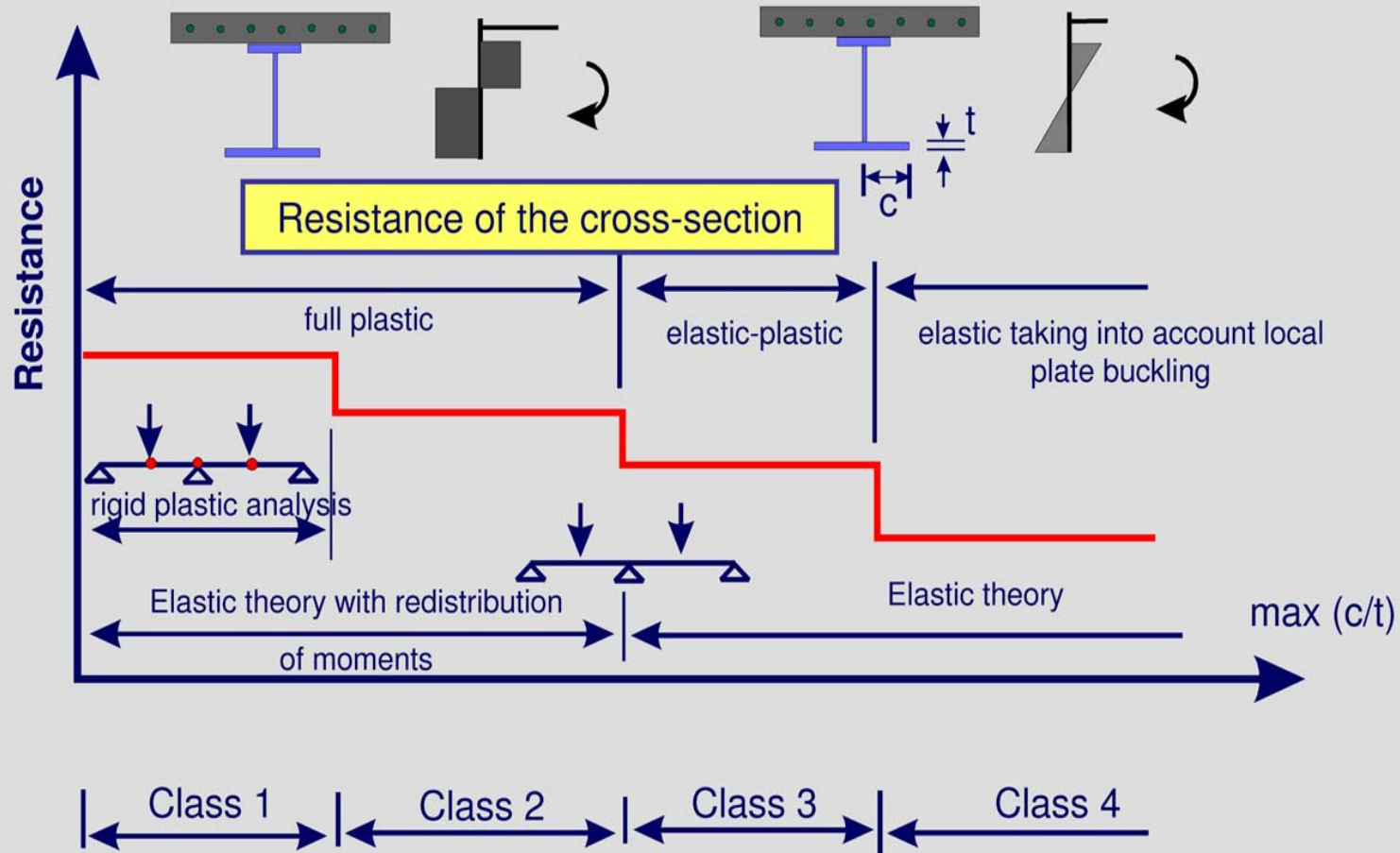
### limitation of strains in case of hogging bending



[Source: Hanswille]



## Classification girders



[Source: Hanswille]

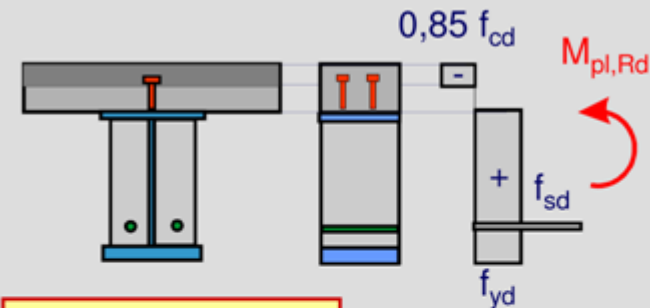


## Resistance of class 1 and 2 sections - classification

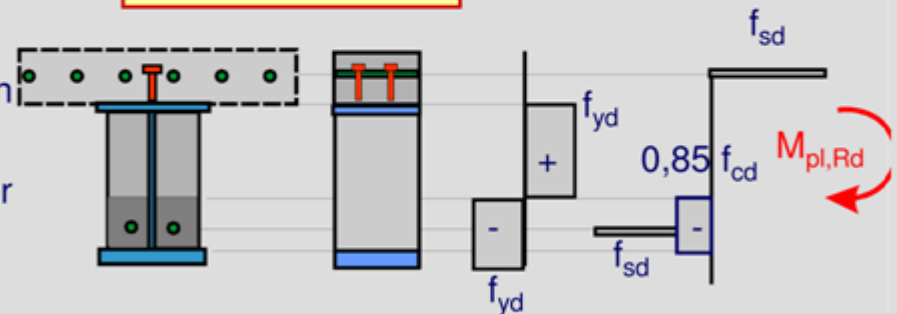
### assumptions for the calculation of the plastic bending resistance

- full interaction between structural steel, reinforcement and concrete,
- the effective area of the structural steel member is stressed to its design yield strength  $f_{yd}$  in tension or compression,
- the effective areas of longitudinal reinforcement in tension and in compression are stressed to their design yield strength  $f_{sd}$  in tension or compression
- the effective area of concrete in compression resists a stress constant over the whole depth between the plastic neutral axis and the most compressed fibre of the concrete, where  $f_{cd}$  is the design cylinder compressive strength of concrete.

### sagging bending



### hogging bending



$$f_{yd} = \frac{f_{yk}}{\gamma_a}$$

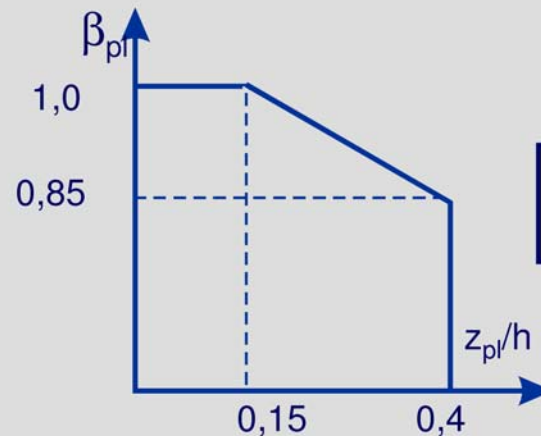
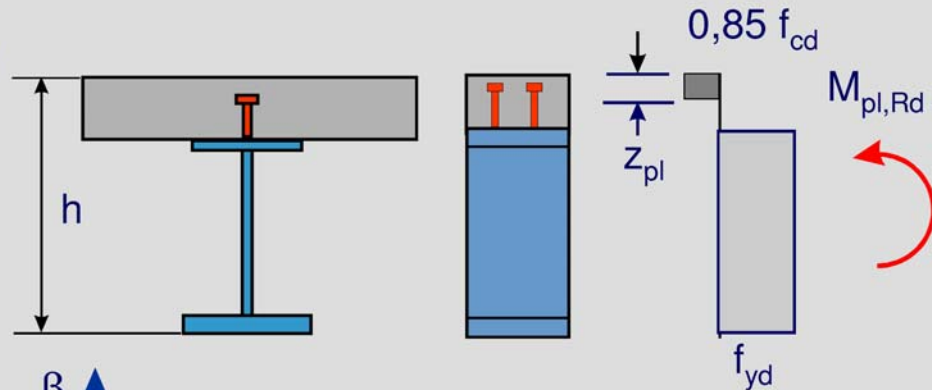
$$f_{cd} = \frac{f_{ck}}{\gamma_c}$$

$$f_{sd} = \frac{f_{sk}}{\gamma_s}$$

[Source: Hanswille]

## Reduction of plastic bending resistance

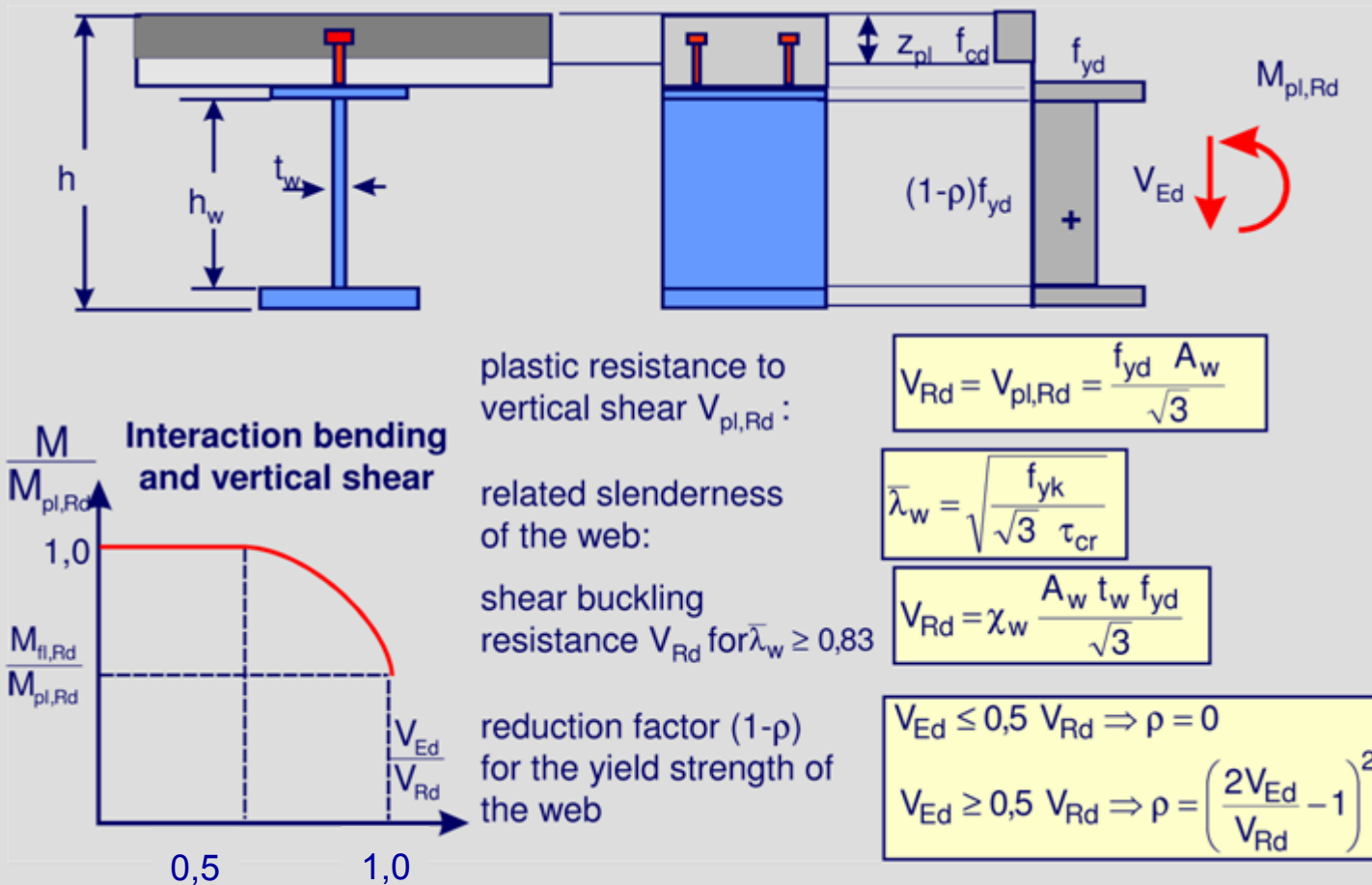
In case of a deep position of the plastic neutral axis in sagging bending the plastic bending resistance is limited by crushing of concrete in the extreme fibre of the concrete slab.



$$M_{Rd} = \beta_{pl} \cdot M_{pl,Rd}$$

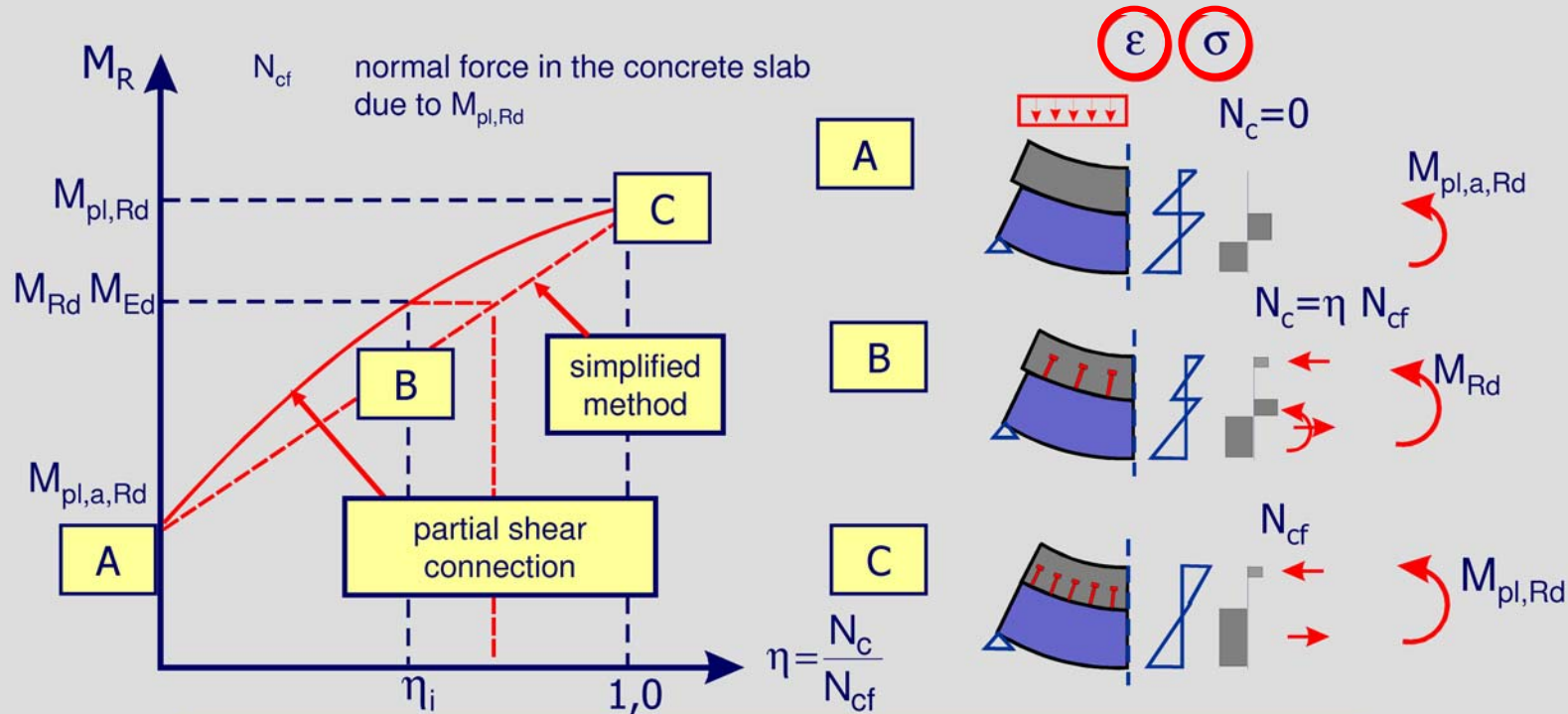
[Source: Hanswille]

## Resistance of class 1 and 2 sections



[Source: Hanswille]

## Resistance of class 1 and 2 sections - Full and partial shear connection



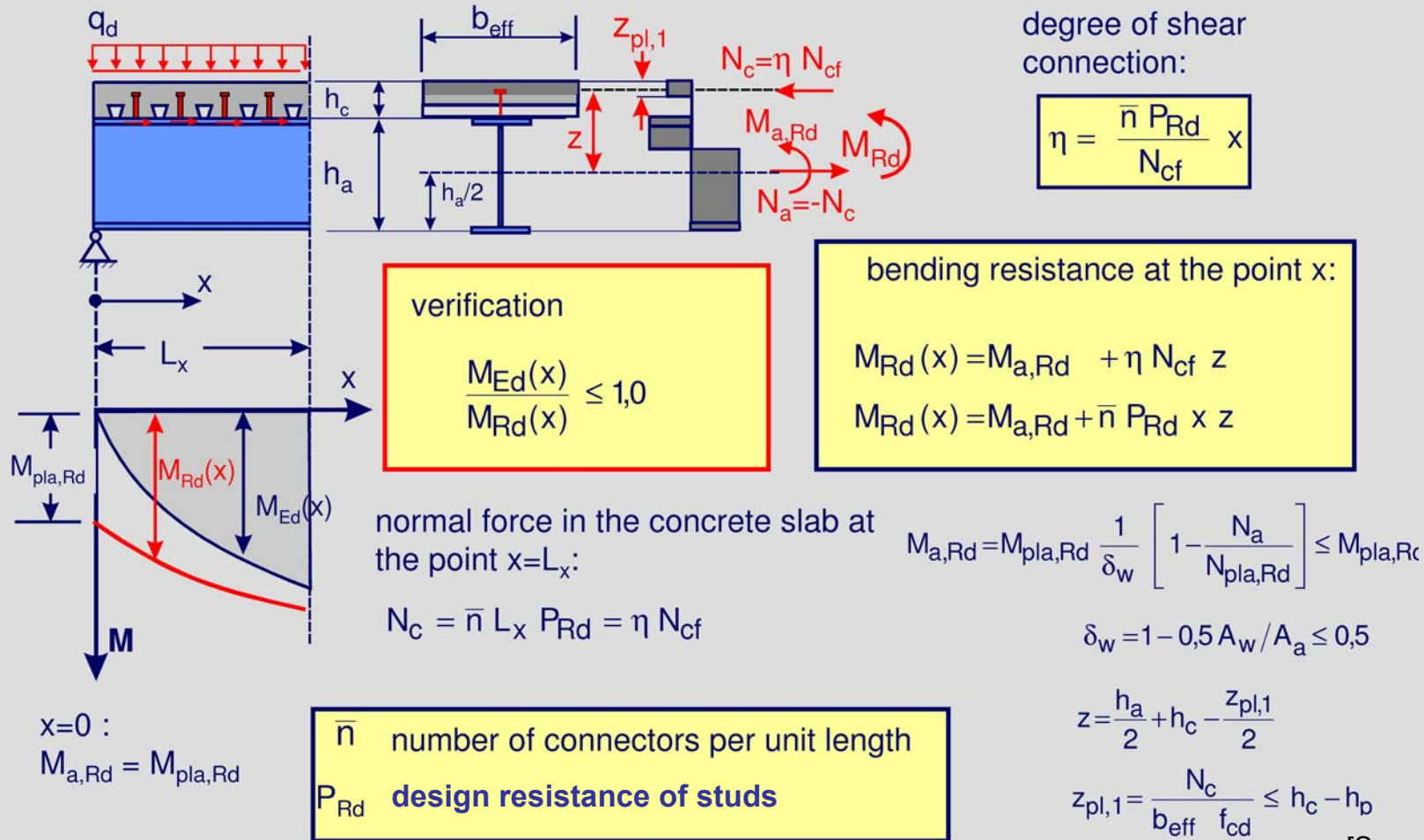
**Simplified method:**  
(Linear interpolation between points A and C)

$$M_{Rd} = M_{pl,a,Rd} + [M_{pl,Rd} - M_{pl,a,Rd}] \frac{N_c}{N_{cf}}$$

$$N_c = \frac{M_{Ed} - M_{pl,Rd}}{M_{pl,Rd} - M_{pl,a,Rd}} N_{cf}$$

[Source: Hanswille]

## Resistance of class 1 and 2 sections - Partial shear connection - general

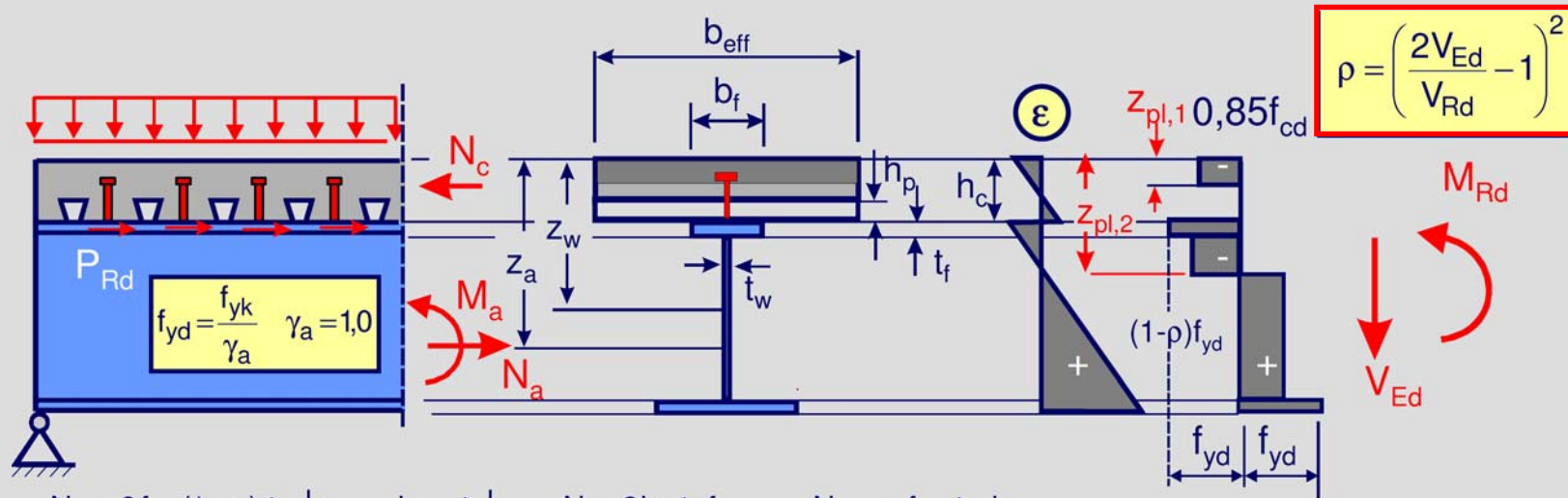


[Source: Hanswille]



## Resistance of class 1 and 2 sections

Partial shear connection – determination of moment resistance



$$N_w = 2f_{yd}(1-\rho)t_w[z_{pl,2} - h_c - t_f] \quad N_f = 2b_f t_f f_{yd} \quad N_{pl,w} = f_{yd} t_w h_w$$

position of the plastic neutral axis in the concrete slab:

$$z_{pl,1} = \frac{\eta N_{cf}}{b_{eff} 0,85 f_{cd}} = \frac{\sum P_{Rd}}{b_{eff} 0,85 f_{cd}} \leq h_c - h_p$$

plastic neutral axis in the web of steel section:

$$z_{pl,2} = h_c + t_f + \frac{N_{pla,Rd} - N_{pl,w} \rho - \eta N_{cf} - N_f}{2 f_{yd} (1-\rho) t_w}$$

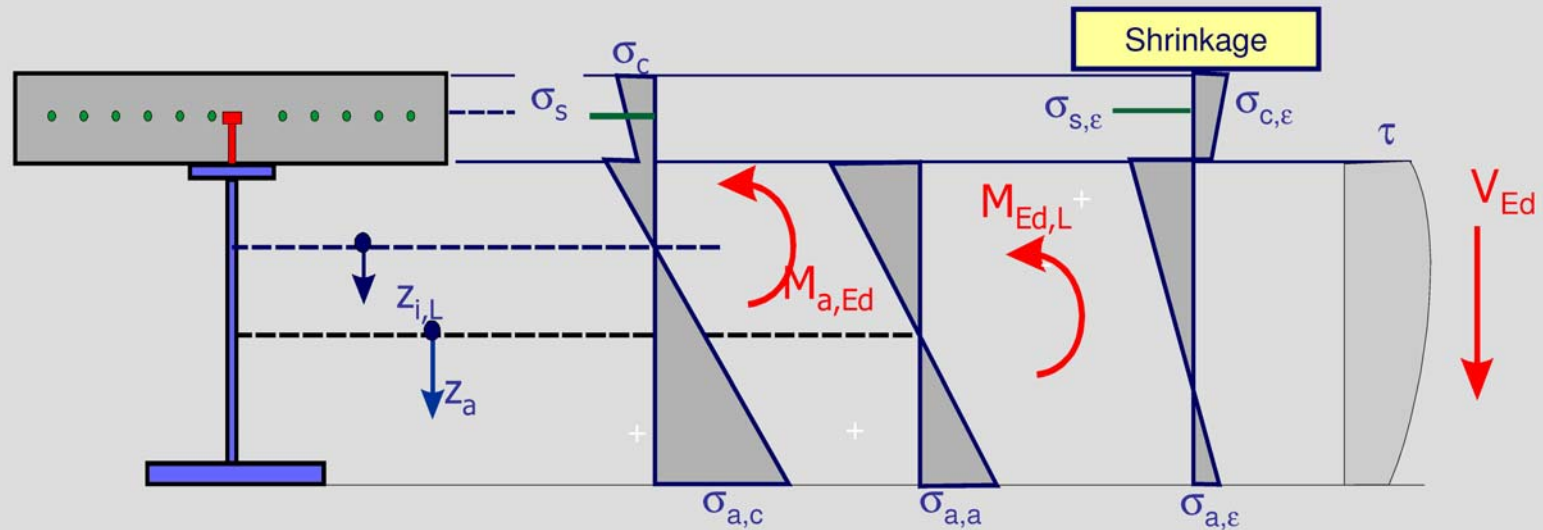
Bending resistance:

$$M_{Rd} = N_{pla,Rd} \left( z_a - \frac{z_{pl,1}}{2} \right) - N_{pl,w} \rho \left( z_w - \frac{z_{pl,1}}{2} \right) - N_f \left( h_c + \frac{t_f - z_{pl,1}}{2} \right) - N_w \left( \frac{z_{pl,2} + h_c + t_f - z_{pl,1}}{2} \right)$$

[Source: Hanswille]



## Resistance of class 3 and 4 sections - class 3



### Stress limits:

concrete:  $\sigma_c \leq f_{cd}$       reinforcement:  $\sigma_s \leq f_{sd}$   
 structural steel:  $\sigma_a \leq f_{yd}$       prestressing steel:  $\sigma_p \leq f_{p,0,1,k}/\gamma_p$

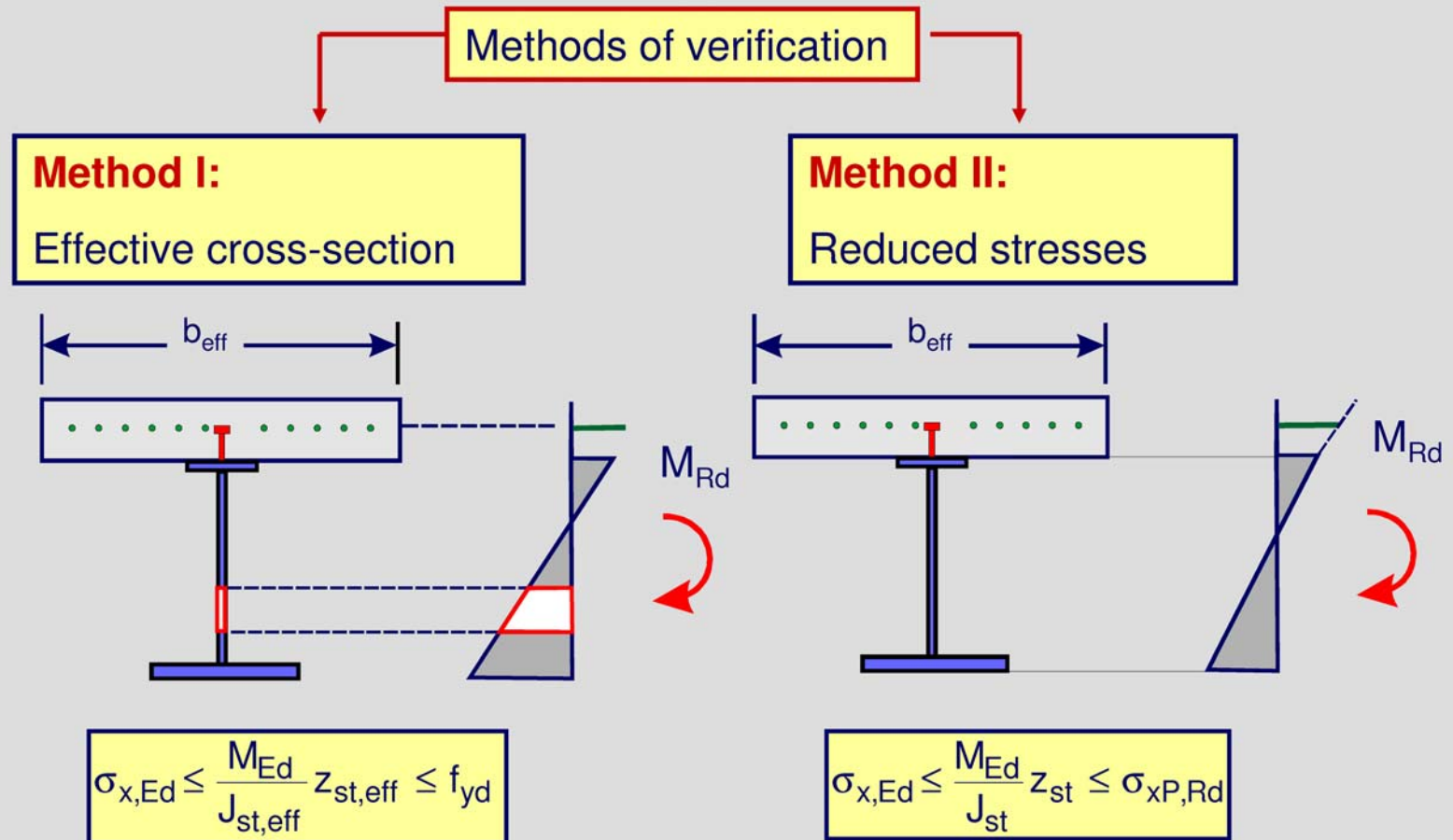
For related shear slenderness:  $\bar{\lambda}_w \leq 0,83$

$$\left( \frac{\sigma_{ax}}{f_{yd}} \right)^2 + \left( \frac{\sqrt{3} \tau}{f_{yd}} \right)^2 \leq 1,0$$

$$\bar{\lambda}_w = \sqrt{\frac{f_{yk} / \sqrt{3}}{\tau_{cr}}}$$

[Source: Hanswille]

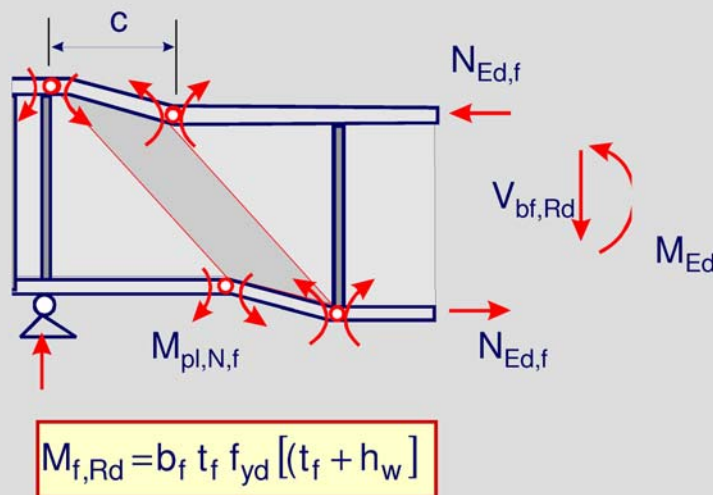
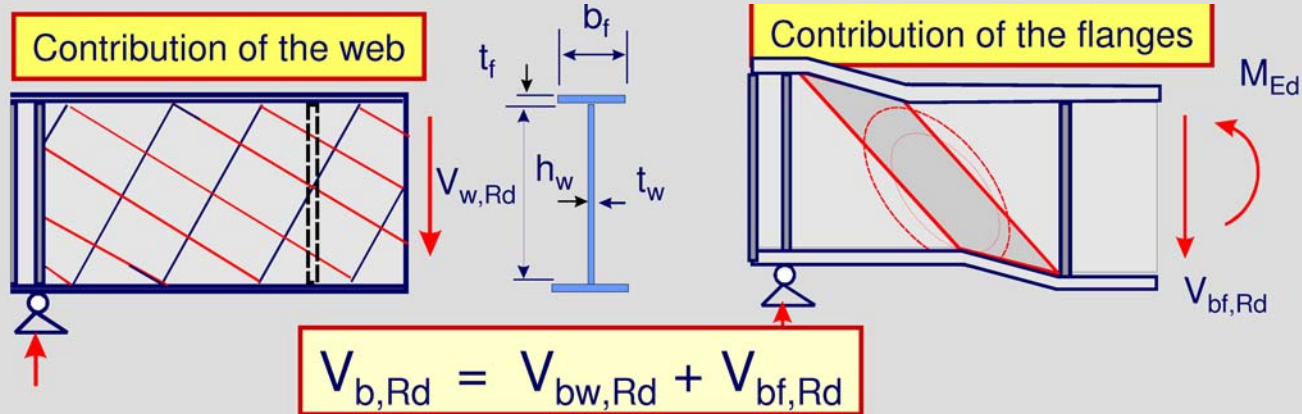
## Resistance of class 3 and 4 sections - class 4



[Source: Hanswille]

## Resistance of class 3 and 4 sections

### Resistance to vertical shear



**Contribution of the flanges**

$$V_{bf,Rd} = \frac{4M_{pl,N,f}}{c} \quad c = a \left[ 0,25 + \frac{1,6 b_f t_f^2 f_{yd}}{t_w h_w^2 f_{yd}} \right]$$

$$M_{pl,N,f} = \frac{b_f t_f^2 f_{yd}}{4} \left[ 1 - \left( \frac{N_{Ed,f}}{N_{pl,d,f}} \right)^2 \right]$$

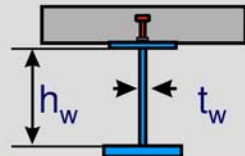
$$V_{bf,Rd} = \frac{b_f t_f^2 f_{yd}}{c} \left[ 1 - \left( \frac{M_{Ed}}{M_{f,Rd}} \right)^2 \right]$$

[Source: Hanswille]

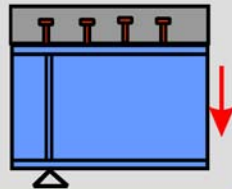
## Resistance of class 3 and 4 sections

### Resistance to vertical shear

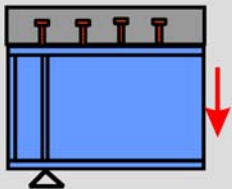
$$V_{b,Rd} = V_{bw,Rd} + V_{bf,Rd} \leq \frac{\eta f_{yw} h_w t}{\sqrt{3} \gamma_{Rd}}$$



non-rigid end post

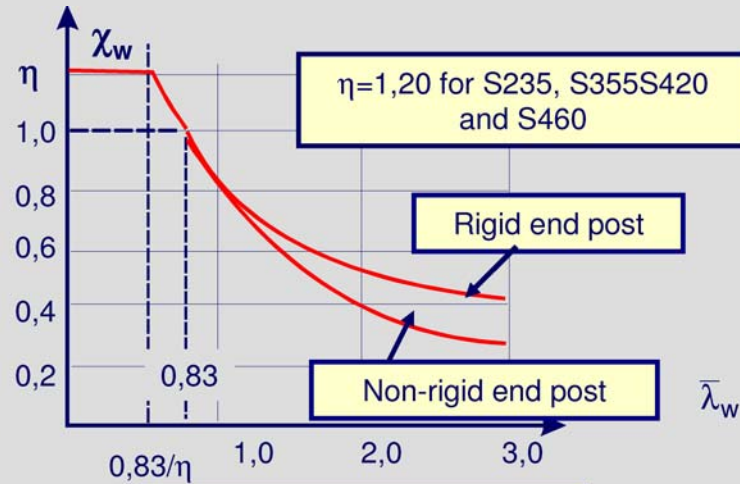


rigid end post



$$\bar{\lambda}_w = \sqrt{\frac{f_{yw} / \sqrt{3}}{\tau_{cr}}}$$

$\tau_{cr}$  – elastic critical shear buckling stress

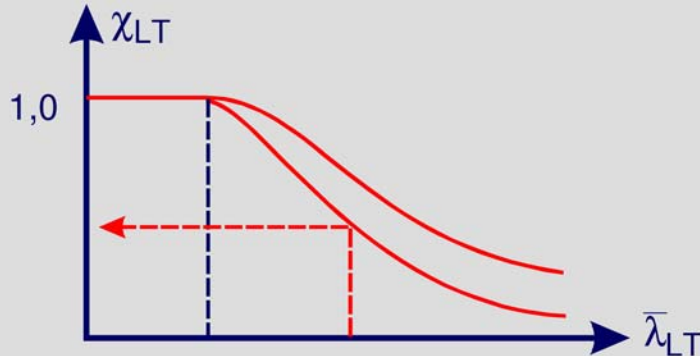
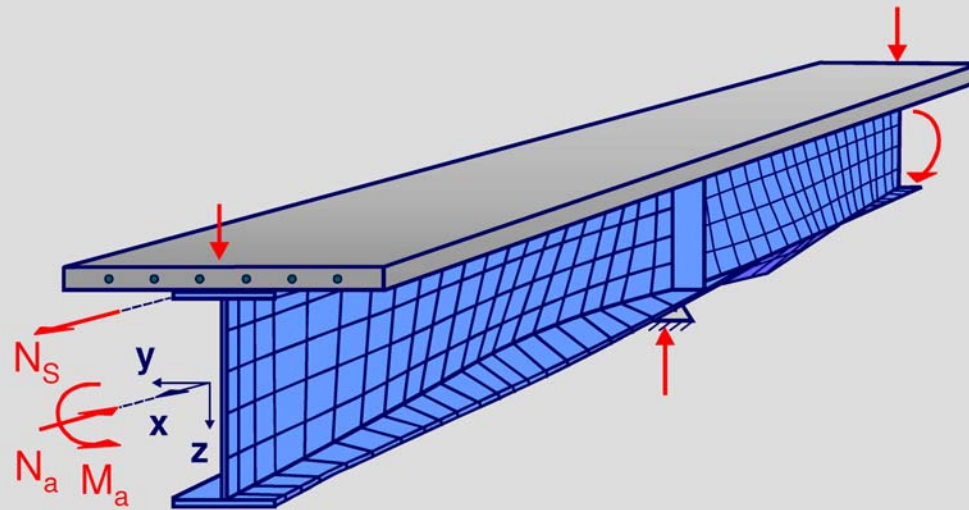


$$V_{bw,Rd} = \chi_w \cdot h_w t_w \frac{f_{yw}}{\sqrt{3} \gamma_{Rd}}$$

Reduction factor $\chi_w$		
	rigid end post	Non-rigid end post
$\bar{\lambda}_w < 0,83 / \eta$	$\eta$	$\eta$
$0,83 / \eta \leq \bar{\lambda}_w < 1,08$	$0,83 / \bar{\lambda}_w$	$0,83 / \bar{\lambda}_w$
$\bar{\lambda}_w \geq 1,08$	$1,37 / (0,7 + \bar{\lambda}_w)$	$0,83 / \bar{\lambda}_w$

[Source: Hanswille]

## Lateral torsional buckling



**Cross-sections in class 1 and 2:**

$$M_{Rd} = M_{pl,Rd}$$

$$\bar{\lambda}_{LT} = \sqrt{\frac{M_{pl,Rk}}{M_{cr}}}$$

$$M_{Ed} \leq \chi_{LT} M_{Rd}$$

**Cross-sections in class 3 and 4:**

$$M_{Rd} = M_{el,Rd}$$

$$\bar{\lambda}_{LT} = \sqrt{\frac{M_{el,Rk}}{M_{cr}}} = \sqrt{\frac{f_{yk}}{\sigma_{cr}}}$$

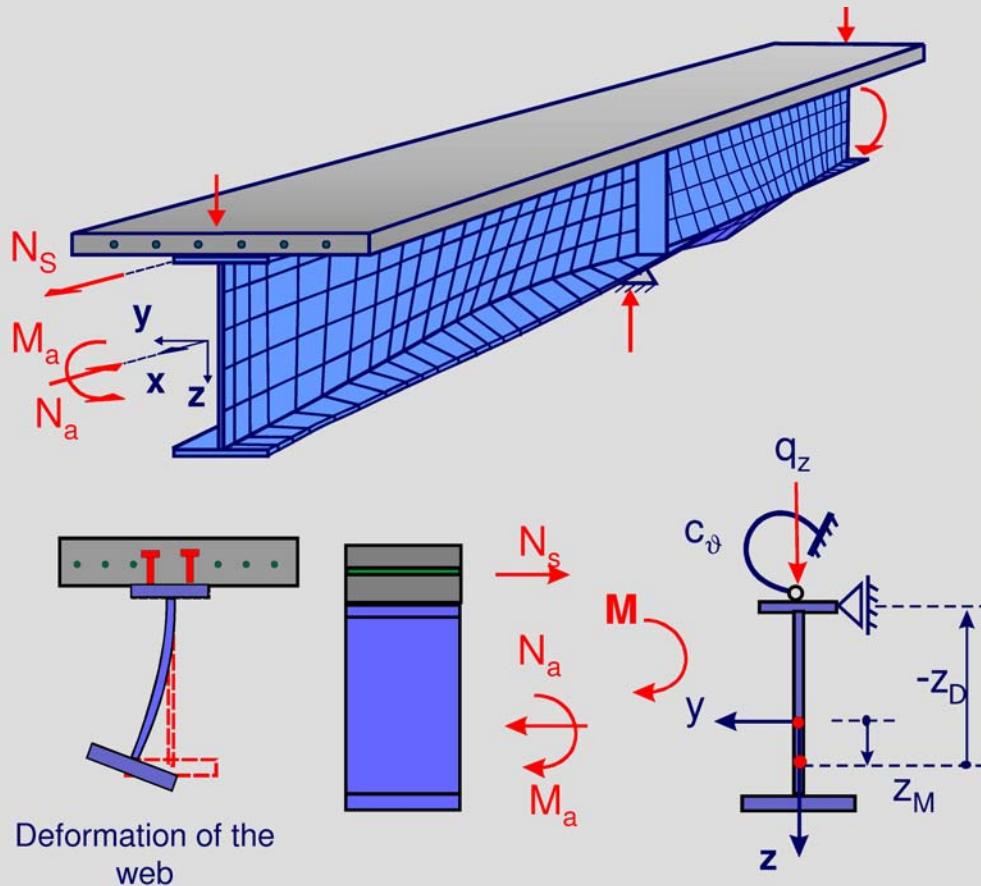
$$M_{Ed} \leq \chi_{LT} M_{el,Rd}$$

$$\text{or } \sigma_{Ed} \leq \chi_{LT} f_{yd}$$

[Source: Hanswille]



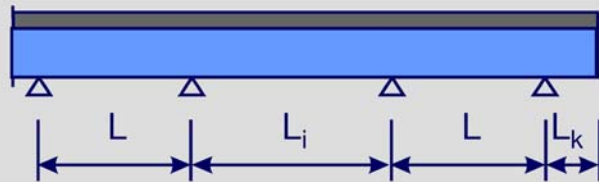
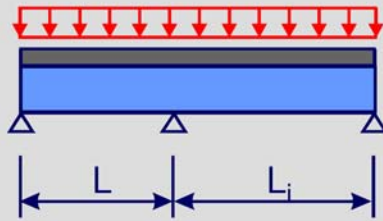
## Lateral torsional buckling – elastic critical bending moment



The determination of the elastic critical bending moment is based on the inverted U-frame model. The model takes into account the lateral displacement of the bottom flange causing bending of the steel web and the rotation of the top flange that is resisted by bending of the concrete slab.

[Source: Hanswille]

## Lateral torsional buckling – without direct calculation



limitation of span ratios:

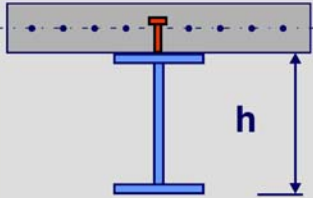
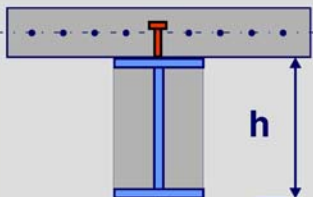
$$0,8 \leq l / l_i \leq 1,25$$

$$L_k / L \leq 0,15$$

limitation regarding variable actions:

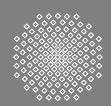
$$\frac{\gamma_G G_k}{\gamma_G G_k + \gamma_Q Q_k} \geq 0,4$$

A direct verification for lateral torsional buckling is not required where special limitations regarding the ratios of span length's and regarding the percentage of the variable actions are fulfilled. The background of simplified method is based on the fact, that the related slenderness of these beams is smaller than 0,4.

maximum depth of the cross-section				
	section	S 235	S 355	S460
	IPE	600	400	270
	HE- Profiles	800	650	500
	IPE	600	600	400
	HE- Profiles	1000	800	650

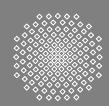
[Source: Hanswille]





**Part 5:**

**SHEAR CONNECTION**



- **Longitudinal shear forces**

- Determination of longitudinal shear forces
- Full and partial shear connection
- Requirements for shear connectors

- **Headed studs**

- Head studs as shear connector
- Horizontally lying studs
- Headed studs used with profiled steel sheeting

- **Longitudinal shear forces in concrete slab**





- **Longitudinal shear forces**

- Determination of longitudinal shear forces
- Full and partial shear connection
- Requirements for shear connectors

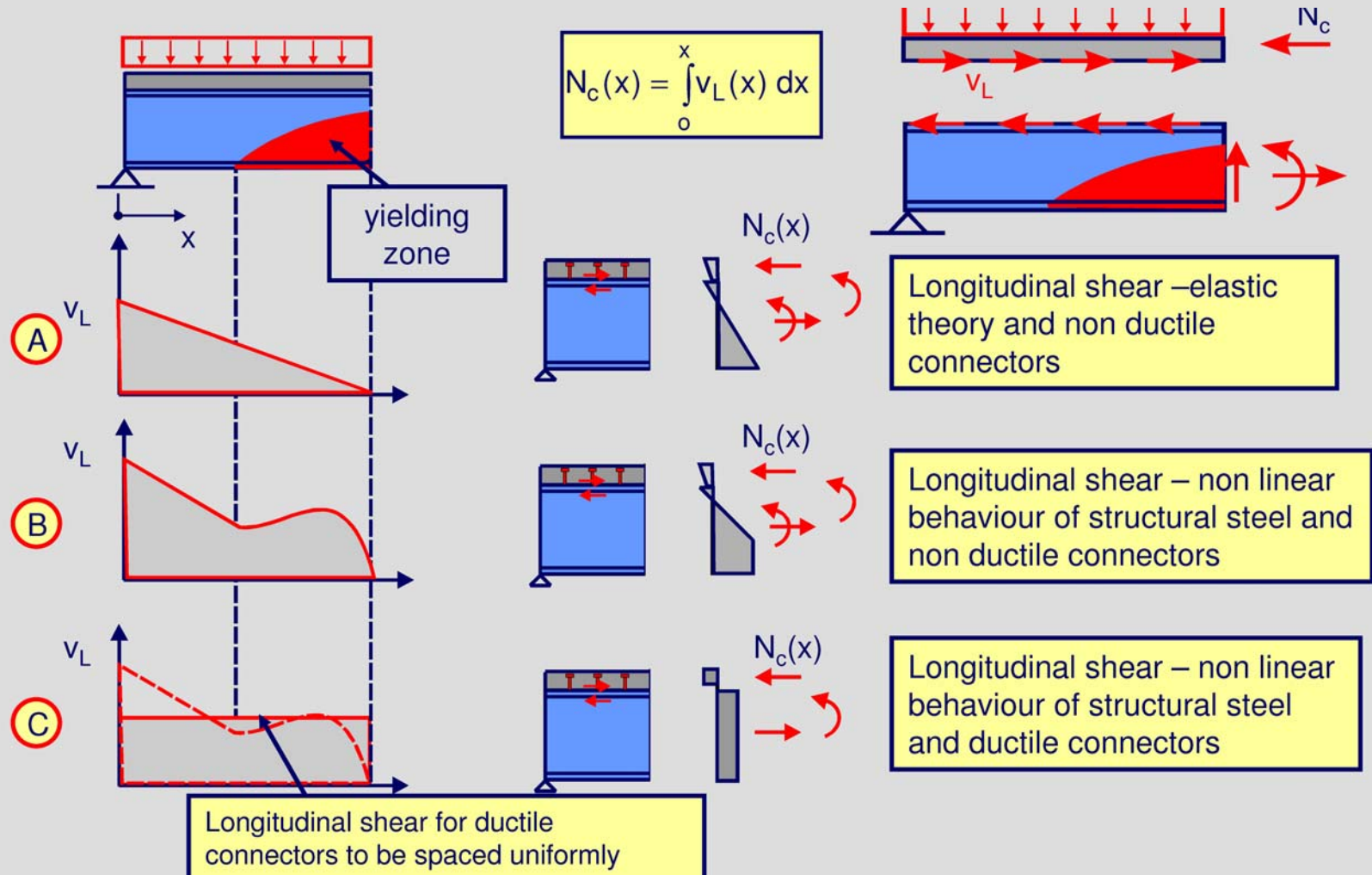
- **Headed studs**

- Head studs as shear connector
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- **Longitudinal shear forces in concrete slab**



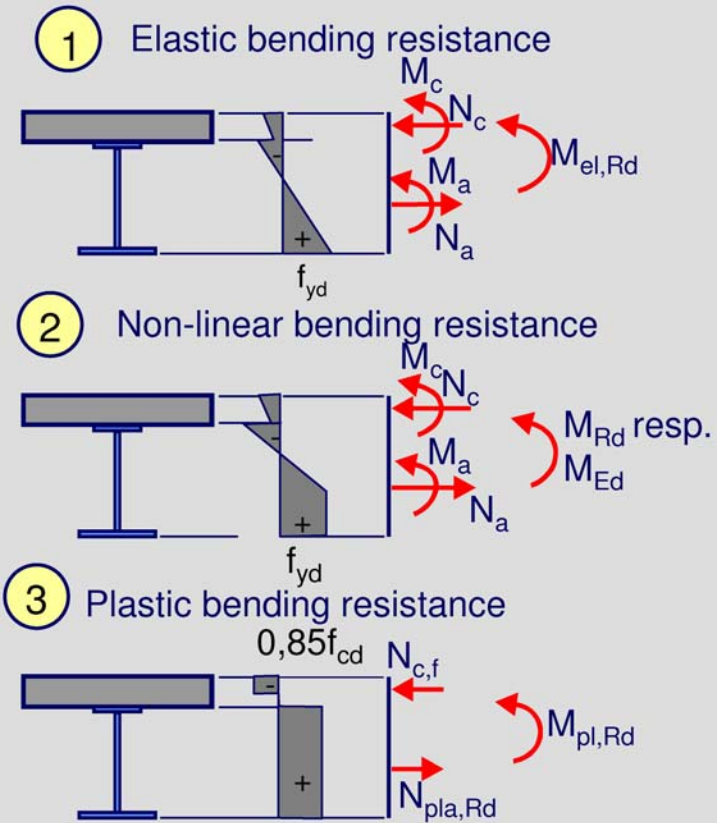
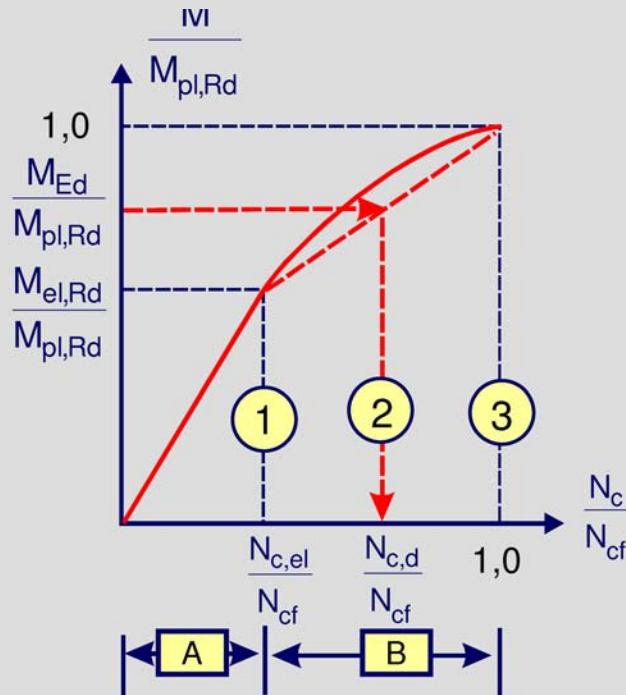
## Longitudinal shear forces



[Source: Hanswille]



# Determination of longitudinal shear forces - by simplified method for $N_c$



Region A:  
elastic behaviour

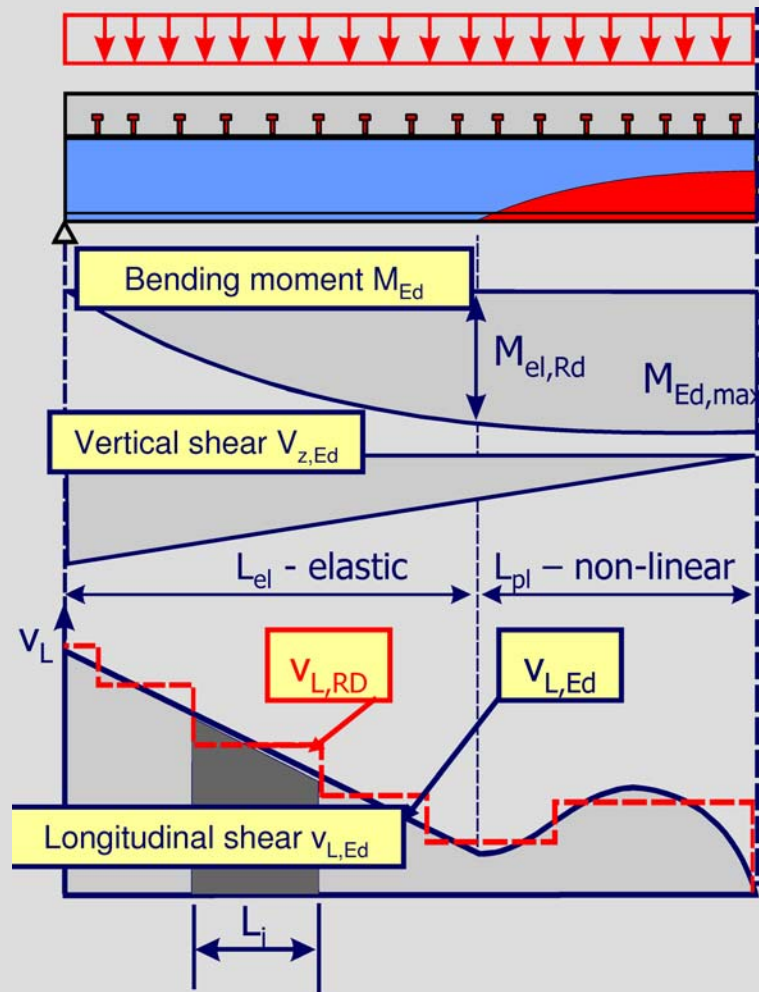
$$N_c = \sum_L M_L \frac{A_{c,L} Z_{ic,L}}{J_{i,L}}$$

Region B:  
inelastic behaviour

$$N_{c,d} = N_{c,el} + \frac{M_{Ed} - M_{el,Rd}}{M_{pl,Rd} - M_{el,Rd}} [N_{c,f} - N_{c,el}]$$

[Source: Hanswille]

## Determination of longitudinal shear forces - general



Elastic region:

$$\frac{V_{L,Ed}}{V_{L,Rd}} \leq 1,0 \quad \frac{V_{L,Ed}}{V_{L,Rd}} \leq 1,1 \quad V_{L,Ed} = \int_{L_i} v_{L,Ed} dx$$

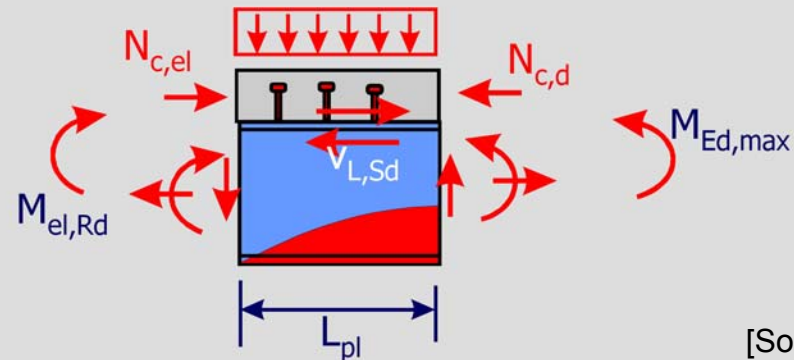
$$v_{L,Ed} = \sum_L v_{z,Ed,L} \frac{(A_{c,L} \cdot z_{ic,L}) + (A_s \cdot z_{is,L})}{J_{i,L}}$$

$v_{L,Ed}$  – longitudinal shear per unit length

$V_{L,Ed}$  – total longitudinal shear within the length  $L_i$

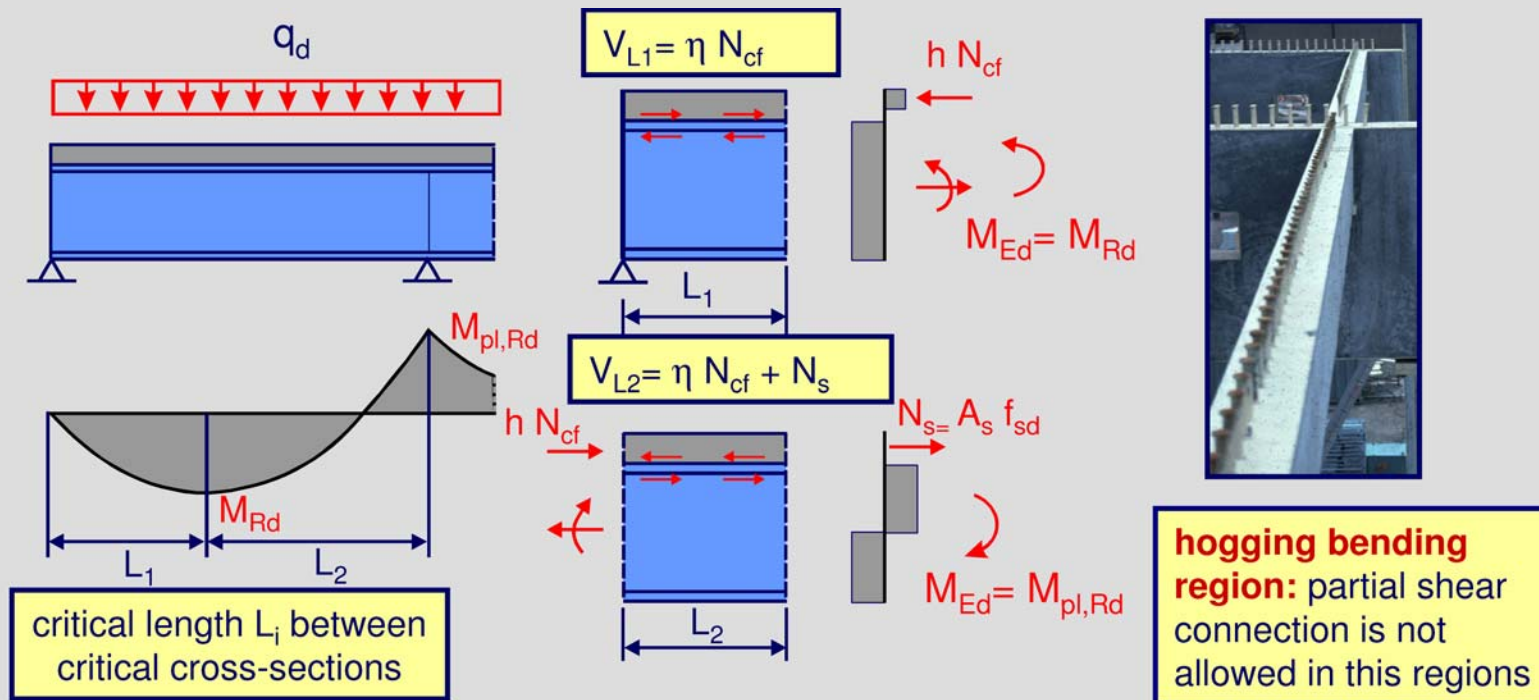
Non-linear region:

$$v_{L,Ed} = \frac{N_{cd} - N_{c,el}}{L_{pl}} \leq v_{L,Rd}$$



[Source: Hanswille]

## Partial shear connection – determination of longitudinal shear forces

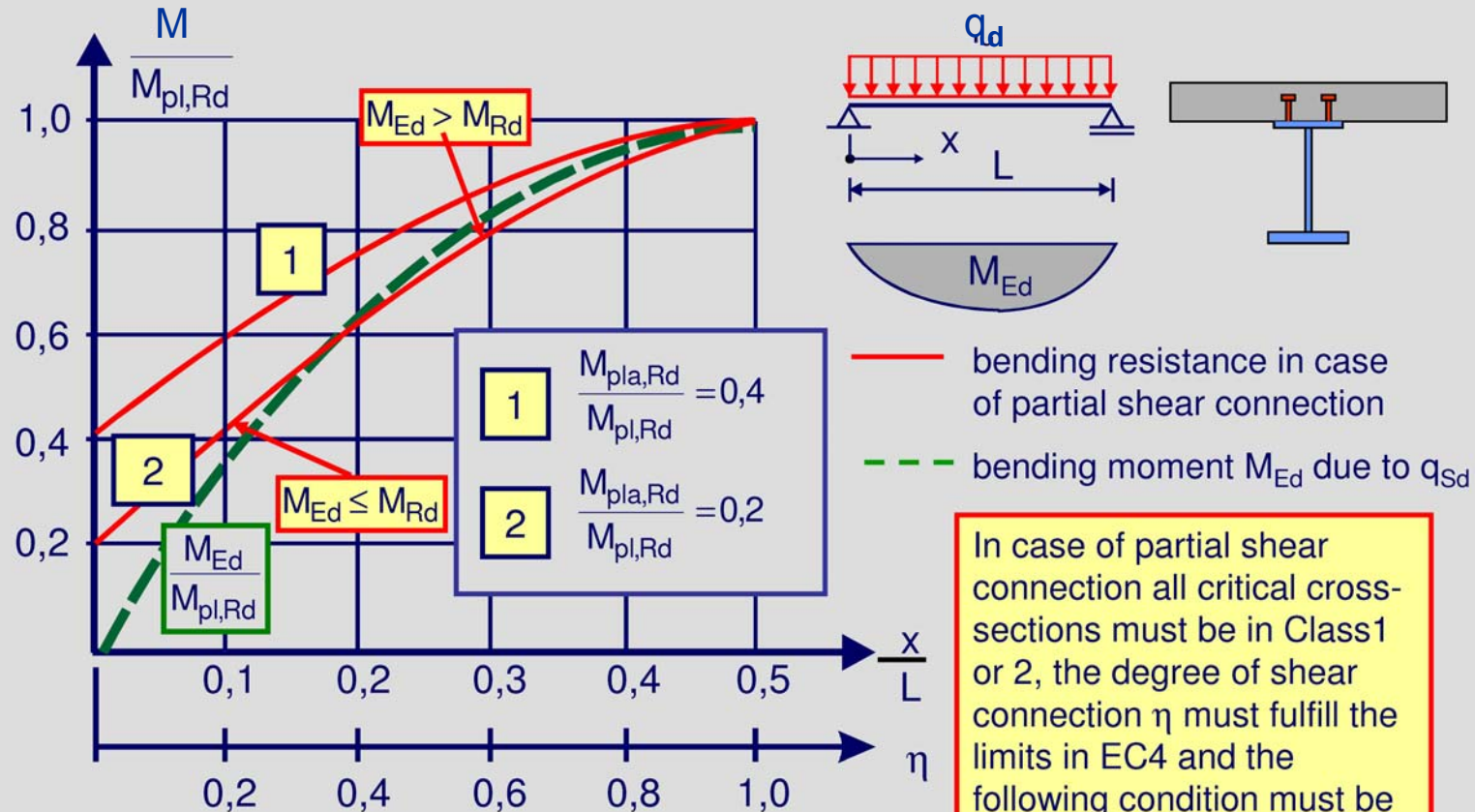


**regions with partial shear connection:** The resistance to bending is limited by the resistance to longitudinal shear in the interface between steel and concrete. Where the condition  $M_{pla,Rd} / M_{pl,Rd} > 0,4$  is not fulfilled additional checks at intermediate critical cross-sections should be made.

[Source: Hanswille]



## Requirements for shear connection – uniformly distribution



where  $M_{pl,Rd}/M_{pl,Rd}$  is smaller than 0,4, the resistance moment can be smaller the design bending moment in some regions of the beam.

In case of partial shear connection all critical cross-sections must be in Class 1 or 2, the degree of shear connection  $\eta$  must fulfill the limits in EC4 and the following condition must be satisfied:

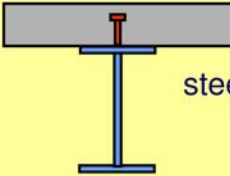
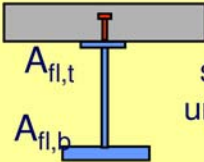
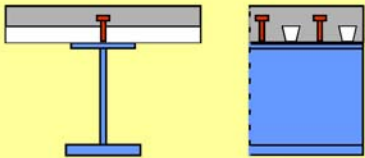
$$\frac{M_{pl,Rd}}{M_{pl,Rd}} \geq 0,4$$

[Source: Hanswille]

## Requirements for shear connection – minimum degree

$L_e$  – effective length [m]

The effective length is given by the distance between the points of zero bending moment.

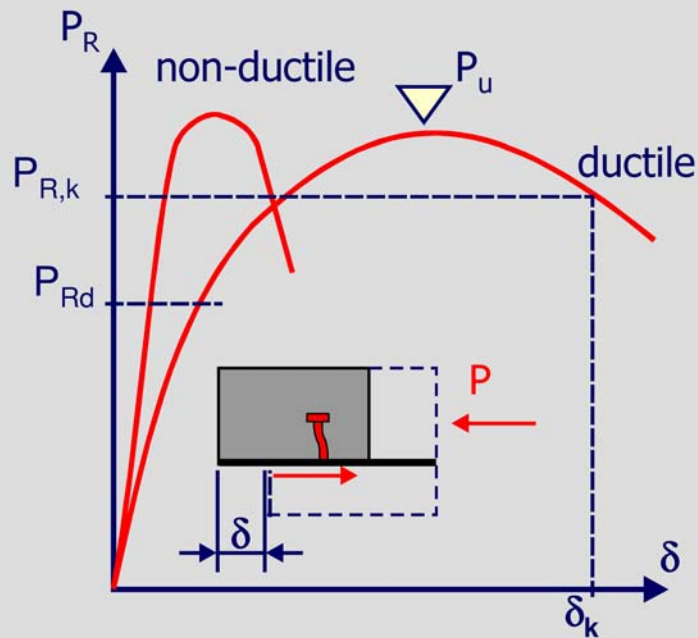
1	 <p>steel sections with equal flanges</p>	$L \leq 25\text{m}$	$\eta_{\min} \geq 1 - \frac{355}{f_{yk}} (0,75 - 0,03 \times L_e) \geq 0,4$
		$L > 25\text{m}$	$\eta_{\min} = 1$
2	 <p>steel sections with unequal flanges with <math>A_{fl,b} \leq 3 A_{fl,t}</math></p>	$L \leq 20\text{m}$	$\eta_{\min} \geq 1 - \frac{355}{f_{yk}} (0,30 - 0,015 \times L_e) \geq 0,4$
		$L > 20\text{m}$	$\eta_{\min} = 1$
3		$L \leq 25\text{m}$	$\eta_{\min} \geq 1 - \frac{355}{f_{yk}} (1,00 - 0,04 \times L_e) \geq 0,4$
		$L > 25\text{m}$	$\eta_{\min} = 1$

The minimum shear degree according to line 3 apply for steel sections with equal flanges, studs with a diameter of 19 mm and a length not smaller than 76 mm and one stud per rib of the sheeting and for sheeting with  $h_p \leq 60\text{mm}$  and  $b_o/h_p \geq 2$ .

[Source: Hanswille]

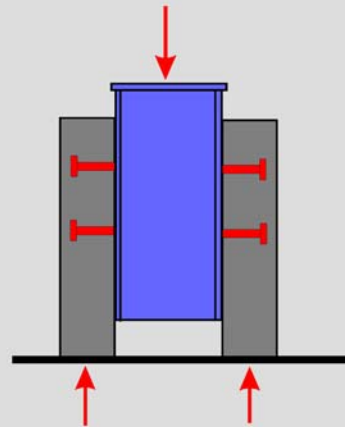
## Requirements for shear connection – ductility

Shear connectors may be classified as ductile if the characteristic slip  $\delta_k$  is at least 6 mm.

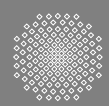


$P_{Rd}$  – design value of shear resistance

$P_{Rk}$  - characteristic value of shear resistance



[Source: Hanswille]



- **Longitudinal shear forces**

- Determination of longitudinal shear forces
- Full and partial shear connection
- Requirements for shear connectors

- **Headed studs**

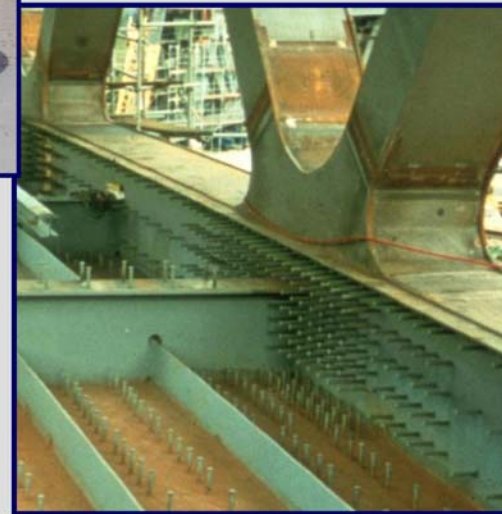
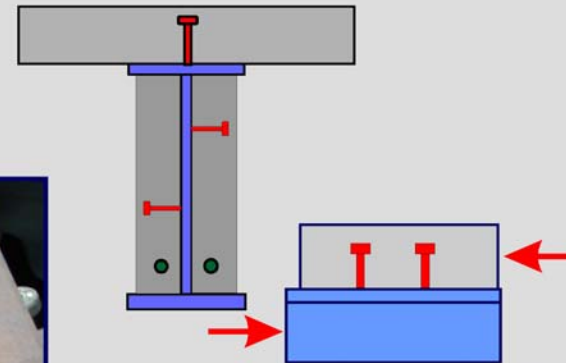
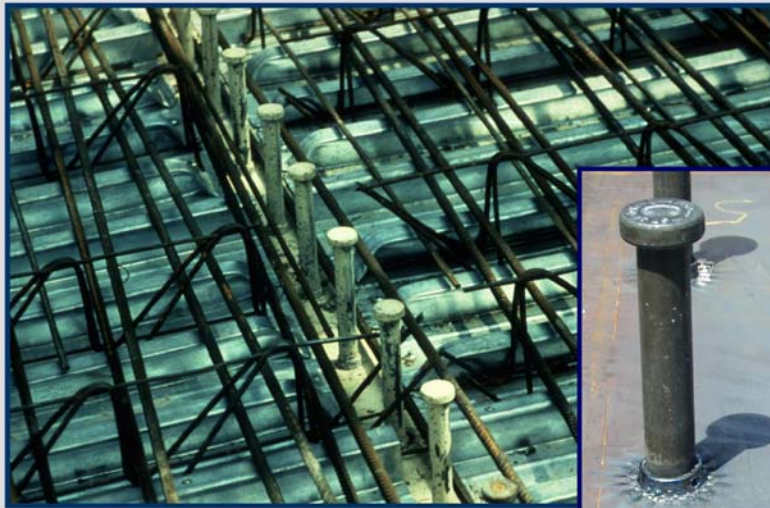
- Head studs as shear connector
- Horizontally lying studs
- Headed studs used with profiled steel sheeting

- **Longitudinal shear forces in concrete slab**





## Headed studs

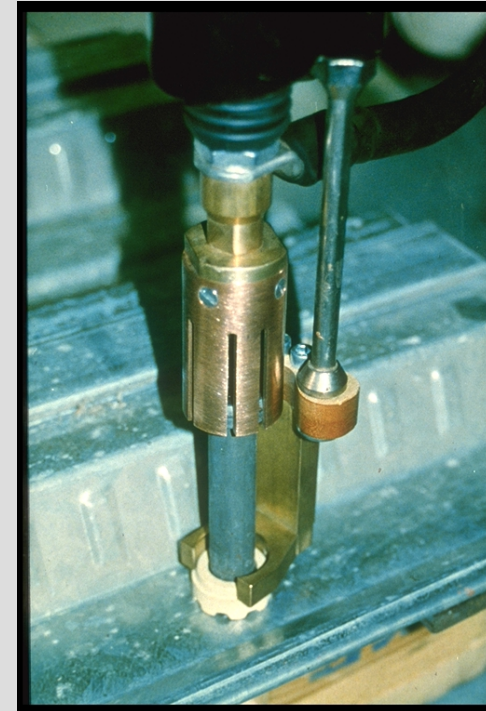
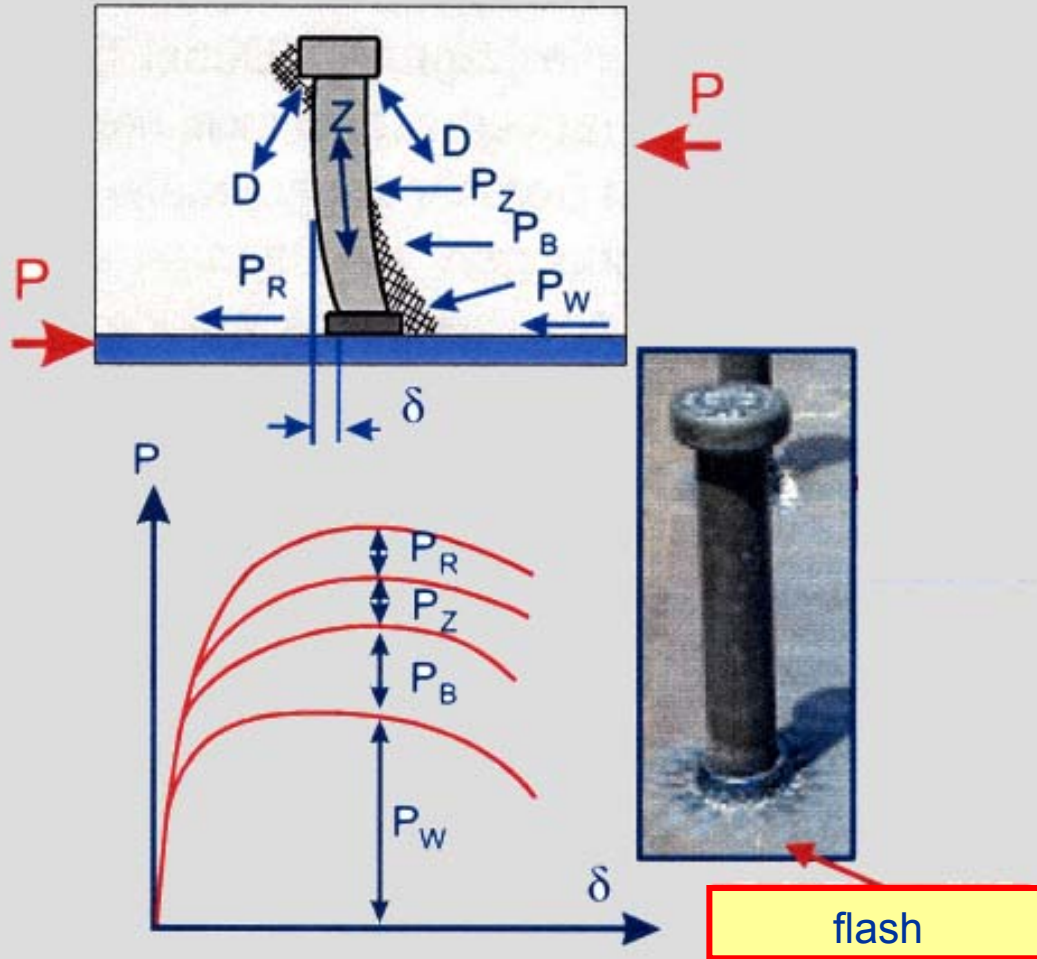


**EN ISO 13918:** Welding –Studs and ceramic ferrules for arc stud welding (1998)

**EN ISO 14555:** Welding –Arc stud welding of metallic materials(1998)

[Source: Hanswille]

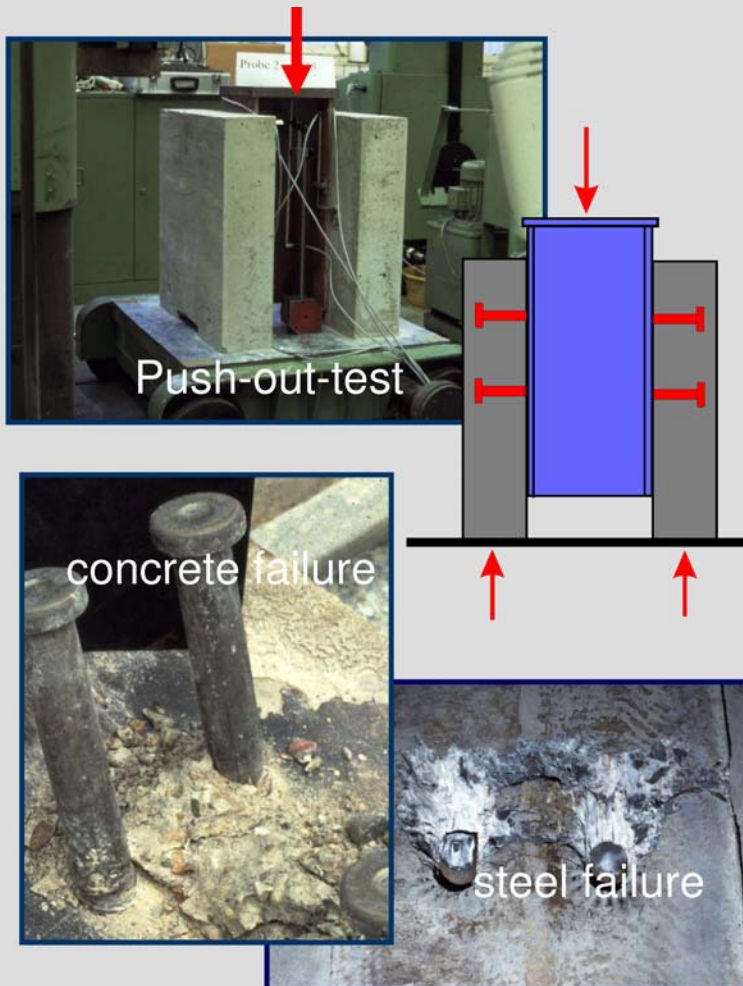
## Headed studs – typical load-slip behaviour



$P_W \dots$	flash
$P_Z \dots$	stud inclination
$P_B \dots$	stud bending
$P_R \dots$	friction



## Headed studs – design shear resistance



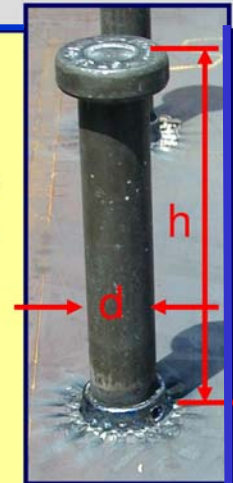
### Concrete failure:

$$P_{Rd,1} = 0.29 \alpha d^2 \sqrt{f_{ck} E_{cm}} \frac{1}{\gamma_V}$$

### Shank failure of the stud:

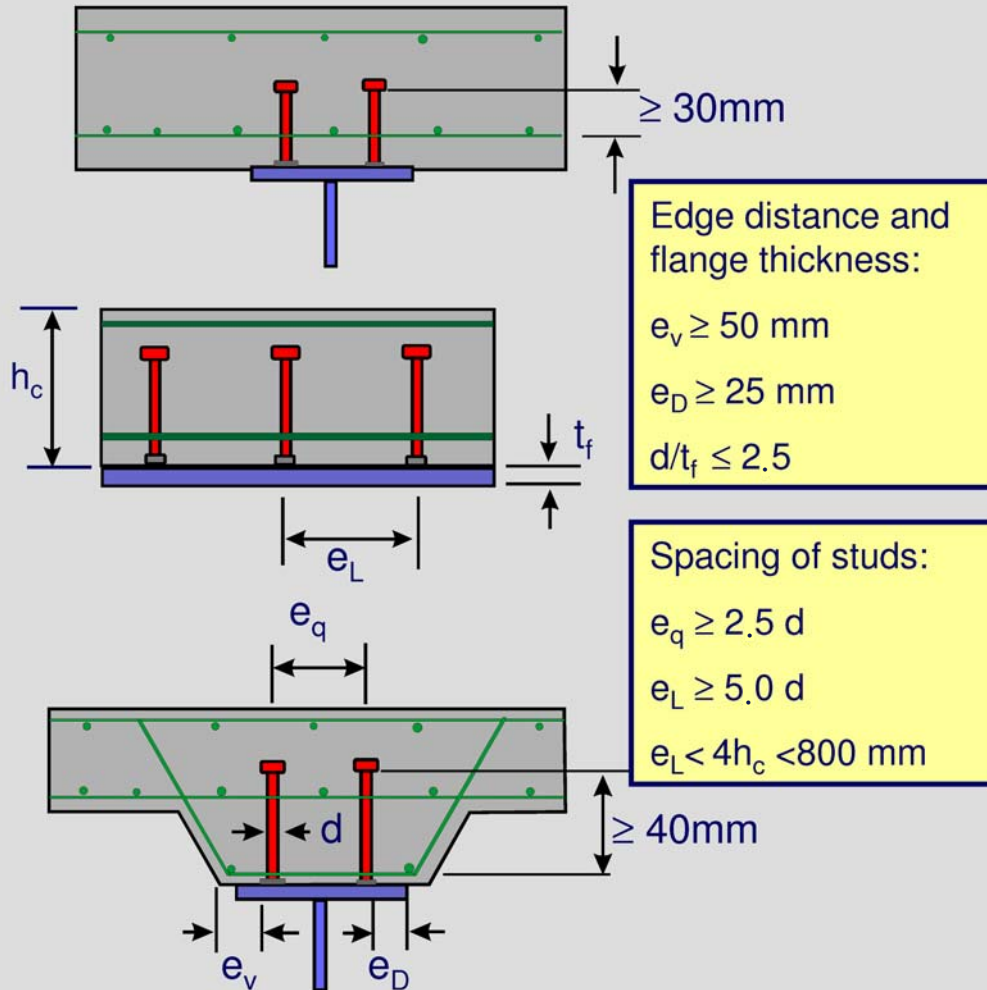
$$P_{Rd,2} = 0.8 \cdot f_u \left( \frac{\pi d^2}{4} \right) \frac{1}{\gamma_V}$$

- $d$  diameter of stud shank  $16 \leq d \leq 25\text{mm}$
- $f_u$  specified ultimate tensile strength of the stud material  $f_u \leq 500 \text{ N/mm}^2$
- $f_{ck}$  cylinder strength of concrete
- $E_{cm}$  secant modulus of elasticity of concrete
- $a = 0.2 [(h/d)+1]$  for  $3 \leq h/d \leq 4$   
 $= 1.0$  for  $h/d > 4$
- $\gamma_V = 1.5$  partial safety factor concrete failure  
 $= 1.25$  partial safety factor steel failure

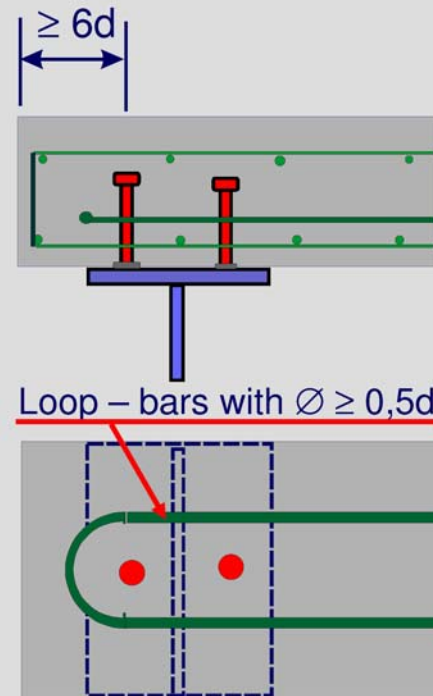


[Source:  
EC4-1  
& Hanswille]

## Headed studs – detailing

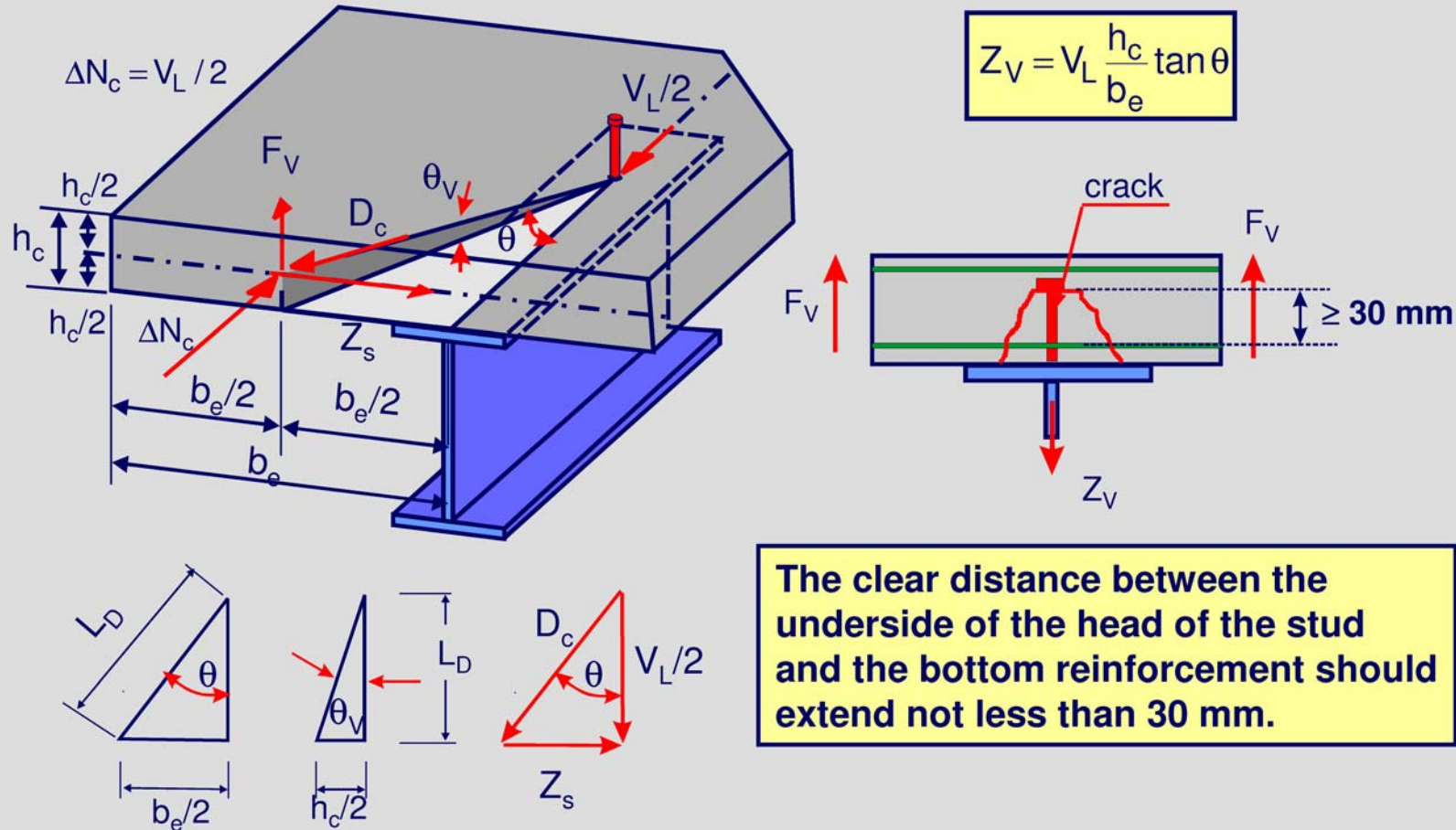


Edge beam

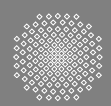


[Source: Hanswille]

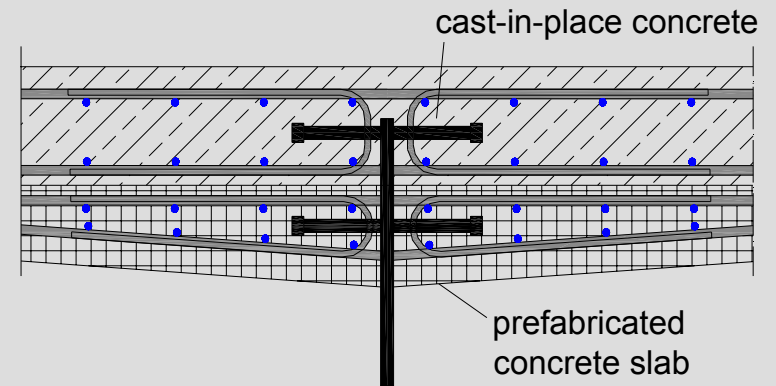
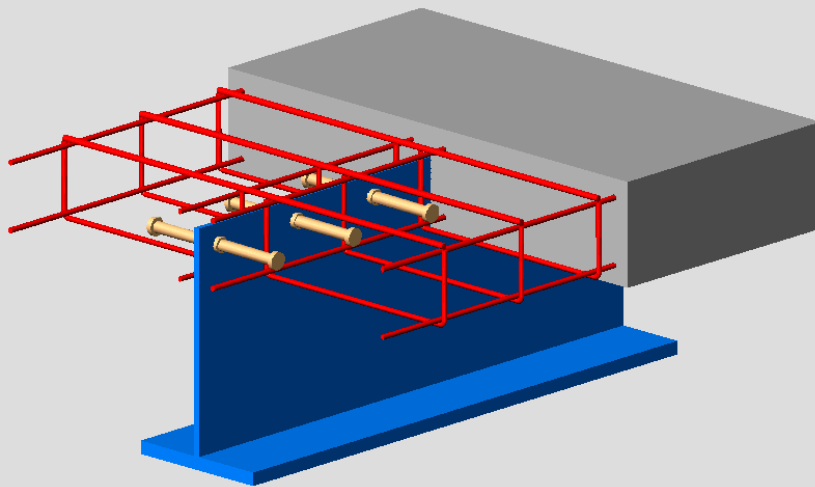
## Headed studs – uplift forces



[Source: Hanswille]



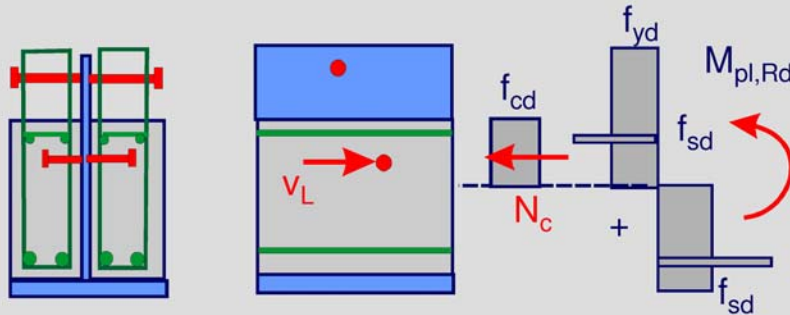
## Horizontally lying studs – examples



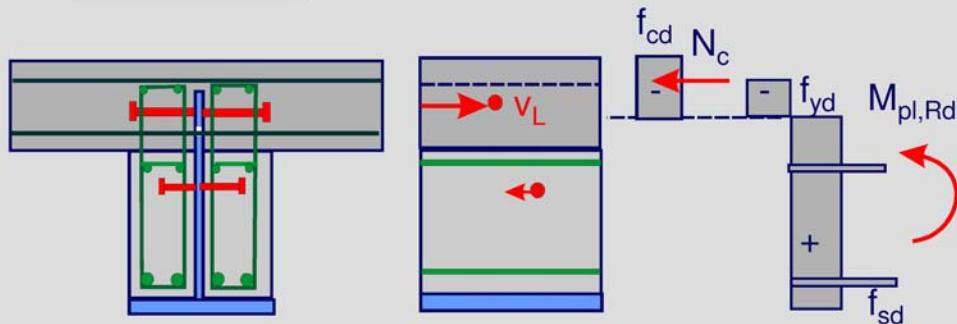


## Horizontally lying studs – examples

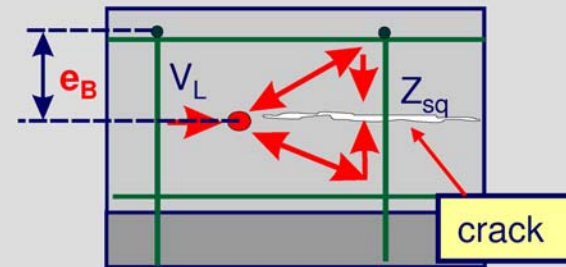
erection stage:



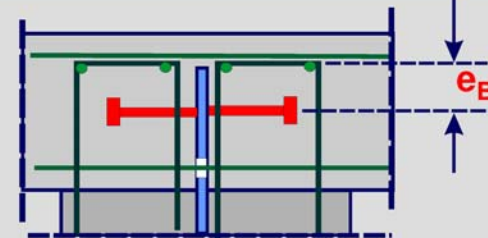
final stage:



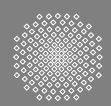
splitting forces in direction  
of slab thickness



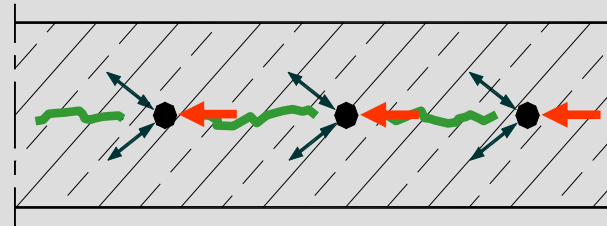
For studs with a edge distance  $e_B \geq 6d$  no reduction of strength occurs ( $d$ -diameter of the shank).



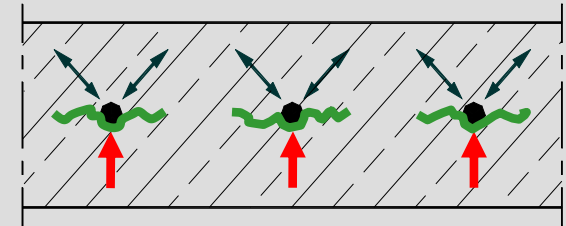
[Source: Hanswille]



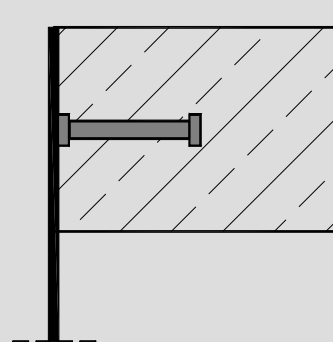
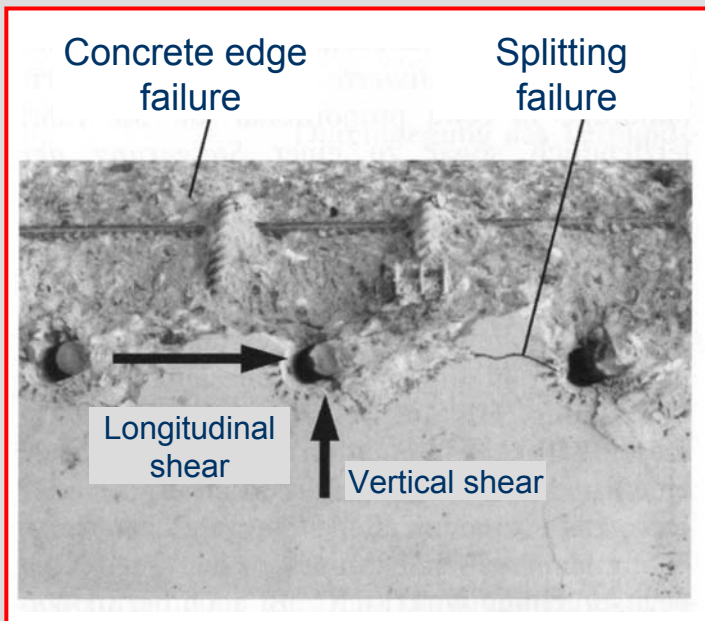
## Horizontally lying studs – failure modes and position



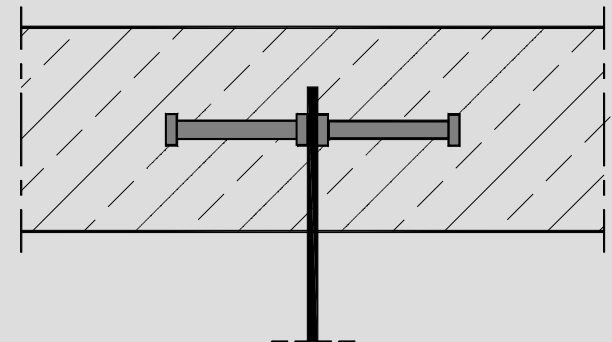
Longitudinal shear  
due to beam bending



Vertical shear  
due to vertical beam support



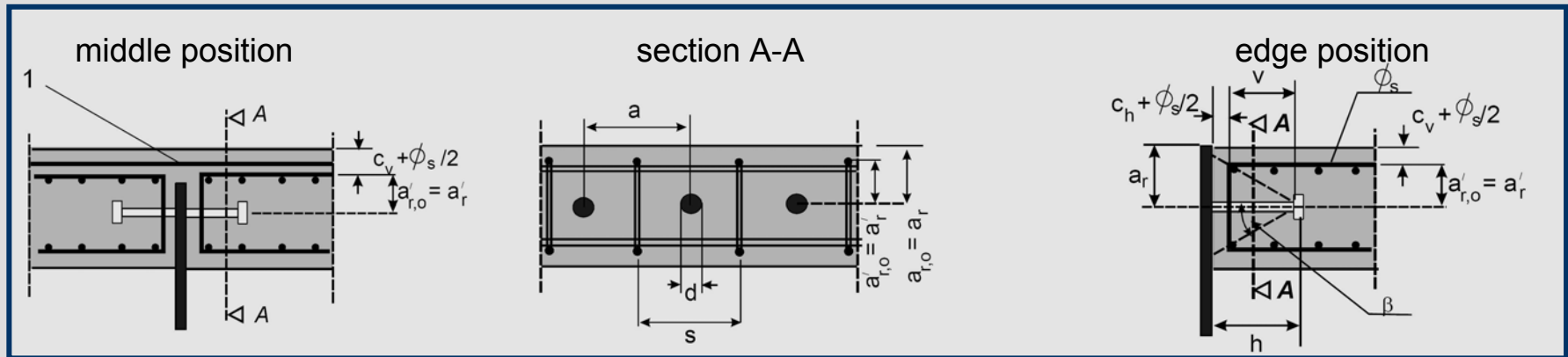
Edge position



Middle position



## Horizontally lying studs – load resistance for longitudinal shear



$$P_{Rd,L} = \frac{1.4 k_v (f_{ck} d a'_r)^{0.4} (a/s)^{0.3}}{\gamma_v}$$

stirrups  $T_d = 0.3 P_{Rd,L}$

$a'_r$  effective edge distance

$$a'_r = a_r - c_v - \phi_s/2 \geq 50 \text{ mm}$$

$k_v$  factor for position of shear connection

$k_v = 1$  edge position

$k_v = 1.4$  middle position

$\gamma_v$  partial factor 1.25

$d$  ... diameter of the stud shank  $19 \leq d \leq 25 \text{ mm}$

$h$  ... overall height of the stud  $h/d \geq 4$

$s$  ... spacing of stirrups  $a/2 \leq s \leq a$

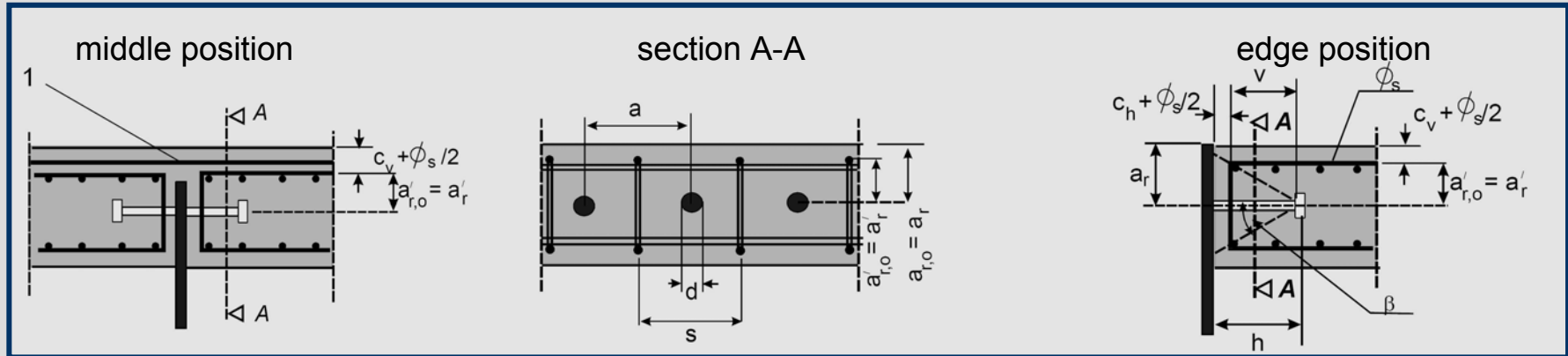
$$s/a'_r \leq 3$$

$\phi_s$  ... diameter of stirrups  $\phi_s \geq 8 \text{ mm}$

$\phi_l$  ... diameter of longitudinal reinforcement  $\phi_l \geq 10 \text{ mm}$

[Source: EN1994-2]

## Horizontally lying studs – load resistance for vertical shear



$$P_{Rd,V} = \frac{0.012 (f_{ck} \varphi_l)^{0.5} (d a / s)^{0.4} (\varphi_s)^{0.3} (a'_{r,o})^{0.7} k_v}{\gamma_v}$$

$a$  ... spacing of studs

$$110 \leq a \leq 440 \text{ mm}$$

$h$  ... overall height of the stud

$$h \geq 100 \text{ mm}$$

$\varphi_s$  ... diameter of stirrups

$$\varphi_s \geq 12 \text{ mm}$$

$\varphi_l$  ... diameter of longitudinal reinforcement

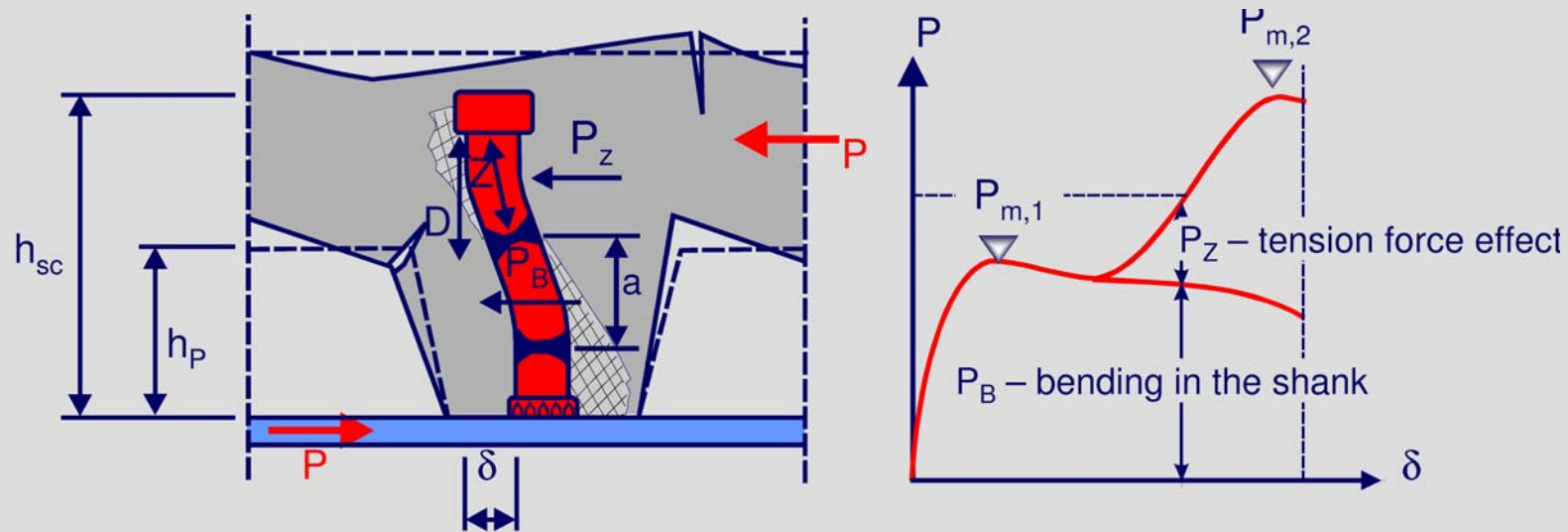
$$\varphi_l \geq 16 \text{ mm}$$

**Interaction:**

$$\left( \frac{F_{d,L}}{P_{Rd,L}} \right)^{1.2} + \left( \frac{F_{d,V}}{P_{Rd,V}} \right)^{1.2} \leq 1$$

[Source: EN1994-2]

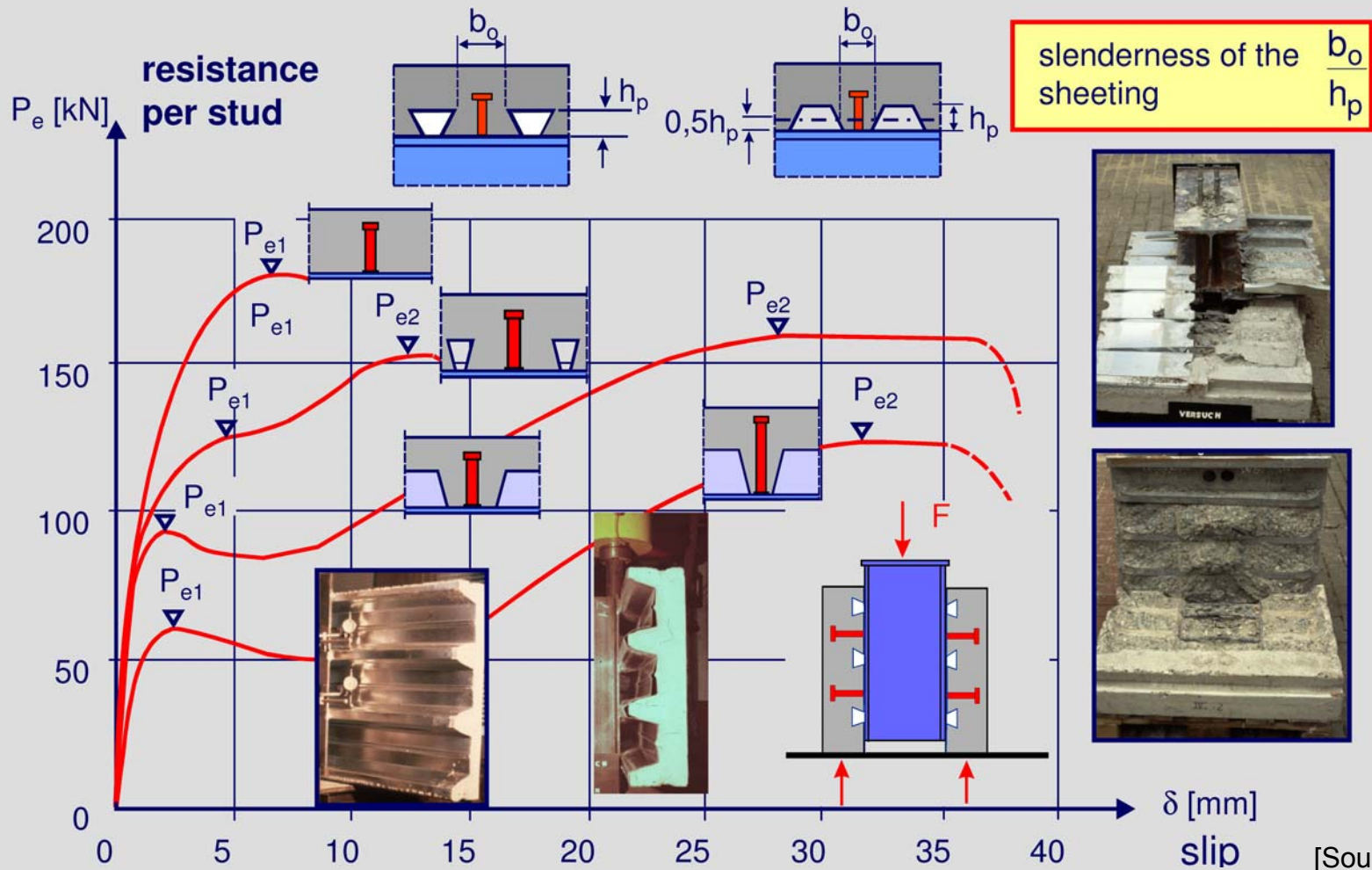
## Headed studs used with profiled steel sheeting



The resistance is significantly influenced by the geometry of the sheeting. In the stud the shear force causes bending moments. The first ultimate Load  $P_{m,1}$  is reached when in the shank of studs two plastic hinges occur. This is only possible, if the nominal height of the connector extends more than  $2d$  above the top of steel sheeting, where  $d$  is the shank diameter of the stud. In case of slender ribs a second load maximum  $P_{m,2}$  is reached. In this stage in the stud significant tension forces occur and the inclination of the studs causes an additional shear resistance. This load level is not taken into account, because significant horizontal reinforcement must be provided to prevent uplift. Otherwise rib shear failure can occur.

[Source: Hanswille]

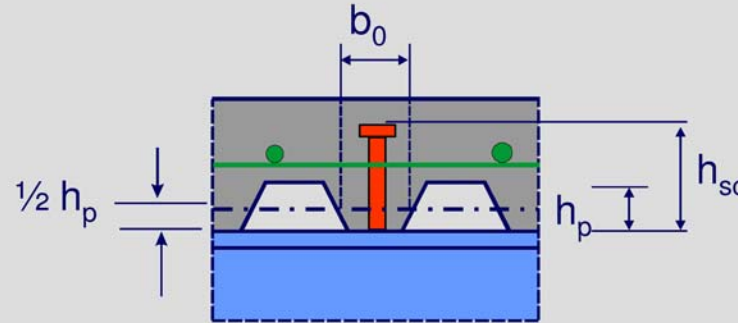
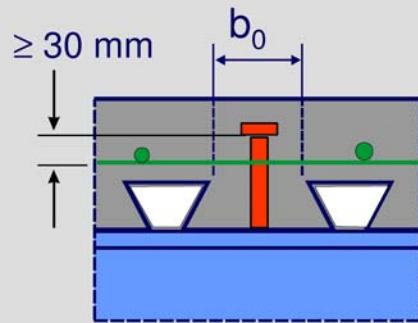
# Headed studs used with profiled steel sheeting – load-slip behaviour



[Source: Hanswille]



## Headed studs used with profiled steel sheeting – load resistance



reduction factor $k_{t,max}$			
number of studs per rib	thickness of the sheeting [mm]	studs welded through profiled steel d= 19mm	profiled steel sheeting with holes d=19 und d=22mm
$n_r=1$	$\leq 1,0$ mm	0.85	0.75
	$> 1,0$ mm	1.0	0.75
$n_r=2$	$\leq 1,0$ mm	0.70	0.60
	$> 1,0$ mm	0.80	0.60

Design resistance :

$$P_{Rd} = P_{Rd,o} k_t$$

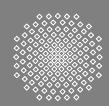
$$k_t = \frac{0.7}{\sqrt{n_r}} \frac{b_o}{h_p} \left[ \frac{h_{sc}}{h_p} - 1 \right] \leq k_{t,max}$$

$$h_p \leq 85 \text{ mm} \quad h - h_p \geq 2d$$

$$b_o \geq h_p \quad b_o \geq 50 \text{ mm}$$

$P_{Rd,o}$ - resistance of the stud in a solid slab with  $f_u = 450 \text{ N/mm}^2$

[Source: Hanswille]



- **Longitudinal shear forces**

- Determination of longitudinal shear forces
- Full and partial shear connection
- Requirements for shear connectors

- **Headed studs**

- Head studs as shear connector
- Horizontally lying studs
- Headed studs used with profiled steel sheeting

- **Longitudinal shear forces in concrete slab**





## Longitudinal shear forces in concrete slab - determination

### Slab in compression

$$V_{L,Ed} = \Delta N_c$$

Longitudinal shear per unit length:

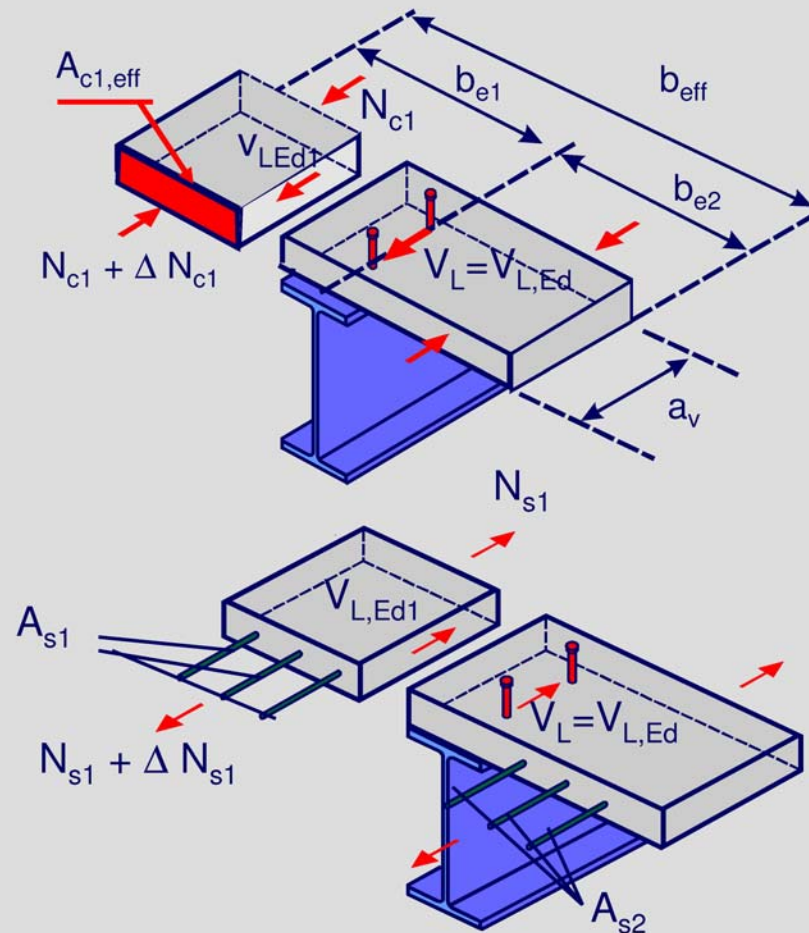
$$v_{L,Ed,1} = \frac{\Delta N_{c1}}{a_v} = \frac{V_{L,Ed}}{a_v} \frac{A_{c1,eff}}{A_{c,eff}}$$

### Slab in tension

$$V_{L,Ed} = \Delta N_s$$

Longitudinal shear per unit length:

$$v_{L,Ed,1} = \frac{\Delta N_{s1}}{a_v} = \frac{V_{L,Ed}}{a_v} \frac{A_{s1}}{A_{s1} + A_{s2}}$$



[Source: Hanswille]

## Longitudinal shear forces in concrete slab – strut-and-tie model

verification:  $V_{L,Ed} \leq V_{Rd,max}$

$V_{L,Ed} \leq V_{Rd,s}$

**Resistance of concrete struts:**

$$V_{Rd,max} = A_{cv} v f_{cd} \sin \theta \cos \theta$$

$$A_{cv} = h_c a_v \quad f_{cd} = \alpha_{cc} f_{ck} / \gamma_c$$

$v$  strength reduction factor

$$v = 0,6 (1 - (f_{ck} / 250)) \text{ with } f_{ck} \text{ in } N/mm^2$$

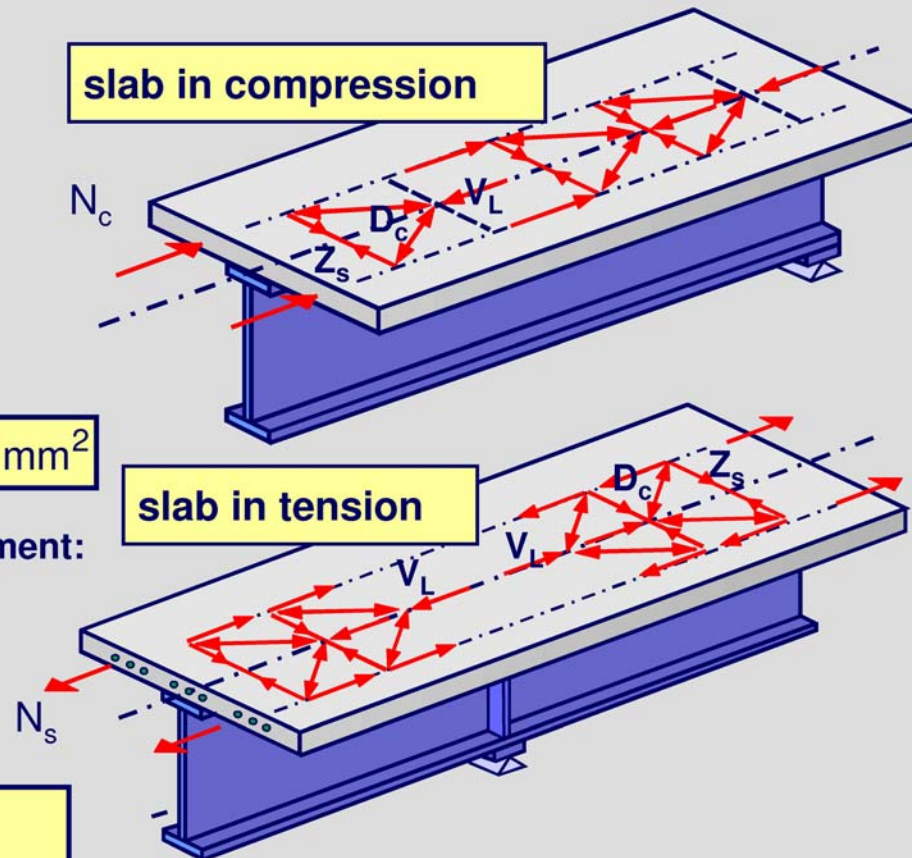
**Resistance of transverse reinforcement:**

$$V_{Rd,s} = \frac{A_{sf}}{s} a_v f_{sd} \cot \theta$$

Inclination of concrete compressive struts:

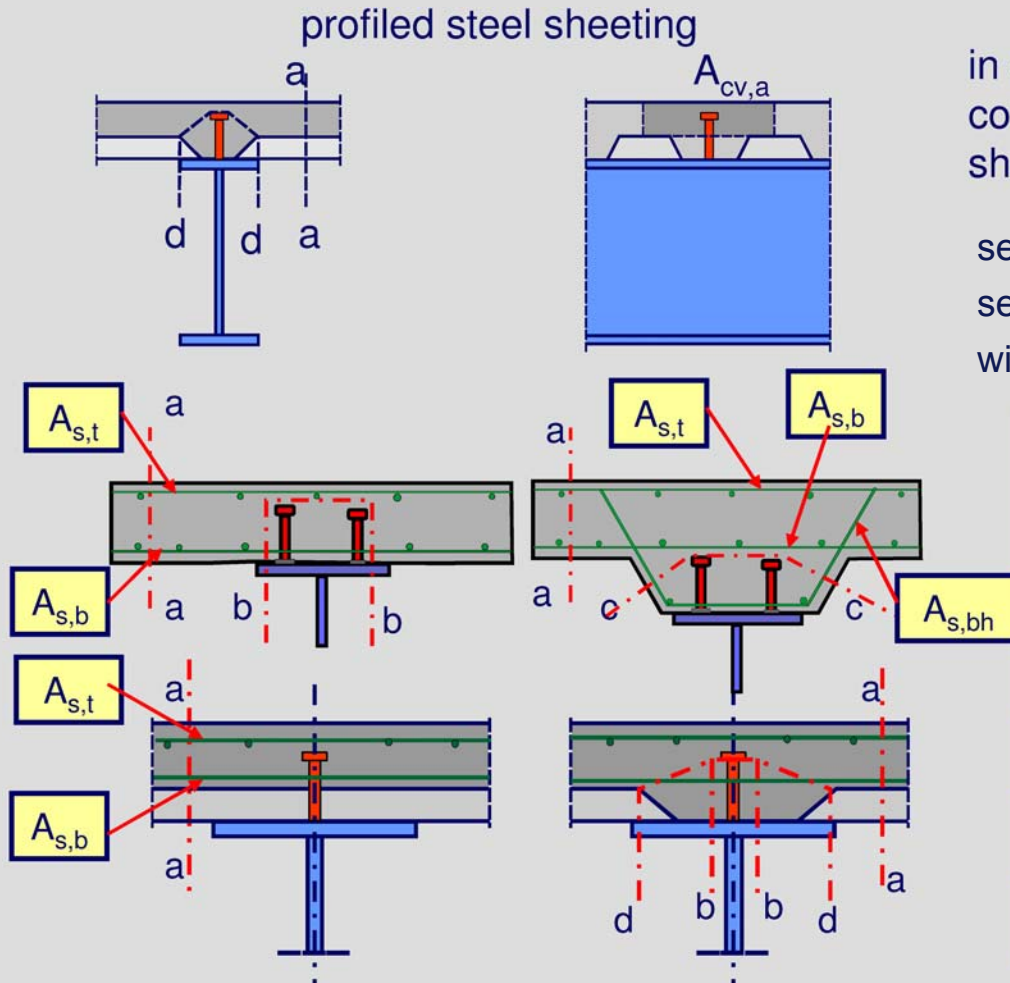
slab in compression:  $1,0 \leq \cot \theta \leq 2,0$

slab in tension:  $1,0 \leq \cot \theta \leq 1,25$



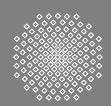
[Source: Hanswille]

## Longitudinal shear forces in concrete slab – shear plane



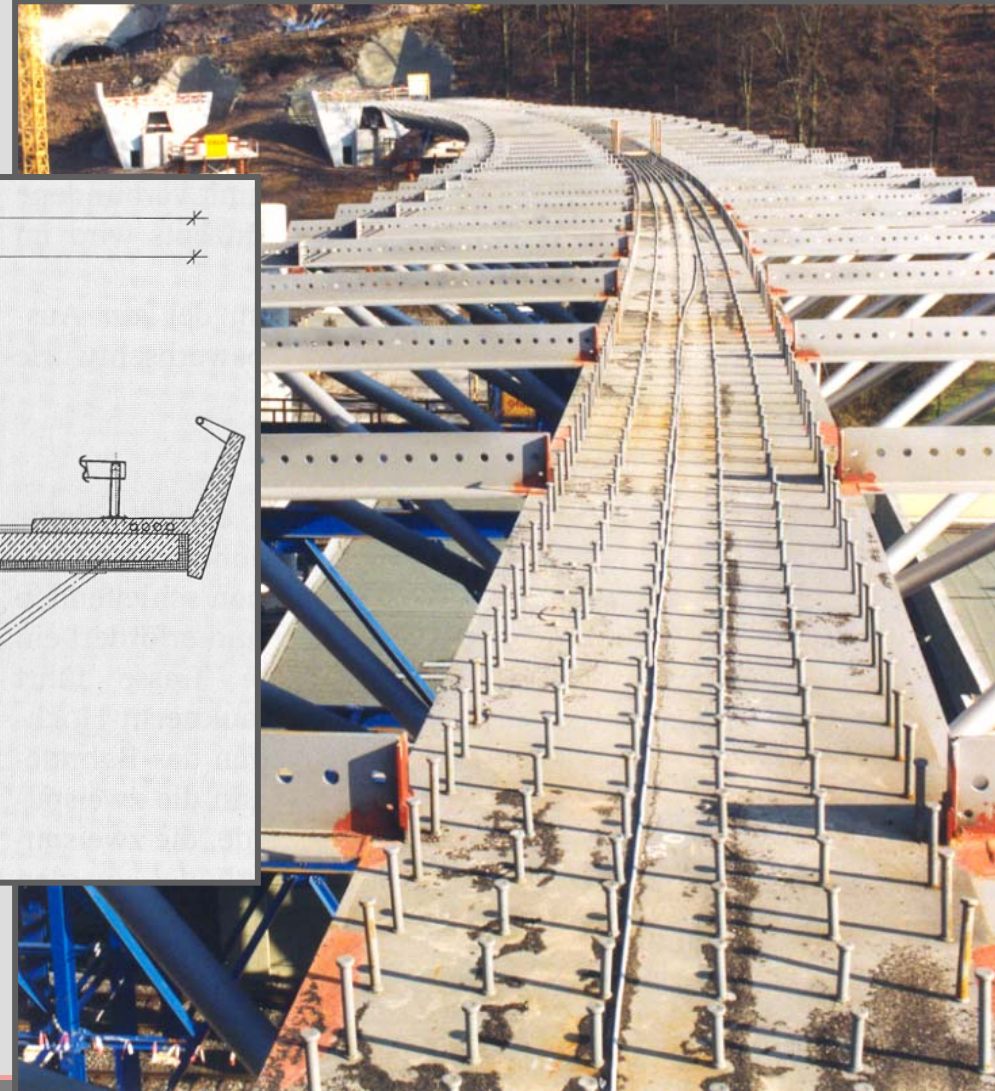
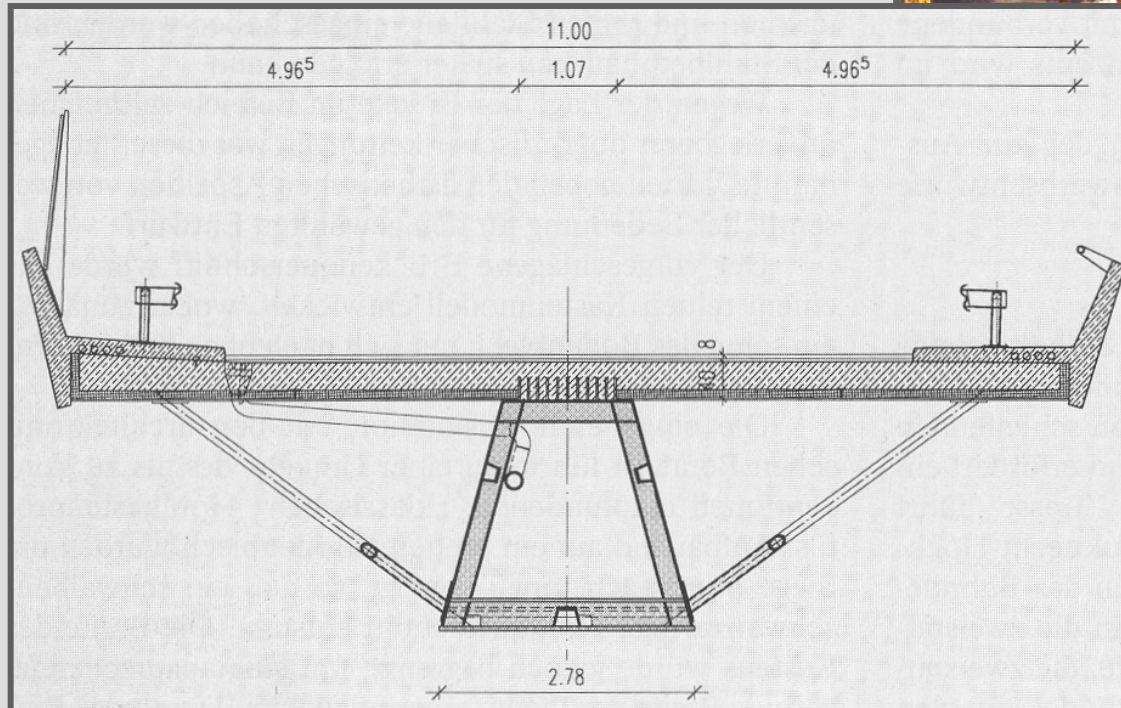
[Source: Hanswille]



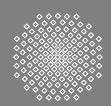


## Innovative composite bridge structures

Bridge Nesenbachtal, Stuttgart



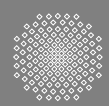




## Nesenbachtal – Result of a design competition







# Acknowledgement and many thanks to

My co-workers

Dipl.-Ing. Gunter **Hauf**

Dipl.-Ing. Matthias **Konrad**

Dipl.-Ing. Ana **Ožbolt**

Dipl.-Ing. Lars **Rölle**

Dipl.-Ing. Markus **Rybinski**

for their support

Prof. Dr.-Ing.

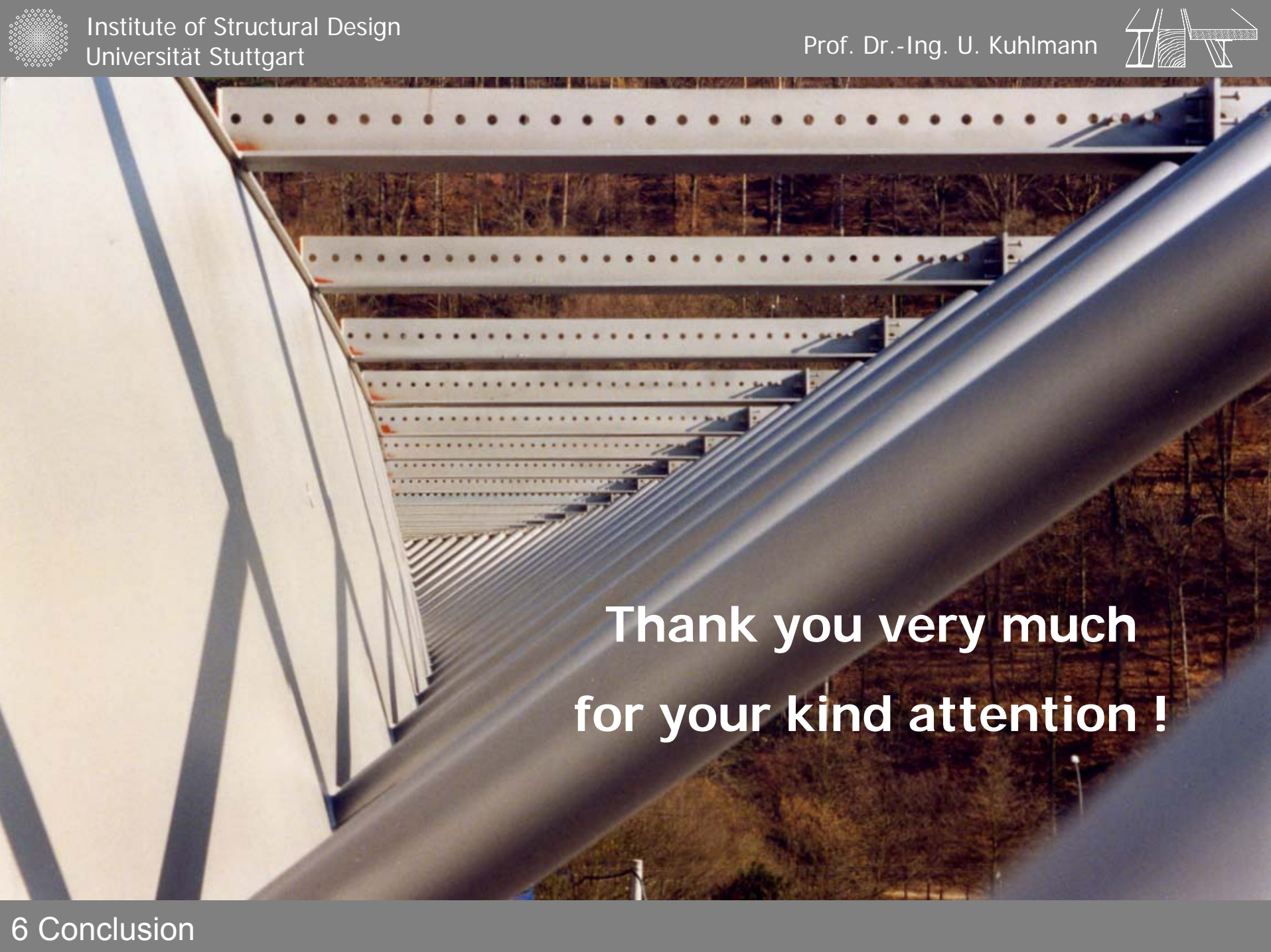
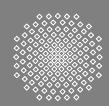
Gerhard **Hanswille**

for allowance

to base on his ppt - presentation

prepared for lectures in Riga

in 2006

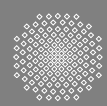


**Thank you very much  
for your kind attention !**



## Literature

- Bode, H.:* Euro-Verbundbau, Konstruktion und Berechnung, publisher Werner Verlag, Düsseldorf, 1998
- Deutsches Institut für Bautechnik:* Slim-Floor Träger mit UPE-Profilen, Allgemeine bauaufsichtliche Zulassung Nr. Z-26.2-48, Technical Approval, 2005.
- DIN 18800-5:* Steel structures – Part 5: Composite structures of steel and concrete – Design and Construction, German Standard, 2006.
- DIN EN 1994-1-1:* Design of composite steel and concrete structures: General rules and rules for buildings, European Standard, 2002
- Hanswille, G., Schäfer, M.,* Verbundtragwerke aus Stahl und Beton, Bemessung und Konstruktion - Kommentar zu DIN V 188000 Teil 5 Ausgabe November 2004, Stahlbaukalender 2005, editor Ulrike Kuhlmann, publisher Verlag Ernst & Sohn, Berlin
- Hanswille G.:* The new German design code for composite bridges,  
Engineering Foundation Conferences Composite Construction V, South Africa, Juli 2004
- Hanswille G., Bergmann R.:* New design methods for composite columns including high strength steel,  
Engineering Foundation Conferences Composite Construction V, South Africa, Juli 2004
- Hanswille G., Piel W.:* Composite shear head systems for improved punching shear resistance of flat slabs,  
Engineering Foundation Conferences Composite Construction V, South Africa, Juli 2004
- Hanswille G., Porsch M.:* Load introduction in composite columns with concrete filled hollow sections,  
Engineering Foundation Conferences Composite Construction V, South Africa, Juli 2004
- Roik, K., Bergmann, R., Haensel, J., Hanswille, G.* Verbundkonstruktionen: Bemessung auf der Grundlage des Eurocode 4 Teil 1, Betonkalender 1993, publisher Verlag Ernst & Sohn, Berlin



## Literature

- Breuninger, U.; Kuhlmann, U.:* Tragverhalten und Tragfähigkeit liegender Kopfbolzendübel unter Längsschubbeanspruchung, Stahlbau 70, p. 835-845, 2001.
- Breuninger, U.:* Zum Tragverhalten liegender Kopfbolzendübel unter Längsschubbeanspruchung, PhD-Thesis, Universität Stuttgart, Mitteilung Nr. 2000-1, 2000.
- Kuhlmann, U.; Breuninger, U.:* Behaviour of horizontally lying studs with longitudinal shear force, In: Hajjar, J.F., Hosain, M., Easterling, W.S. and Shahrooz, B.M. (eds), Composite Construction in Steel and Concrete IV, American Society of Civil Engineers, p.438-449, 2002.
- Kuhlmann, U.; Kürschner, K.:* Structural behaviour of horizontally lying shear studs, In: Leon, R.T. and Lange, J. (eds), Composite Construction in Steel and Concrete V, American Society of Civil Engineers, p.534-543, 2006.
- Kuhlmann, U.; Rieg, A.; Hauf, G.:* Effective Width Of Composite Girders With Reduced Height, Prof. Aribert - Symposium, July 2006, Institut National des Sciences Appliquées (Rennes), France, 2006.
- Kürschner, K.; Kuhlmann, U.:* Trag- und Ermüdungsverhalten liegender Kopfbolzendübel unter Quer- und Längsschub, Stahlbau 73, p.505-516, 2004.
- Kürschner, K.:* Trag- und Ermüdungsverhalten liegender Kopfbolzendübel im Verbundbau, PhD-Thesis, Universität Stuttgart, Mitteilung Nr. 2003-4, 2003.
- Raichle, J.:* Fatigue behaviour and application of horizontally lying shear studs, In: 6th International PhD Symposium in Civil Engineering, Zurich, Switzerland, 2006.
- Rybinski, M.:* Structural behaviour of steel to concrete joints on basis of the component method, In: 6th International PhD Symposium in Civil Engineering, Zurich, Switzerland, 2006.